

# **Data and Text Mining**

**Part of  
Jožef Stefan IPS Programme – ICT2**

**2020 / 2021**

**Nada Lavrač**

Jožef Stefan Institute  
Ljubljana, Slovenia

# 2020/2021 Logistics: Course lecturers

Contacts: [http://kt.ijs.si/petra\\_kralj/dmtm2.html](http://kt.ijs.si/petra_kralj/dmtm2.html)

- Data Mining:
  - Nada Lavrač: [nada.lavrac@ijs.si](mailto:nada.lavrac@ijs.si),
  - Petra Kralj Novak: [petra.kralj.novak@ijs.si](mailto:petra.kralj.novak@ijs.si),
  - Martin Žnidaršič: [martin.znidarsic@ijs.si](mailto:martin.znidarsic@ijs.si)
- Data preparation:
  - Bojan Cestnik: [bojan.cestnik@temida.si](mailto:bojan.cestnik@temida.si)
- Text mining
  - Dunja Mladenec: [dunja.mladenec@ijs.si](mailto:dunja.mladenec@ijs.si)

# Course Schedule – 2020/21

ICT2 – see [http://kt.ijs.si/petra\\_kralj/dmtm2.html](http://kt.ijs.si/petra_kralj/dmtm2.html)

4.11.2020	15:00 - 18:00	prof. dr. Nada Lavrač
11.11.2020	15:00 - 18:00	doc. dr. Petra Kralj Novak
18.11.2020	15:00 - 18:00	prof. dr. Nada Lavrač
25.11.2020	15:00 - 18:00	doc. dr. Petra Kralj Novak
2.12.2020	15:00 - 18:00	prof. dr. Bojan Cestnik
9.12.2020	15:00 - 18:00	prof. dr. Dunja Mladenić
10.12.2020	15:00 - 18:00	doc. dr. Petra Kralj Novak - Oral partial exam on Data mining
16.12.2020	15:00 - 18:00	Erik Novak
23.12.2020	15:00 - 18:00	prof. dr. Bojan Cestnik
6.1.2021	15:00 - 18:00	prof. dr. Dunja Mladenić
13.1.2021	15:00 - 18:00	prof. dr. Dunja Mladenić
20.1.2021	15:00 - 18:00	prof. dr. Nada Lavrač - Data mining seminar presentations (partial exam)
3.2.2021	15:00 - 17:00	Erik Novak

# Data and Text Mining:

## ICT2 Credits, Supporting material

- 20 credits
  - 8 credits Nada Lavrač and Petra Kralj Novak
  - 4 credits Bojan Cestnik
  - 8 credits Dunja Mladenić
- Supporting material on [videlectures.net](http://videlectures.net):  
Seminar: AI for Industry and Society, Ljubljana 2020
  - <http://videlectures.net/AIindustrySeminar2019/>
  - Marko Robnik Šikonja: Artificial Intelligence: Techniques, Trends and Applications
  - Nada Lavrač: Data Science, Machine Learning and Big Data: Current trends
  - Blaž Zupan: Data Science with the OrangeToolbox
  - Dunja Mladenić: Text Mining Applications for Industry

# Data Mining: MSc Credits and Coursework for Data mining part

Requirements for Data Mining part by Nada Lavrač  
and Petra Kralj Novak (8 ECTS credits):

- Attending lectures
- Attending practical exercises
  - Theory exercises and hands-on (intro to Orange DM toolbox by dr. Petra Kralj Novak)
- Oral exam (40%)
- Seminar (60%):
  - Data analysis of your own data (e.g., using Orange for questionnaire data analysis)
  - .... own initiatives are welcome ...

# Data Mining: MSc Credits and coursework

**Exam:** Oral exam - Theory

**Seminar: topic selection + results presentation**

- One hour available for seminar topic discussion – one page written proposal defining the task and the selected dataset
- Deliver written report + electronic copy (4 pages in Information Society paper format, instructions on the web)
  - Report on data analysis of own data needs to follow the CRISP-DM methodology
  - Presentation of your seminar results (15 minutes each: 10 minutes presentation + 5 minutes discussion)

# Course Outline

## I. Introduction

- Data Mining and KDD process
- Introduction to Data Mining
- Data Mining platforms

## II. Predictive DM

- Decision Tree learning
- Bayesian classifier
- Classification rule learning
- Classifier evaluation

## III. Predictive DM

- Regression

## IV. Descriptive DM

- Predictive vs. descriptive induction
- Subgroup discovery
- Association rule learning
- Hierarchical clustering

# Part I. Introduction

- Data Mining and the KDD process
- Introduction to Data Mining
- Data Mining platforms



# Machine Learning and Data Mining

- **Machine Learning (ML)** – computer algorithms/machines that learn predictive models from class-labeled data
- **Data Mining (DM)** – extraction of useful information from data: discovering relationships and patterns that have not previously been known, and use of **ML** techniques applied to solving real-life data analysis problems
- **Knowledge discovery in databases (KDD)** – the process of knowledge discovery

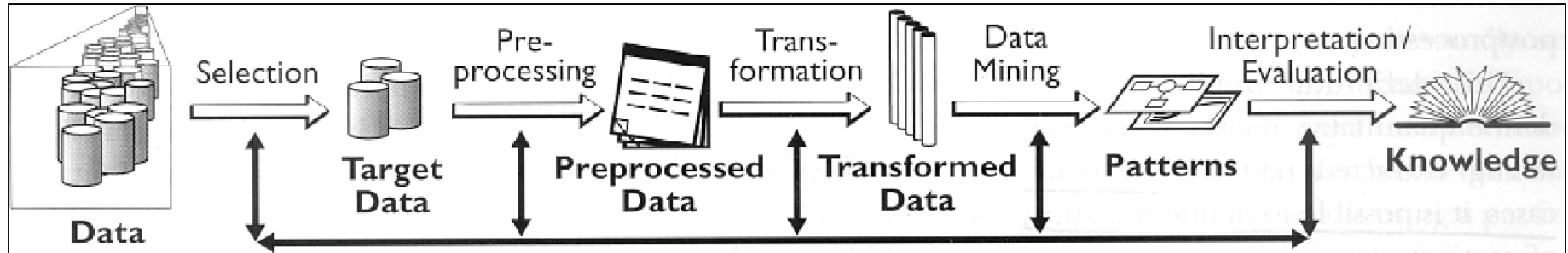
# Data Mining and KDD

- Buzzword since 1996
- KDD is defined as “the process of identifying valid, novel, potentially useful and ultimately understandable models/patterns in data.” \*
- Data Mining (DM) is the key step in the KDD process, performed by using data mining techniques for extracting models or interesting patterns from the data.

*Usama M. Fayyad, Gregory Piatetsky-Shapiro, Pedhraic Smyth: The KDD Process for Extracting Useful Knowledge from Volumes of Data. Comm ACM, Nov 96/Vol 39 No 11*

# KDD Process: CRISP-DM

KDD process of discovering useful knowledge from data

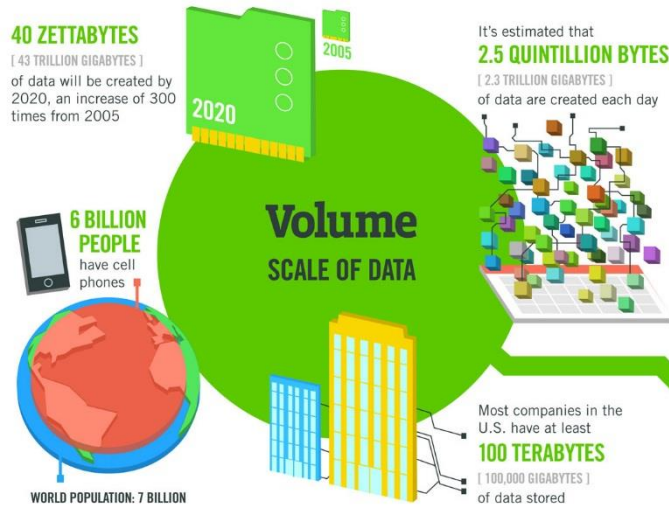


- KDD process involves several phases:
  - data preparation
  - data mining (machine learning, statistics)
  - evaluation and use of discovered patterns
- Data mining is the key step, but represents only 15%-25% of the entire KDD process

# Big Data

- **Big Data** – Buzzword since 2008 (special issue of Nature on Big Data)
  - data and techniques for dealing with very large volumes of data, possibly dynamic data streams
  - requiring large data storage resources, special algorithms for parallel computing architectures.

# The 4 Vs of Big Data



## The FOUR V's of Big Data

From traffic patterns and music downloads to web history and medical records, data is recorded, stored, and analyzed to enable the technology and services that the world relies on every day. But what exactly is big data, and how can these massive amounts of data be used?

As a leader in the sector, IBM data scientists break big data into four dimensions: **Volume, Velocity, Variety and Veracity**

Depending on the industry and organization, big data encompasses information from multiple internal and external sources such as transactions, social media, enterprise content, sensors and mobile devices. Companies can leverage data to adapt their products and services to better meet customer needs, optimize operations and infrastructure, and find new sources of revenue.

By 2015  
**4.4 MILLION IT JOBS**  
will be created globally to support big data, with 1.9 million in the United States



As of 2011, the global size of data in healthcare was estimated to be

**150 EXABYTES**  
[ 161 BILLION GIGABYTES ]



**30 BILLION PIECES OF CONTENT**  
are shared on Facebook every month



By 2014, it's anticipated there will be **420 MILLION WEARABLE, WIRELESS HEALTH MONITORS**

**4 BILLION+ HOURS OF VIDEO**  
are watched on YouTube each month



**400 MILLION TWEETS**  
are sent per day by about 200 million monthly active users

**Variety DIFFERENT FORMS OF DATA**



The New York Stock Exchange captures **1 TB OF TRADE INFORMATION** during each trading session



Modern cars have close to **100 SENSORS** that monitor items such as fuel level and tire pressure

**Velocity ANALYSIS OF STREAMING DATA**

By 2016, it is projected there will be

**18.9 BILLION NETWORK CONNECTIONS**

— almost 2.5 connections per person on earth



**1 IN 3 BUSINESS LEADERS**

don't trust the information they use to make decisions



Poor data quality costs the US economy around

**\$3.1 TRILLION A YEAR**



**27% OF RESPONDENTS**

**Veracity UNCERTAINTY OF DATA**

in one survey were unsure of how much of their data was inaccurate

# Data Science

- **Data Science** – buzzword since 2012 when Harvard Business Review called it "The Sexiest Job of the 21st Century"
  - an interdisciplinary field that uses scientific methods, processes, algorithms and systems to extract knowledge and insights from data in various forms, both structured and unstructured, similar to **data mining**.
  - used interchangeably with earlier concepts like business analytics, business intelligence, predictive modeling, and statistics.

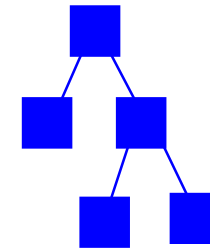
# Machine Learning and Data Mining

data

Person	Age	Spect. presc.	Astigm.	Tear prod.	Lenses
O1	17	myope	no	reduced	NONE
O2	23	myope	no	normal	SOFT
O3	22	myope	yes	reduced	NONE
O4	27	myope	yes	normal	HARD
O5	19	hypermetrope	no	reduced	NONE
O6-O13	...	...	...	...	...
O14	35	hypermetrope	no	normal	SOFT
O15	43	hypermetrope	yes	reduced	NONE
O16	39	hypermetrope	yes	normal	NONE
O17	54	myope	no	reduced	NONE
O18	62	myope	no	normal	NONE
O19-O23	...	...	...	...	...
O24	56	hypermetrope	yes	normal	NONE

knowledge discovery  
from data

Machine Learning  
Data Mining



model, patterns, ...

data

**Given:** class labeled data

**Find:** a classification model, a set of interesting patterns

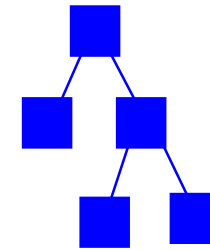
# Machine Learning and Data Mining

data

Person	Age	Spect. presc.	Astigm.	Tear prod.	Lenses
O1	17	myope	no	reduced	NONE
O2	23	myope	no	normal	SOFT
O3	22	myope	yes	reduced	NONE
O4	27	myope	yes	normal	HARD
O5	19	hypermetrope	no	reduced	NONE
O6-O13	...	...	...	...	...
O14	35	hypermetrope	no	normal	SOFT
O15	43	hypermetrope	yes	reduced	NONE
O16	39	hypermetrope	yes	normal	NONE
O17	54	myope	no	reduced	NONE
O18	62	myope	no	normal	NONE
O19-O23	...	...	...	...	...
O24	56	hypermetrope	yes	normal	NONE

knowledge discovery  
from data

Machine Learning  
Data Mining



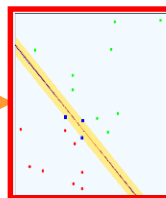
model, patterns, ...

data

**Given:** class labeled data

**Find:** a classification model, a set of interesting patterns

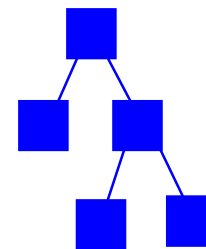
new unclassified instance



classified instance



black box classifier  
no explanation



symbolic model  
symbolic patterns

explanation

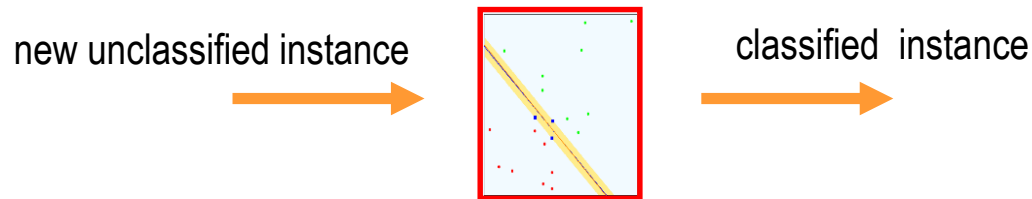




# Why learn and use black-box models

**Given:** the learned classification model  
(e.g, a linear classifier, a deep neural network, ...)

**Find:** - the class label for a new unlabeled instance



## Advantages:

- best classification results in image recognition and other complex classification tasks

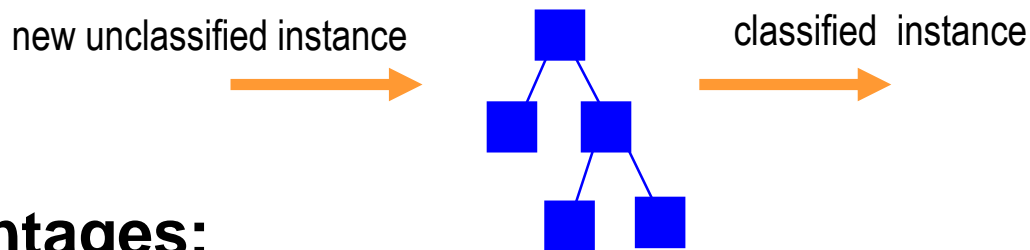
## Drawbacks:

- poor interpretability of results
- can not be used for pattern analysis

# Why learn and use symbolic models

**Given:** the learned classification model  
(a decision tree or a set of rules)

**Find:** - the class label for a new unlabeled instance



## Advantages:

- use the model for the explanation of classifications of new data instances
- use the discovered patterns for data exploration

## Drawbacks:

- lower accuracy than deep NNs

# Simplified example: Learning a classification model from contact lens data

Person	Age	Spect. presc.	Astigm.	Tear prod.	Lenses
O1	17	myope	no	reduced	NONE
O2	23	myope	no	normal	SOFT
O3	22	myope	yes	reduced	NONE
O4	27	myope	yes	normal	HARD
O5	19	hypermetrope	no	reduced	NONE
O6-O13	...	...	...	...	...
O14	35	hypermetrope	no	normal	SOFT
O15	43	hypermetrope	yes	reduced	NONE
O16	39	hypermetrope	yes	normal	NONE
O17	54	myope	no	reduced	NONE
O18	62	myope	no	normal	NONE
O19-O23	...	...	...	...	...
O24	56	hypermetrope	yes	normal	NONE

# Pattern discovery in Contact lens data

Person	Age	Spect. presc.	Astigm.	Tear prod.	Lenses
O1	17	myope	no	reduced	NONE
O2	23	myope	no	normal	SOFT
O3	22	myope	yes	reduced	NONE
O4	27	myope	yes	normal	HARD
O5	19	hypermetrope	no	reduced	NONE
O6-O13	...	...	...	...	...
O14	35	hypermetrope	no	normal	SOFT
O15	43	hypermetrope	yes	reduced	NONE
O16	39	hypermetrope	yes	normal	NONE
O17	54	myope	no	reduced	NONE
O18	62	myope	no	normal	NONE
O19-O23	...	...	...	...	...
O24	56	hypermetrope	yes	normal	NONE

**PATTERN**

**Rule:**

IF

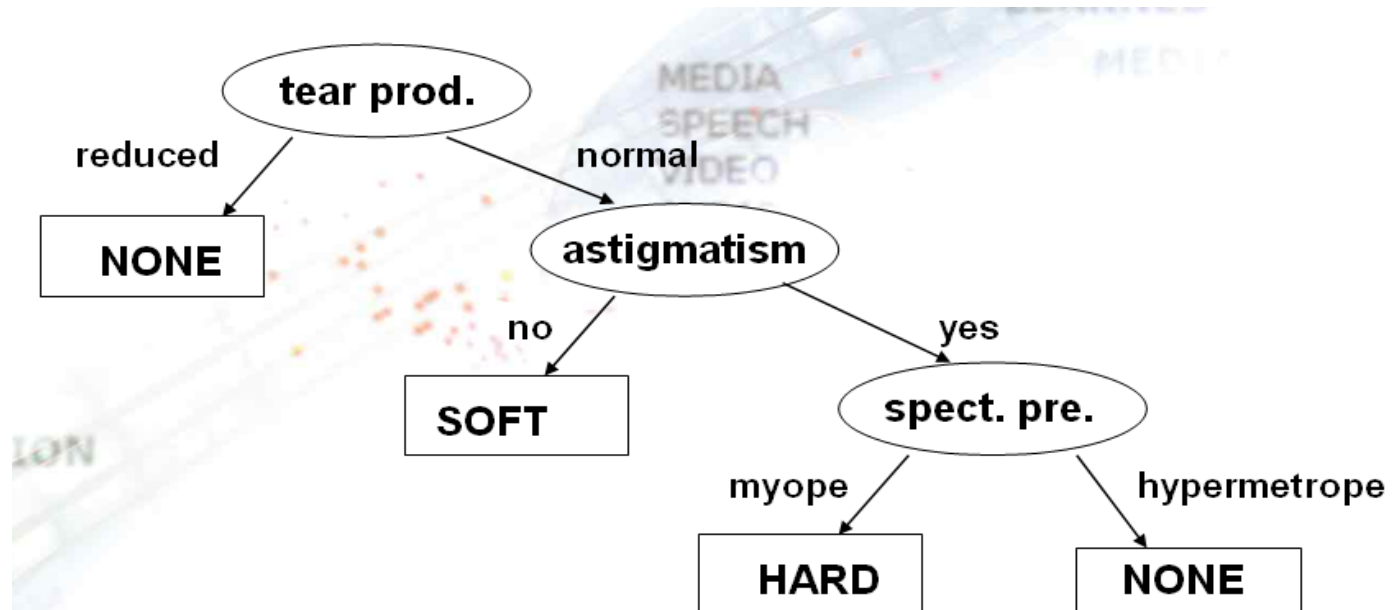
Tear prod. =  
reduced

THEN

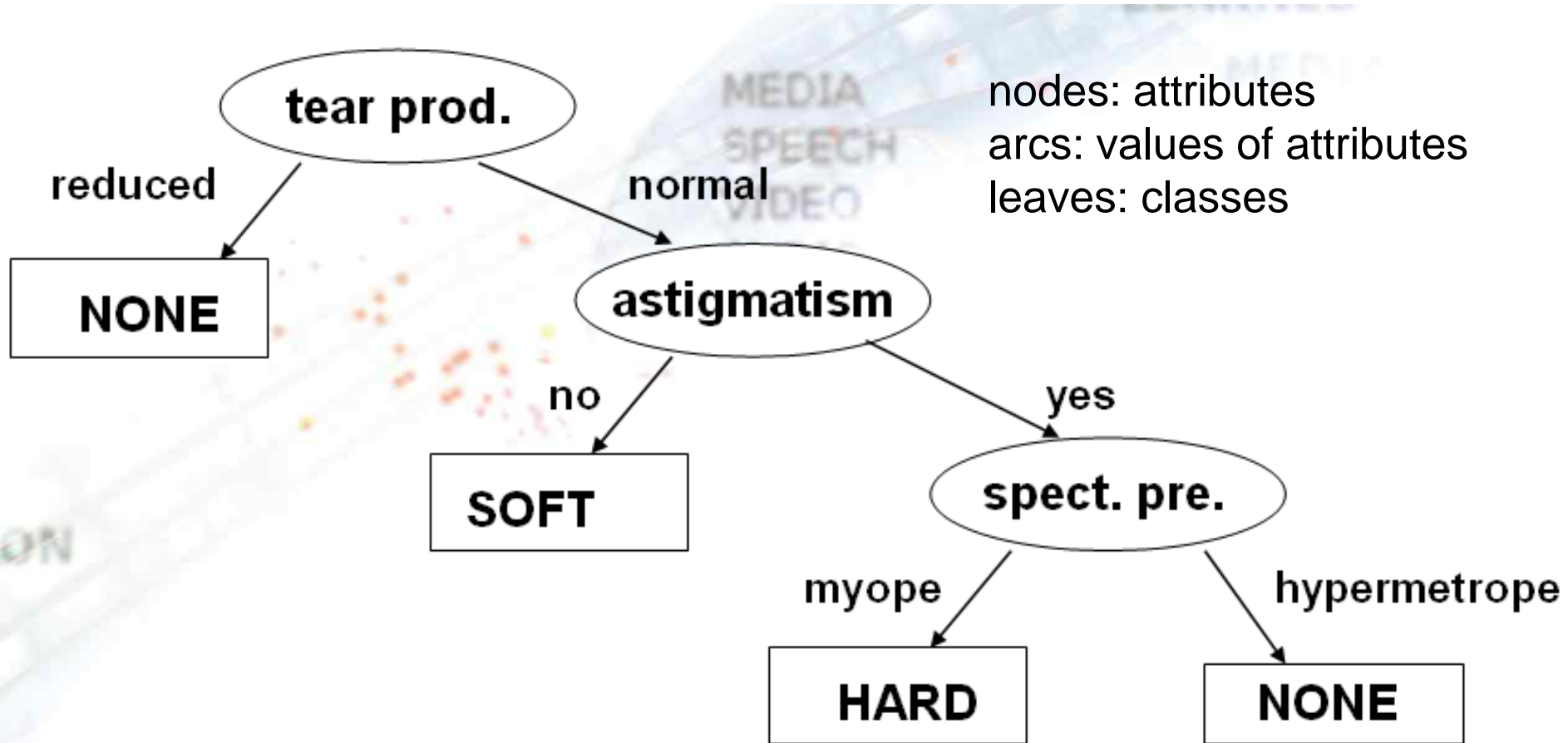
Lenses =  
NONE

# Learning a classification model from contact lens data

Person	Age	Spect. presc.	Astigm.	Tear prod.	Lenses
O1	young	myope	no	reduced	NONE
O2	young	myope	no	normal	SOFT
O3	young	myope	yes	reduced	NONE
O4	young	myope	yes	normal	HARD
O5	young	hypermetrope	no	reduced	NONE
O6-O13	...	...	...	...	...
O14	pre-presbyc	hypermetrope	no	normal	SOFT
O15	pre-presbyc	hypermetrope	yes	reduced	NONE
O16	pre-presbyc	hypermetrope	yes	normal	NONE
O17	presbyopic	myope	no	reduced	NONE
O18	presbyopic	myope	no	normal	NONE
O19-O23	...	...	...	...	...
O24	presbyopic	hypermetrope	yes	normal	NONE

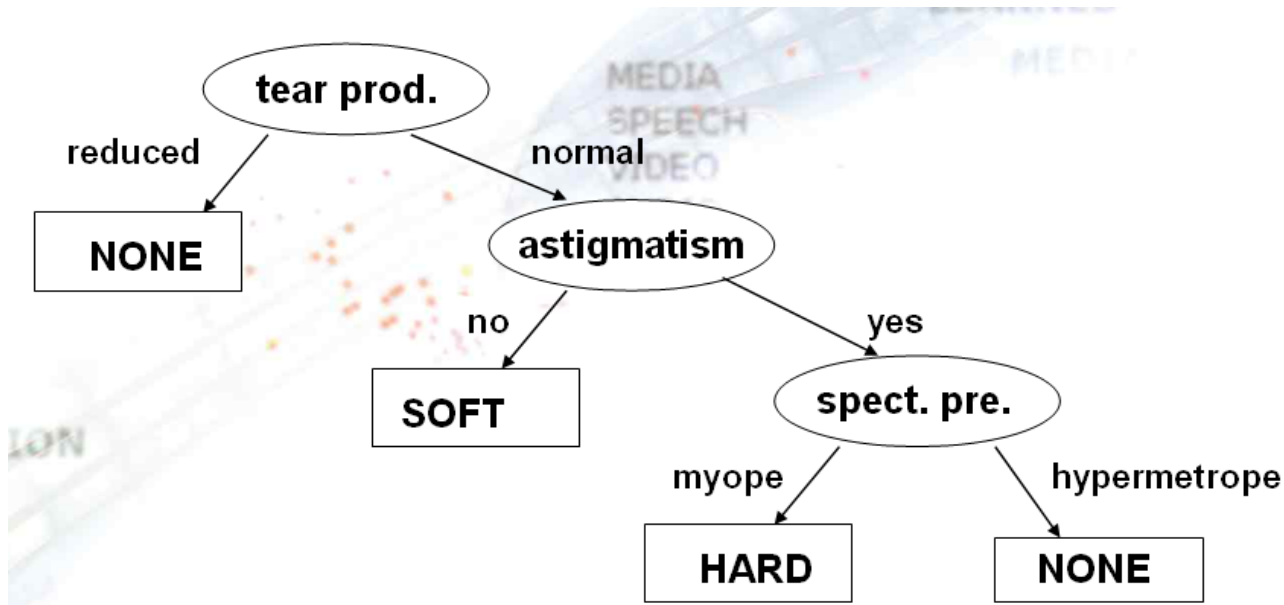


# Decision tree classification model learned from contact lens data



# Learning a decision tree classification model

23



Using  $\text{Gain}(S, A)$  heuristic for determining the most informative attribute

$$\text{Gain}(S, A) = E(S) - \sum_{v \in \text{Values}(A)} p_v \cdot E(S_v)$$

$\text{Gain}(S, A)$  estimates the reduction of entropy of set  $S$  after splitting into subsets based on values of attribute  $A$

# Heuristics for estimating the informativity of attributes and features

- **Search heuristics:** Which attribute to test at each node in the tree ?  
The attribute that is most useful for classifying examples.
- Define a statistical property, called **information gain**, measuring how well a given attribute separates the training examples w.r.t their target classification.
- First define a measure commonly used in information theory, called **entropy**, to characterize the (im)purity of an arbitrary collection of examples, and **Informativity of an attribute** measured as **reduction of entropy of a training set**
- **Entropy:**  $E(S) = - p_+ \log_2 p_+ - p_- \log_2 p_-$ .
- **Most informative attribute:**
  - Select S
  - Select A to split S into  $S_1, S_2, \dots, S_v$
  - Select A, which maximizes info. Gain

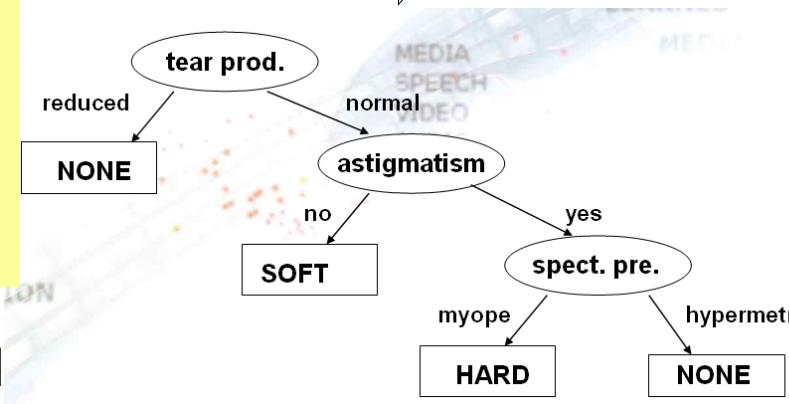
$$\max_{A} \text{Gain}(S, A)$$

$$\text{Gain}(S, A) = E(S) - \sum_{v \in \text{Values}(A)} \frac{|S_v|}{|S|} \cdot E(S_v)$$



# Learning a classification model from contact lens data

Person	Age	Spect. presc.	Astigm.	Tear prod.	Lenses
O1	17	myope	no	reduced	NONE
O2	23	myope	no	normal	SOFT
O3	22	myope	yes	reduced	NONE
O4	27	myope	yes	normal	HARD
O5	19	hypermetrope	no	reduced	NONE
O6-O13	...	...	...	...	...
O14	35	hypermetrope	no	normal	SOFT
O15	43	hypermetrope	yes	reduced	NONE
O16	39	hypermetrope	yes	normal	NONE
O17	54	myope	no	reduced	NONE
O18	62	myope	no	normal	NONE
O19-O23	...	...	...	...	...
O24	56	hypermetrope	yes	normal	NONE



**lenses=NONE** ← tear production=red

**lenses=NONE** ← tear production=normal AND astigmatism=yes AND spect. pre.=hypermetrope

**lenses=SOFT** ← tear production=normal AND astigmatism=no

**lenses=HARD** ← tear production=normal AND astigmatism=yes AND spect. pre.=myope

**lenses=NONE** ←

# Classification rules model learned from contact lens data

**lenses=NONE** ← tear production=reduced

**lenses=NONE** ← tear production=normal AND  
astigmatism=yes AND  
spect. pre.=hypermetrope

**lenses=SOFT** ← tear production=normal AND  
astigmatism=no

**lenses=HARD** ← tear production=normal AND  
astigmatism=yes AND  
spect. pre.=myope

**lenses=NONE** ←

# Learning from Unlabeled Data

Person	Age	Spect. presc.	Astigm.	Tear prod.	Lenses
O1	17	myope	no	reduced	NONE
O2	23	myope	no	normal	SOFT
O3	22	myope	yes	reduced	NONE
O4	27	myope	yes	normal	HARD
O5	19	hypermetrope	no	reduced	NONE
O6-O13	...	...	...	...	...
O14	35	hypermetrope	no	normal	SOFT
O15	43	hypermetrope	yes	reduced	NONE
O16	39	hypermetrope	yes	normal	NONE
O17	54	myope	no	reduced	NONE
O18	62	myope	no	normal	NONE
O19-O23	...	...	...	...	...
O24	56	hypermetrope	yes	normal	NONE

**Unlabeled data** - clustering: grouping of similar instances  
 - association rule learning

# Learning from Numeric Class Data

Person	Age	Spect. presc.	Astigm.	Tear prod.	LensPrice
O1	17	myope	no	reduced	0
O2	23	myope	no	normal	8
O3	22	myope	yes	reduced	0
O4	27	myope	yes	normal	5
O5	19	hypermetrope	no	reduced	0
O6-O13	...	...	...	...	...
O14	35	hypermetrope	no	normal	5
O15	43	hypermetrope	yes	reduced	0
O16	39	hypermetrope	yes	normal	0
O17	54	myope	no	reduced	0
O18	62	myope	no	normal	0
O19-O23	...	...	...	...	...
O24	56	hypermetrope	yes	normal	0

**Numeric class values** – regression analysis

# Task reformulation: Binary Class Values

Person	Age	Spect. presc.	Astigm.	Tear prod.	Lenses
O1	17	myope	no	reduced	NO
O2	23	myope	no	normal	YES
O3	22	myope	yes	reduced	NO
O4	27	myope	yes	normal	YES
O5	19	hypermetrope	no	reduced	NO
O6-O13	...	...	...	...	...
O14	35	hypermetrope	no	normal	YES
O15	43	hypermetrope	yes	reduced	NO
O16	39	hypermetrope	yes	normal	NO
O17	54	myope	no	reduced	NO
O18	62	myope	no	normal	NO
O19-O23	...	...	...	...	...
O24	56	hypermetrope	yes	normal	NO

**Binary classes** (positive vs. negative examples of **Target class**)

- for Concept learning – classification and class description
- for Subgroup discovery – exploring patterns characterizing groups of instances of target class

# Task reformulation: Binary Class and Feature Values

Person	Young	Myope	Astigm.	Reduced tea	Lenses
O1	1	1	0	1	NO
O2	1	1	0	0	YES
O3	1	1	1	1	NO
O4	1	1	1	0	YES
O5	1	0	0	1	NO
O6-O13	...	...	...	...	...
O14	0	0	0	0	YES
O15	0	0	1	1	NO
O16	0	0	1	0	NO
O17	0	1	0	1	NO
O18	0	1	0	0	NO
O19-O23	...	...	...	...	...
O24	0	0	1	0	NO

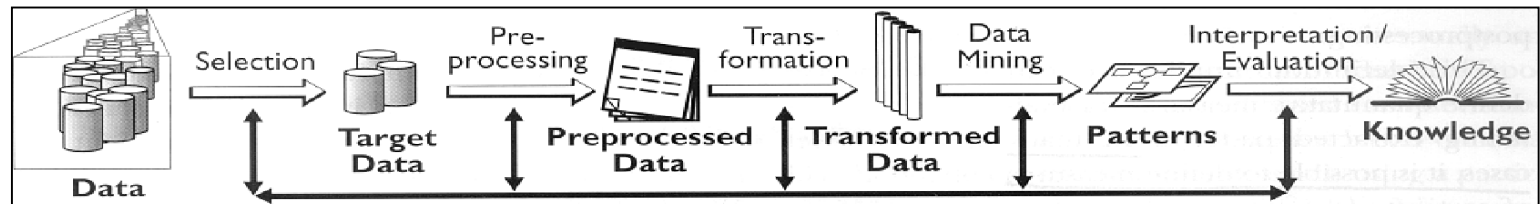
Binary features and class values

# First Generation Data Mining

- **First machine learning algorithms for**
  - Decision tree and rule learning in 1970s and early 1980s by Quinlan, Michalski et al., Breiman et al., ...
- **Characterized by**
  - Learning from data stored in a single data table
  - Relatively small set of instances and attributes
- **Lots of ML research followed in 1980s**
  - Numerous conferences ICML, ECML, ... and ML sessions at AI conferences IJCAI, ECAI, AAAI, ...
  - Extended set of learning tasks and algorithms addressed

# Second Generation Data Mining

- **Developed since 1990s:**
  - Focused on data mining tasks characterized by large datasets described by large numbers of attributes
  - Industrial standard: CRISP-DM methodology (1997)

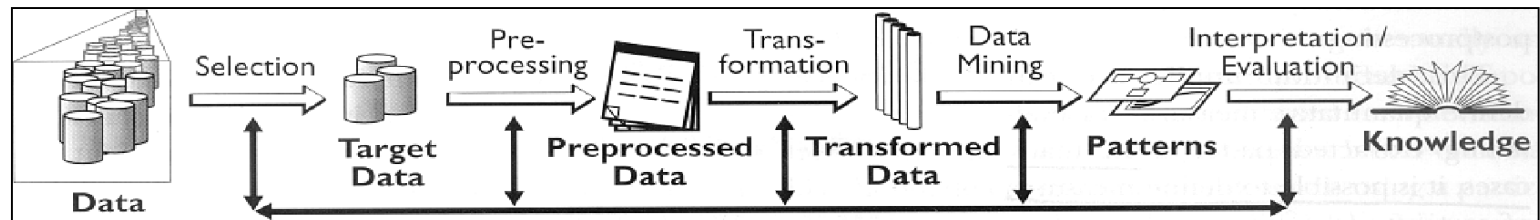




# Second Generation Data Mining

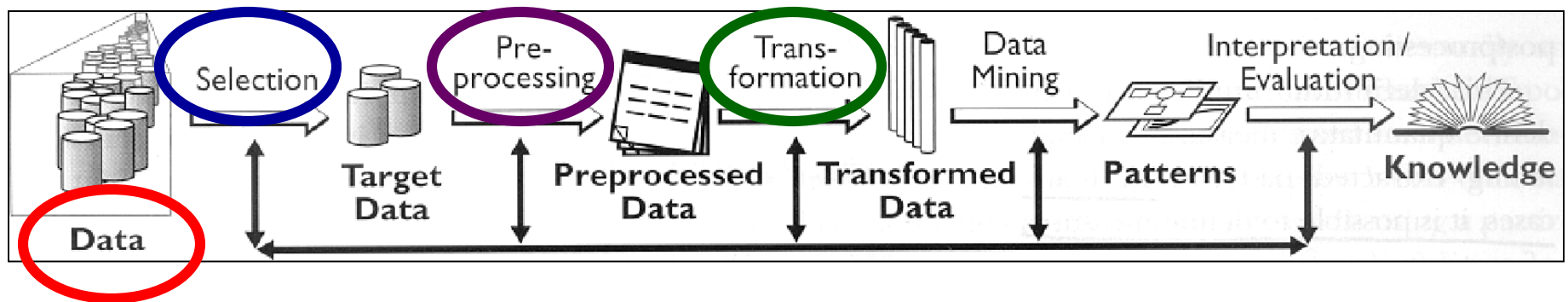
- **Developed since 1990s:**

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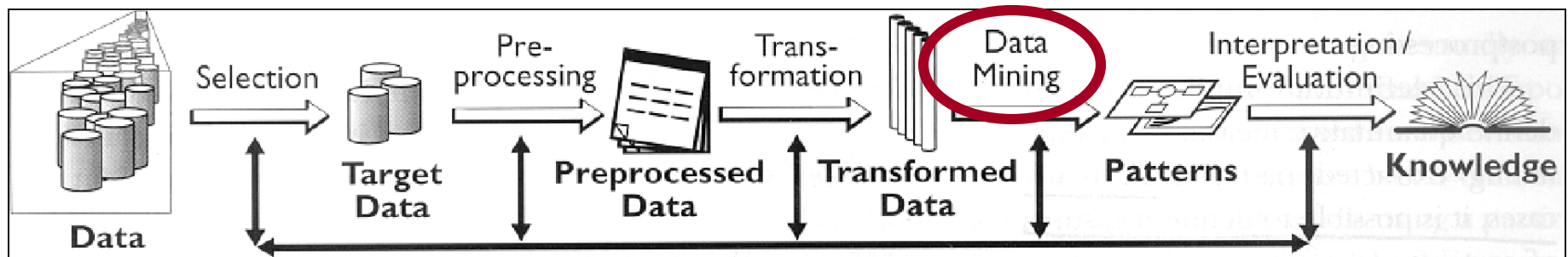
- New conferences on practical aspects of data mining and knowledge discovery: KDD, PKDD, ...
- New learning tasks and efficient learning algorithms:
  - Learning predictive models: Bayesian network learning,, **relational data mining**, statistical relational learning, SVMs, ...
  - Learning descriptive patterns: association rule learning, **subgroup discovery**, ...

# MEDIANA – analysis of media research data



- Questionnaires about journal/magazine reading, watching of TV programs and listening of radio programs, about 1200 questions. Yearly publication: frequency of reading/listening/watching, distribution w.r.t. Sex, Age, Education, Buying power,...
- Data about 8000 questionnaires, covering lifestyle, spare time activities, personal viewpoints, reading/listening/watching of media (yes/no/how much), interest for specific topics in media, social status
- good quality, “clean” data
- table of n-tuples (rows: individuals, columns: attributes, in classification tasks selected class)

# MEDIANA – media research pilot study



- **Patterns uncovering regularities concerning:**
  - Which other journals/magazines are read by readers of a particular journal/magazine ?
  - What are the properties of individuals that are consumers of a particular media offer ?
  - Which properties are distinctive for readers of different journals ?
- **Induced models: description (association rules, clusters) and classification (decision trees, classification rules)**

# Simplified association rules

## Finding profiles of readers of the Delo daily newspaper

1. reads\_Marketing\_magazine 116 →  
reads\_Delo 95 (0.82)
2. reads\_Finance 223 → reads\_Delo 180 (0.81)
3. reads\_Views 201 → reads\_Delo 157 (0.78)
4. reads\_Money 197 → reads\_Delo 150 (0.76)
5. reads\_Vip 181 → reads\_Delo 134 (0.74)

**Interpretation:** Most readers of Marketing magazine, Finance, Views, Money and Vip read also Delo.

# Simplified association rules

1. reads\_Sara 332 → reads\_Slovenian\_news 211 (0.64)
2. reads\_Love\_stories 283 →  
reads\_Slovenian\_news 174 (0.61)
3. reads\_Dolenjska\_news 520 →  
reads\_Slovenian\_news 310 (0.6)
4. reads\_Omama 154 → reads\_Slovenian\_news 90 (0.58)
5. reads\_Workers\_news 177 →  
reads\_Slovenian\_news 102 (0.58)

Most of the readers of Sara, Love stories, Dolenjska news, Omama in Workers news read also Slovenian news.

# Simplified association rules

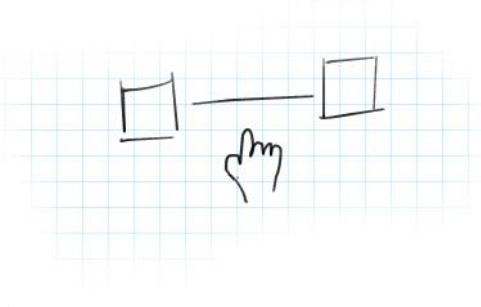
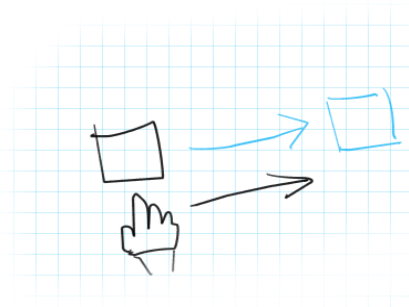
1. reads\_Sports\_news 303 →  
reads\_Slovenian\_shareholders\_magazine 164 (0.54)
2. reads\_Sports\_news 303 →  
reads\_Salomon\_advertisemens 155 (0.51)
3. reads\_Sports\_news 303 →  
reads\_Lady 152 (0.5)

More than half of readers of Sports news reads also Slovenian shareholders magazine, Solomon advertisements and Lady.



# Data Mining Workflows for Open Data Science

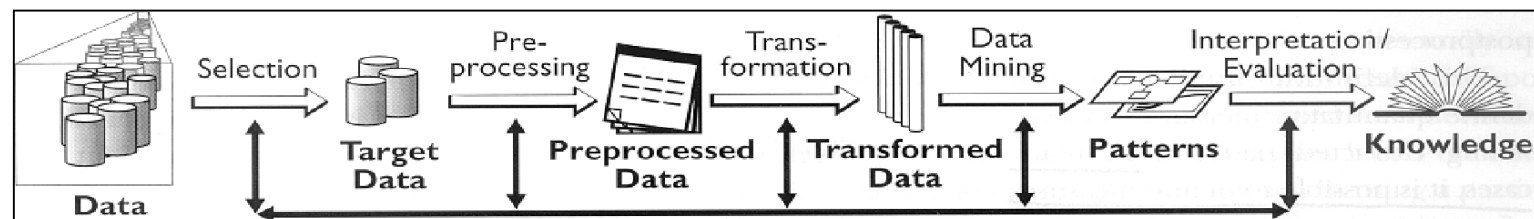
- Workflows are executable visual representations of procedures
  - divided into smaller chunks of code (components)
  - organized as sequences of connected components.
- Suitable for representing complex scientific pipelines
  - by explicitly modeling dependencies of components
- Building scientific workflows consists of simple operations on workflow elements (drag, drop, connect), suitable for non-experts





# Third Generation Data Mining

- **Developed since 2010s:**
  - Focused on big data analytics
  - Addressing complex data mining tasks and scenarios
  - New conferences on data science and big data analytics; e.g., IEEE Big Data, Complex networks, ...
  - New learning tasks and efficient learning algorithms:
    - Analysis of dynamic data streams, Network analysis, Text mining, Semantic data analysis, ...
  - Lots of emphasis on automated **data transformation**
    - **Propositionalization** of relational data, of heterogeneous information networks, ...
    - **Embedding** of texts, networks, knowledge graphs, entities (features), ... is highly popular in the last few years



# Propositionalization: Data transformation for Relational Data Mining

customer							
ID	Zip	Sex	Status	Income	Age	Club	Response
...	...	...	...	...	...	...	...
3478	34677	m	si	60-70	32	me	nr
3479	43666	f	ma	80-90	45	nm	re
...	...	...	...	...	...	...	...

order				
Customer ID	Order ID	Store ID	Delivery Mode	Payment Mode
...	...	...	...	...
3478	2140267	12	regular	cash
3478	3446778	12	express	check
3478	4728386	17	regular	check
3479	3233444	17	express	credit
3479	3475886	12	regular	credit
...	...	...	...	...

store			
Store ID	Size	Type	Location
...	...	...	...
12	small	franchise	city
17	large	indep	rural
...	...	...	...

Relational representation of customers, orders and stores.

Step 1

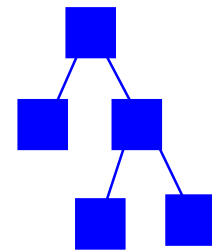
Propositionalization

	f1	f2	f3	f4	f5	f6	...	...	...	...	fn
g1	1	0	0	1	1	1	0	0	1	0	1
g2	0	1	1	0	1	1	0	0	0	1	1
g3	0	1	1	1	0	0	1	1	0	0	0
g4	1	1	1	0	1	1	0	0	1	1	1
g5	1	1	1	0	0	1	0	1	1	0	1
g1	0	0	1	1	0	0	0	1	0	0	0
g2	1	1	0	0	1	1	0	1	0	1	1
g3	0	0	0	0	1	0	0	1	1	1	0
g4	1	0	1	1	1	0	1	0	0	1	0

Step 2

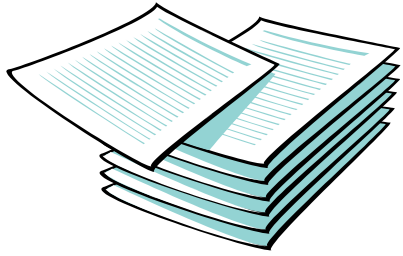
Data Mining

	f1	f2	f3	f4	f5	f6	...	...	...	...	fn
g1	1	0	0	1	1	1	0	0	1	0	1
g2	0	1	1	0	1	1	0	0	0	1	1
g3	0	1	1	1	0	0	1	1	0	0	0
g4	1	1	1	0	1	1	0	0	1	1	1
g5	1	1	1	0	0	1	0	1	1	0	1
g1	0	0	1	1	0	0	0	1	0	0	0
g2	1	1	0	0	1	1	0	1	0	1	1
g3	0	0	0	0	1	0	0	1	1	1	0
g4	1	0	1	1	1	0	1	0	0	1	0



model, patterns, ...

# Bag-of-Words Data Transformation for Text mining



Step 1

BoW vector construction

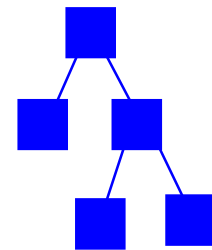
1. BoW features construction
2. Table of BoW vectors construction

Document	Word1	Word2	...	WordN	Class
d1	1	1	0	1	NO
d2	1	1	0	0	YES
d3	1	1	1	1	NO
d4	1	1	1	0	YES
d5	1	0	0	1	NO
d6-d13	...	...	...	...	...
d14	0	0	0	0	YES
d15	0	0	1	1	NO
d16	0	0	1	0	NO
d17	0	1	0	1	NO
d18	0	1	0	0	NO
d19-d23	...	...	...	...	...
d24	0	0	1	0	NO

Document	Word1	Word2	...	WordN	Class
d1	1	1	0	1	NO
d2	1	1	0	0	YES
d3	1	1	1	1	NO
d4	1	1	1	0	YES
d5	1	0	0	1	NO
d6-d13	...	...	...	...	...
d14	0	0	0	0	YES
d15	0	0	1	1	NO
d16	0	0	1	0	NO
d17	0	1	0	1	NO
d18	0	1	0	0	NO
d19-d23	...	...	...	...	...
d24	0	0	1	0	NO

Step 2

Data Mining



model, patterns, clusters,

...

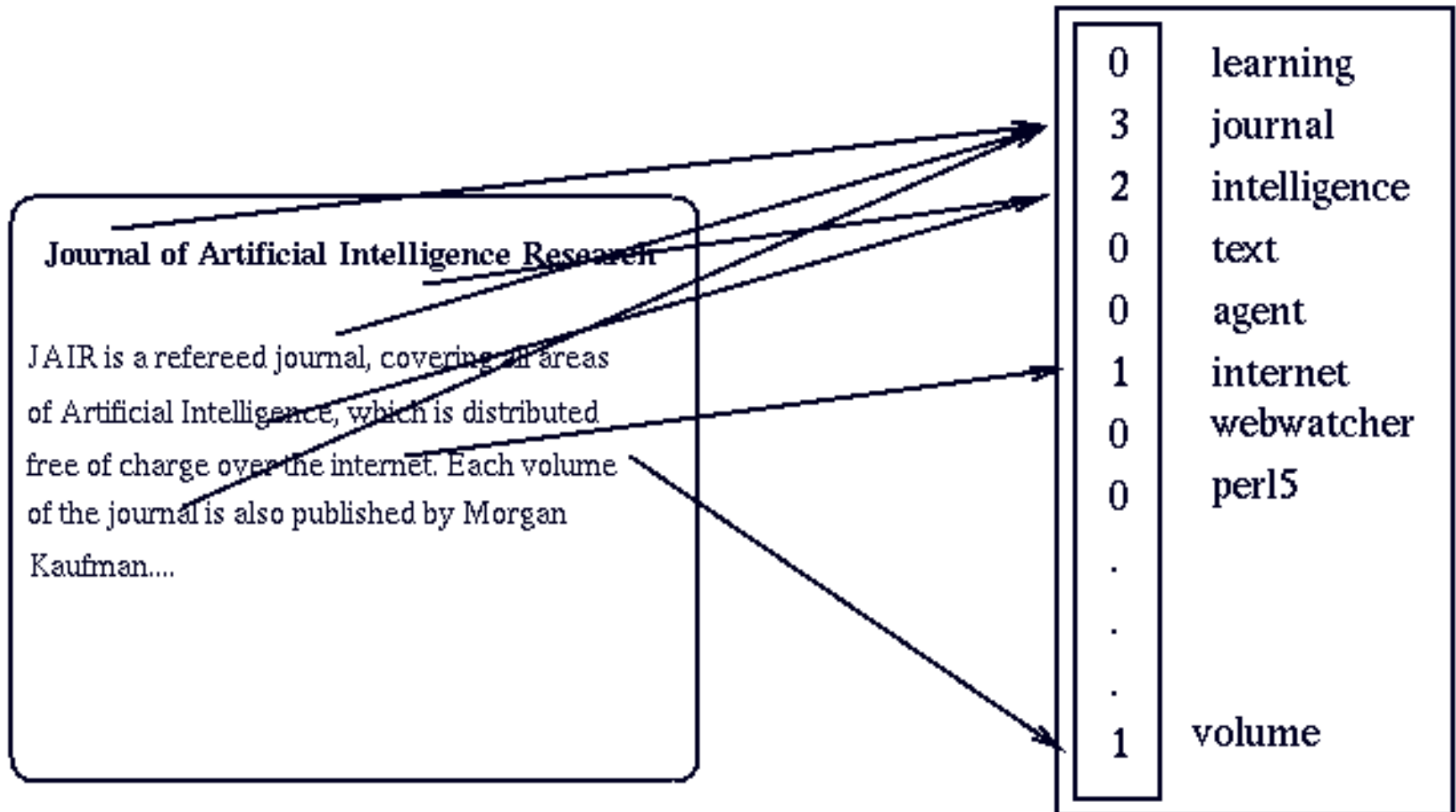
# Text mining: Words/terms as binary features

Document	Word1	Word2	...	WordN	Class
d1	1	1	0	1	NO
d2	1	1	0	0	YES
d3	1	1	1	1	NO
d4	1	1	1	0	YES
d5	1	0	0	1	NO
d6-d13	...	...	...	...	...
d14	0	0	0	0	YES
d15	0	0	1	1	NO
d16	0	0	1	0	NO
d17	0	1	0	1	NO
d18	0	1	0	0	NO
d19-d23	...	...	...	...	...
d24	0	0	1	0	NO

Instances = documents

Words and terms = Binary features

# Bag-of-Words document representation



# Word weighting for BoW document representation

- In bag-of-words representation each word is represented as a separate variable having numeric weight.
- The most popular weighting schema is normalized word frequency TFIDF:

$$tfidf(w) = tf \cdot \log\left(\frac{N}{df(w)}\right)$$

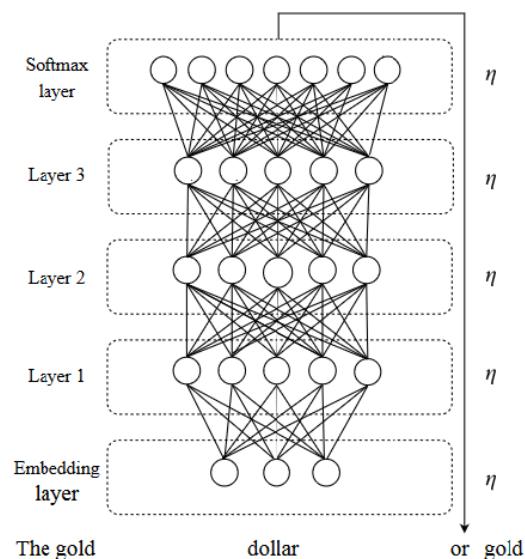
- $Tf(w)$  – term frequency (number of word occurrences in a document)
- $Df(w)$  – document frequency (number of documents containing the word)
- $N$  – number of all documents
- $Tfidf(w)$  – relative importance of the word in the document

The word is more important if it appears several times in a target document

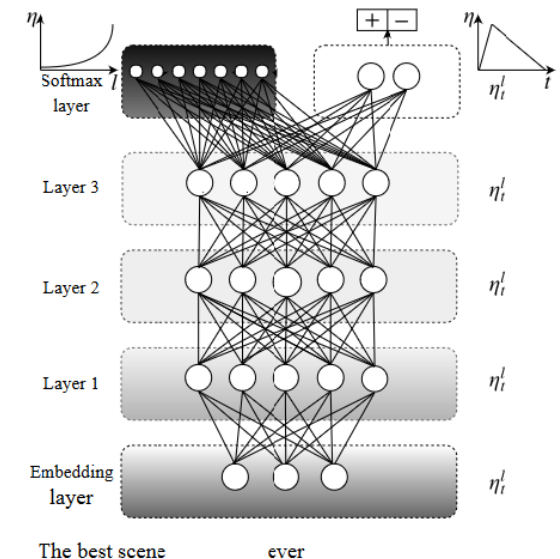
The word is more important if it appears in less documents

# Embeddings-based Data Transformations

- Embedding networks, knowledge graphs, relational data, entities (features), texts ...
  - Transforming data by projecting individual data instances into vectors (rows of a data table) – **dense data representation**
  - Weights correspond to weights in the embedding layer of a neural network



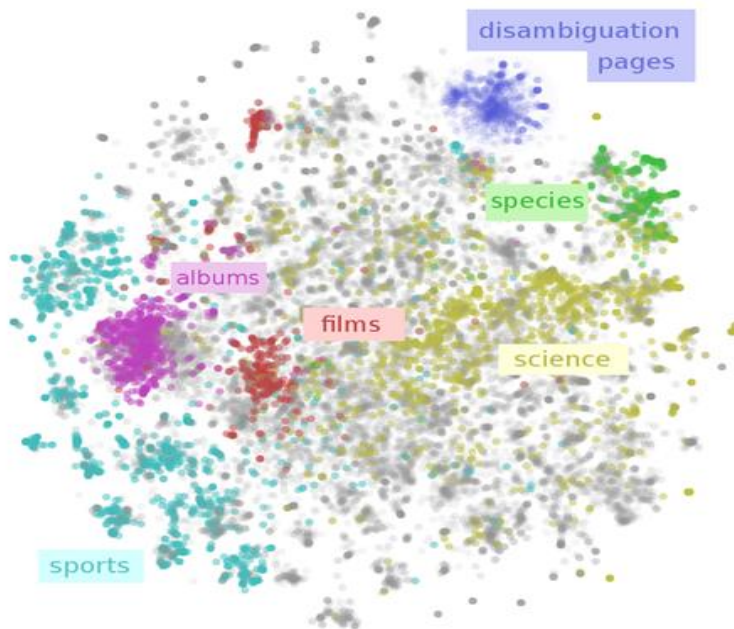
LM pre-training



Classifier fine-tuning

# Embedding-based Data Transformation for Text mining

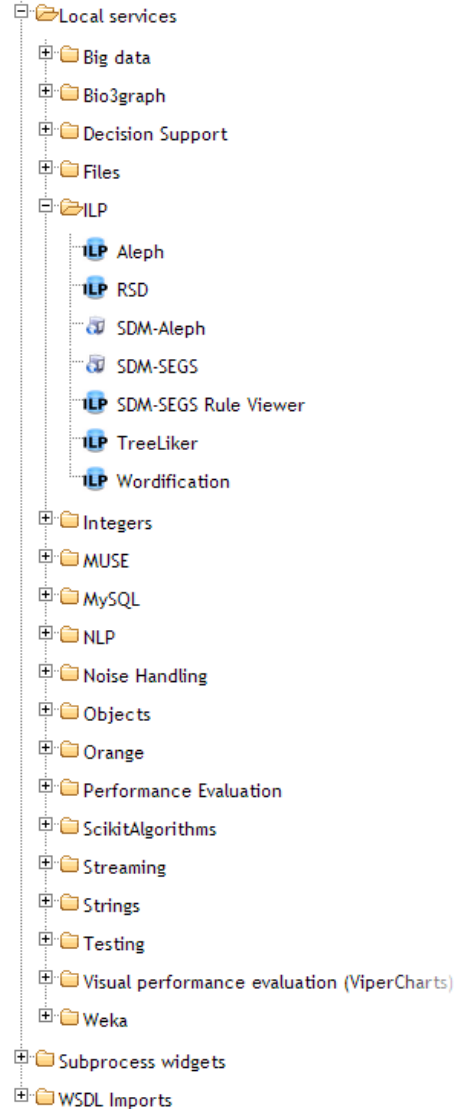
- Corpus embedding, Document embedding, Sentence embedding, **word embedding**, ...
  - Representations of word meaning obtained from corpus statistics
  - Spatial relationships correspond to linguistic relationships





# Third Generation Data Mining Platforms

- **Orange4WS** (Podpečan et al. 2009), **ClowdFlows** (Kranjc et al. 2012) and **TextFlows** (Perovšek et al. 2016)
  - are service oriented (DM algorithms as web services)
  - user-friendly HCI: canvas for workflow construction
  - include functionality of standard data mining platforms
    - WEKA algorithms, implemented as Web services
  - Include new functionality
    - relational data mining
    - semantic data mining
    - NLP processing and text mining
  - enable simplified construction of Web services from available algorithms
  - ClowdFlows and TextFlows run in a browser – enables data mining, workflow construction and sharing on the web

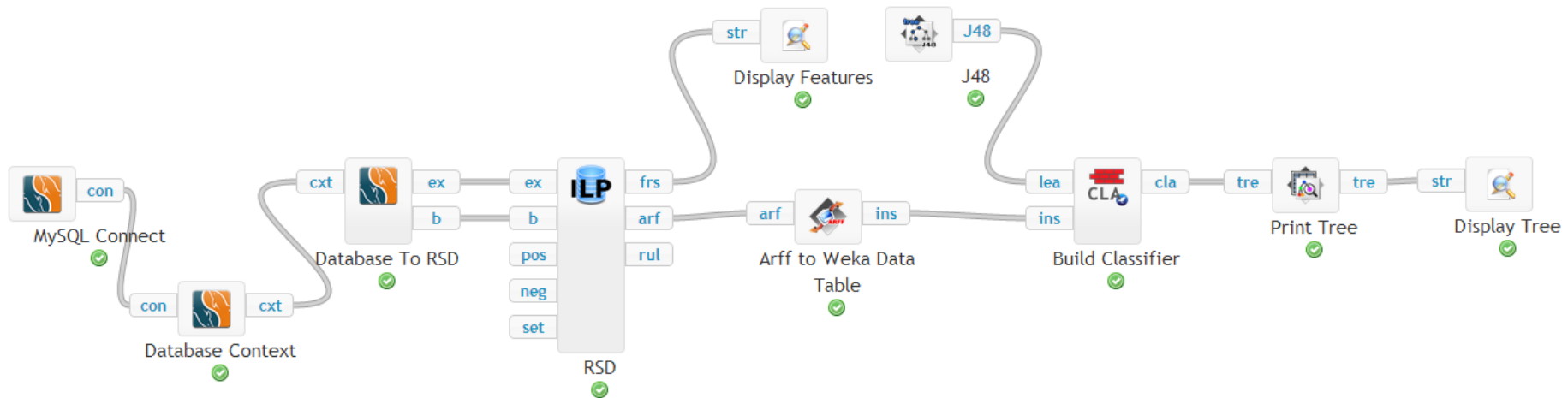


# CloudFlows platform

- **Large algorithm repository**
  - Relational data mining
  - All Orange algorithms
  - WEKA algorithms as web services
  - Data and results visualization
  - Text analysis
  - Social network analysis
  - Analysis of big data streams
- **Large workflow repository**
  - Enables access to our technology heritage

# CloudFlows platform

- Large repository of algorithms
- Large repository of workflows



## Example workflow:

Propositionalization with RSD  
available in CloudFlows at

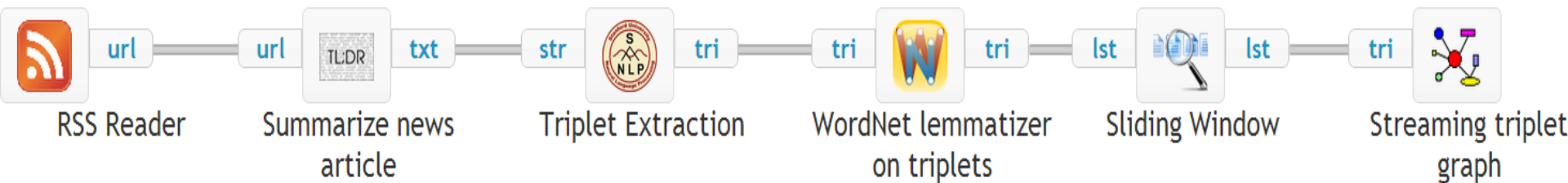
<http://clowdflows.org/workflow/611/>

# TextFlows

- Motivation:
  - Develop an online text mining platform for composition, execution and sharing of text mining workflows
- TextFlows platform – fork of ClowdFlows.org:
  - Specialized on text mining
  - Web-based user interface
  - Visual programming
  - Big roster of existing workflow (mostly text mining) components
  - Cloud-based service-oriented architecture

# “Big Data” Use Case

- Real-time analysis of big data streams
- Example: semantic graph construction from news streams. <http://cloudfloows.org/workflow/1729/>.



- Example: news monitoring by graph visualization (graph of CNN RSS feeds)

<http://cloudfloows.org/streams/data/31/1>



# Part I: Summary

- KDD is the overall process of discovering useful knowledge in data
  - many steps including data preparation, cleaning, transformation, pre-processing
- Data Mining is the data analysis phase in KDD
  - DM takes only 15%-25% of the effort of the overall KDD process
  - employing techniques from machine learning and statistics
- Predictive and descriptive induction have different goals: classifier vs. pattern discovery
- Many application areas, many powerful tools available

# Summary of types of learning tasks

- **Supervised learning vs. Unsupervised learning = Learning from Labeled vs. Learning from Unlabeled data**, i.e. depending whether the data includes class labels for a predefined target class attribute or not.
- **Prediction (classification, predictive modeling, classifier learning)** - learning classifiers from class labeled data, e.g., decision tree learning
- **Concept learning** – learning classifiers for a preselected target class from binary labeled data
- **Regression** – learning classifiers from data with numeric class labels
- **Multi-label prediction** - learning classifiers from data labeled by several target class attributes
- **Description (descriptive pattern mining)** - learning individual rules/patterns, describing properties of parts of the data set, e.g. association rule learning
- **Subgroup discovery** – combining supervised learning from class labeled data and descriptive pattern mining
- **Clustering** – grouping of unlabeled data, based on data similarity

# Technical paper outline

Book: Foundations of Rule Learning

Publisher: Springer, 2012

Authors: J. Fuernkranz, D. Gamberger and N. Lavrač

Chapter: Machine Learning and Data Mining

1.1 Introduction . . . . .	1
1.2 Historical background . . . . .	3
1.3 Knowledge discovery process and standardization ..	4
1.4 Terminology and categorization of learning tasks . . . .	6
1.5 Predictive data mining: Induction of models . . . . .	8
1.6 Descriptive data mining: Induction of patterns . . . . .	13
1.7 Relational data mining . . . . .	15
1.8 Conclusion . . . . .	17



# Course Outline

## I. Introduction

- Data Mining and KDD process
- Introduction to Data Mining
- Data Mining platforms

## II. Predictive DM

- Decision Tree learning
- Bayesian classifier
- Classification rule learning
- Classifier evaluation

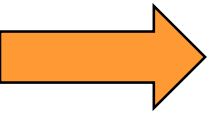
## III. Predictive DM

- Regression

## IV. Descriptive DM

- Predictive vs. descriptive induction
- Subgroup discovery
- Association rule learning
- Hierarchical clustering

## Part II. Predictive DM techniques



Decision tree learning

- Bayesian Classifier
- Rule learning
- Evaluation

# Predictive DM - Classification

- data are objects, characterized with attributes - they belong to different classes (discrete labels)
- given objects described with attribute values, induce a model to predict different classes
- decision trees, if-then rules, discriminant analysis, ...

# Predictive DM - classification

## formulated as a machine learning task

- Given a set of labeled **training examples** (n-tuples of attribute values, labeled by class name)

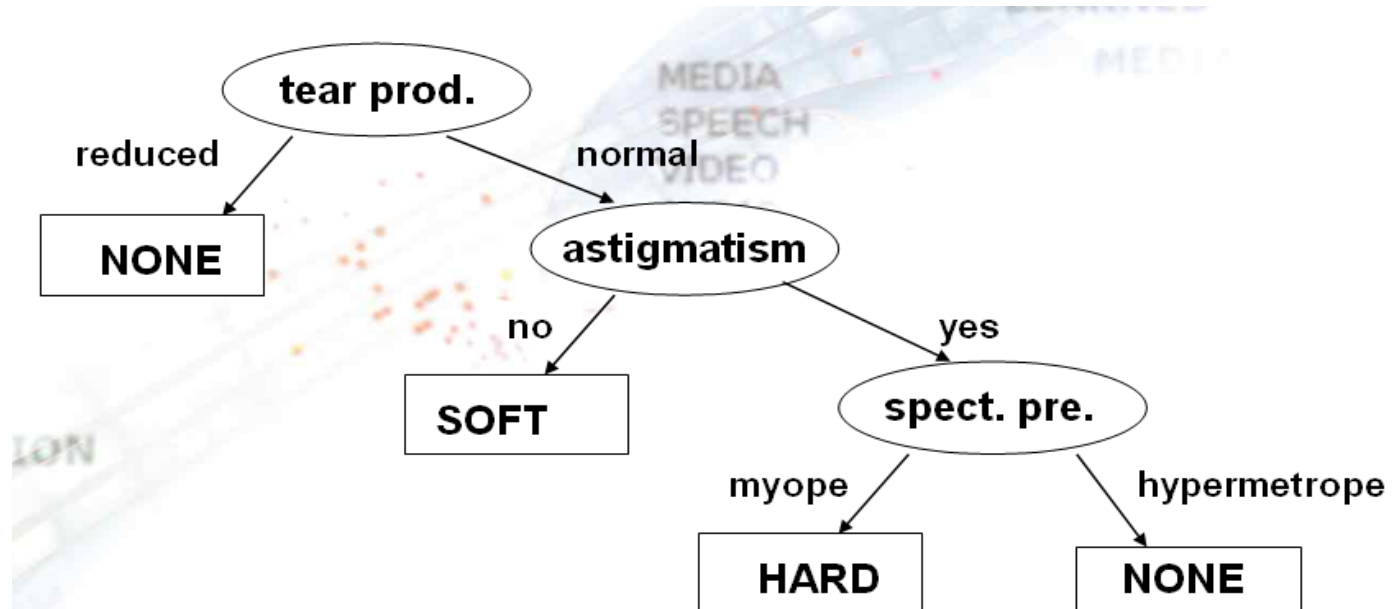
	A1	A2	A3	Class
example1	$v_{1,1}$	$v_{1,2}$	$v_{1,3}$	$C_1$
example2	$v_{2,1}$	$v_{2,2}$	$v_{2,3}$	$C_2$
..				

- Performing generalization from examples (induction)
- Find a **hypothesis** (a decision tree or classification rules) which explains the training examples, e.g. decision trees or classification rules of the form:

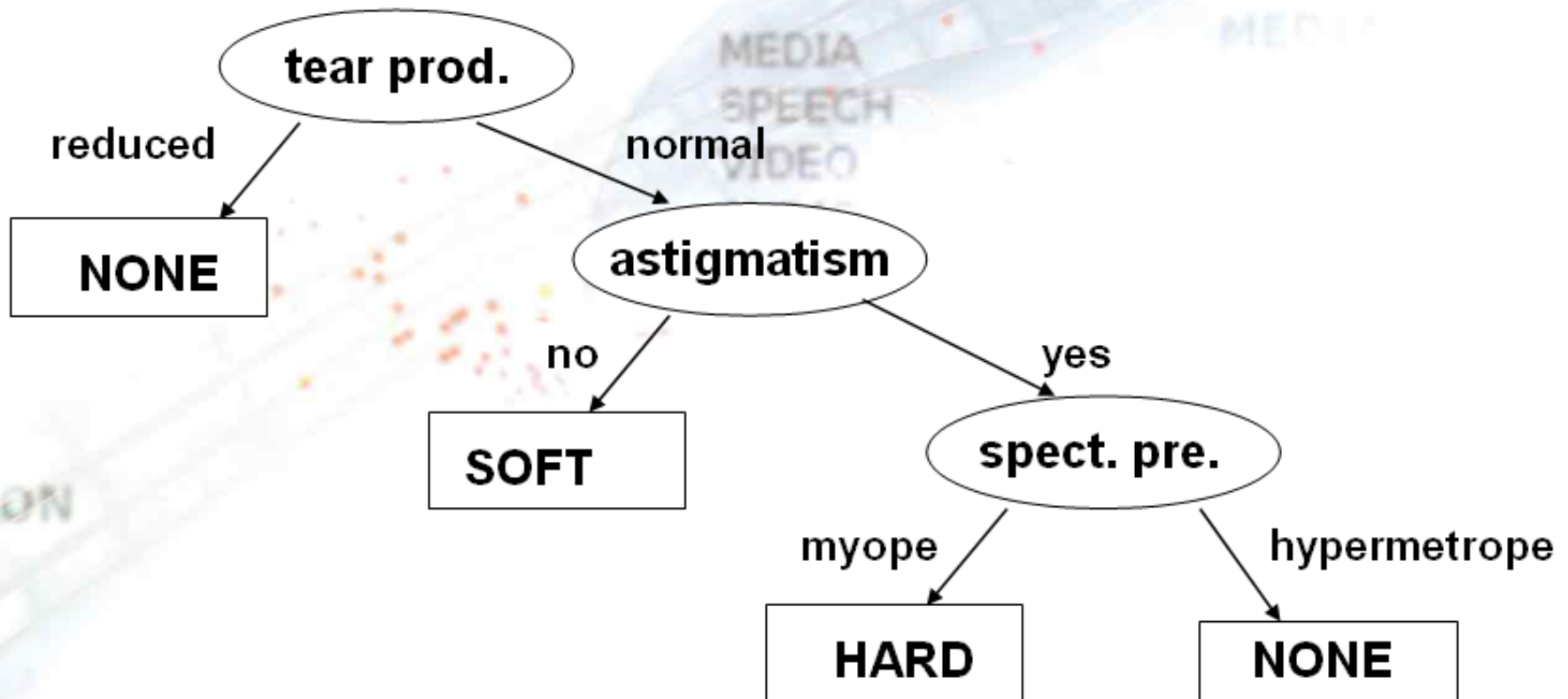
IF  $(A_i = v_{i,k})$  &  $(A_j = v_{j,l})$  & ... THEN Class =  $C_n$

# Decision Tree Learning

Person	Age	Spect. presc.	Astigm.	Tear prod.	Lenses
O1	young	myope	no	reduced	NONE
O2	young	myope	no	normal	SOFT
O3	young	myope	yes	reduced	NONE
O4	young	myope	yes	normal	HARD
O5	young	hypermetrope	no	reduced	NONE
O6-O13	...	...	...	...	...
O14	pre-presbyc	hypermetrope	no	normal	SOFT
O15	pre-presbyc	hypermetrope	yes	reduced	NONE
O16	pre-presbyc	hypermetrope	yes	normal	NONE
O17	presbyopic	myope	no	reduced	NONE
O18	presbyopic	myope	no	normal	NONE
O19-O23	...	...	...	...	...
O24	presbyopic	hypermetrope	yes	normal	NONE

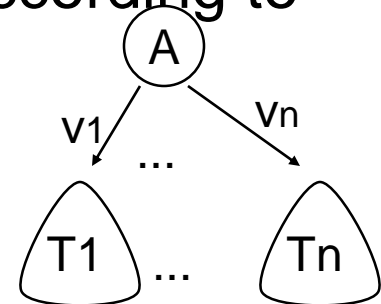


# Decision Tree classifier



# Decision tree learning algorithm

- ID3 (Quinlan 1979), CART (Breiman et al. 1984), C4.5, J48 in WEKA, ...
  - create the root node of the tree
  - if all examples from  $S$  belong to the same class  $C_j$ 
    - then label the root with  $C_j$
  - else
    - select the ‘most informative’ attribute  $A$  with values  $v_1, v_2, \dots, v_n$
    - divide training set  $S$  into  $S_1, \dots, S_n$  according to values  $v_1, \dots, v_n$
    - recursively build sub-trees  $T_1, \dots, T_n$  for  $S_1, \dots, S_n$



# Decision tree search heuristics

- Central choice in decision tree algorithms: Which attribute to test at each node in the tree ? The attribute that is most useful for classifying examples.
- Define a statistical property, called **information gain**, measuring how well a given attribute separates the training examples w.r.t their target classification.
- First define a measure commonly used in information theory, called **entropy**, to characterize the (im)purity of an arbitrary collection of examples.



# Entropy

- **S** - training set, **C<sub>1</sub>, ..., C<sub>N</sub>** - classes
- **Entropy E(S)** – measure of the impurity of training set S

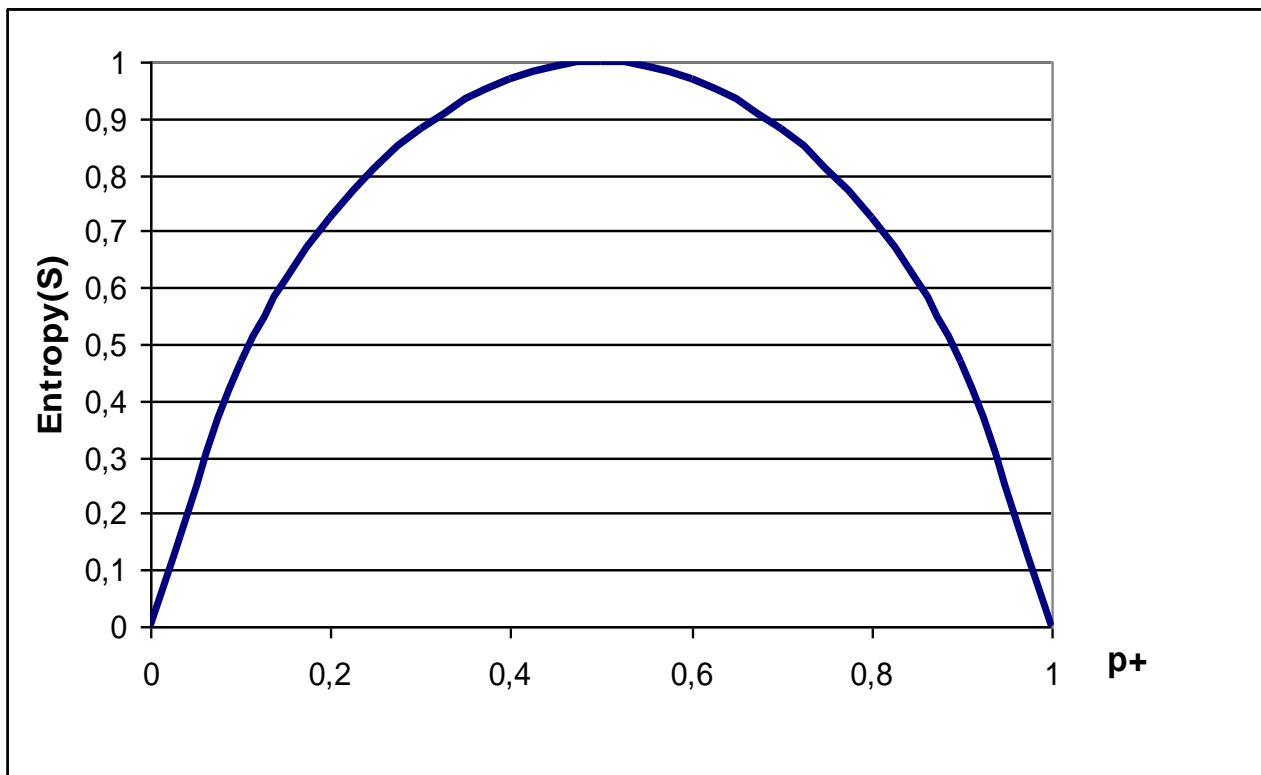
$$E(S) = - \sum_{c=1}^N p_c \cdot \log_2 p_c \quad \mathbf{p}_c \text{ - prior probability of class } \mathbf{C}_c \text{ (relative frequency of } \mathbf{C}_c \text{ in } \mathbf{S})$$

- Entropy in binary classification problems

$$\mathbf{E(S)} = - \mathbf{p}_+ \log_2 \mathbf{p}_+ - \mathbf{p}_- \log_2 \mathbf{p}_-$$

# Entropy

- $E(S) = - p_+ \log_2 p_+ - p_- \log_2 p_-$ .
- The entropy function relative to a Boolean classification, as the proportion  $p_+$  of positive examples varies between 0 and 1



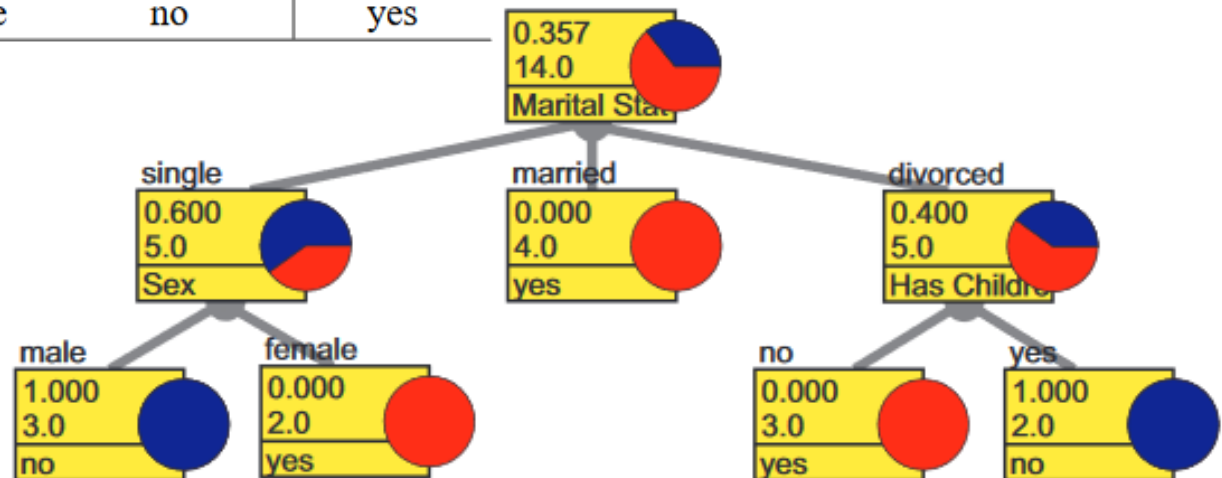
# Entropy – why ?

- **Entropy  $E(S)$**  = expected amount of information (in bits) needed to assign a class to a randomly drawn object in  $S$  (under the optimal, shortest-length code)
- Why ?
- Information theory: optimal length code assigns  $-\log_2 p$  bits to a message having probability  $p$
- So, in binary classification problems, the expected number of bits to encode + or – of a random member of  $S$  is:

$$p_+ (-\log_2 p_+) + p_- (-\log_2 p_-) = -p_+ \log_2 p_+ - p_- \log_2 p_-$$

# Binary classification problem: Survey data

Education	Marital Status	Sex	Has Children	Approved
primary	single	male	no	no
primary	single	male	yes	no
primary	married	male	no	yes
university	divorced	female	no	yes
university	married	female	yes	yes
secondary	single	male	no	no
university	single	female	no	yes
secondary	divorced	female	no	yes
secondary	single	female	yes	yes
secondary	married	male	yes	yes
primary	married	female	no	yes
secondary	divorced	male	yes	no
university	divorced	female	yes	no
secondary	divorced	male	no	yes



# Entropy – example calculation

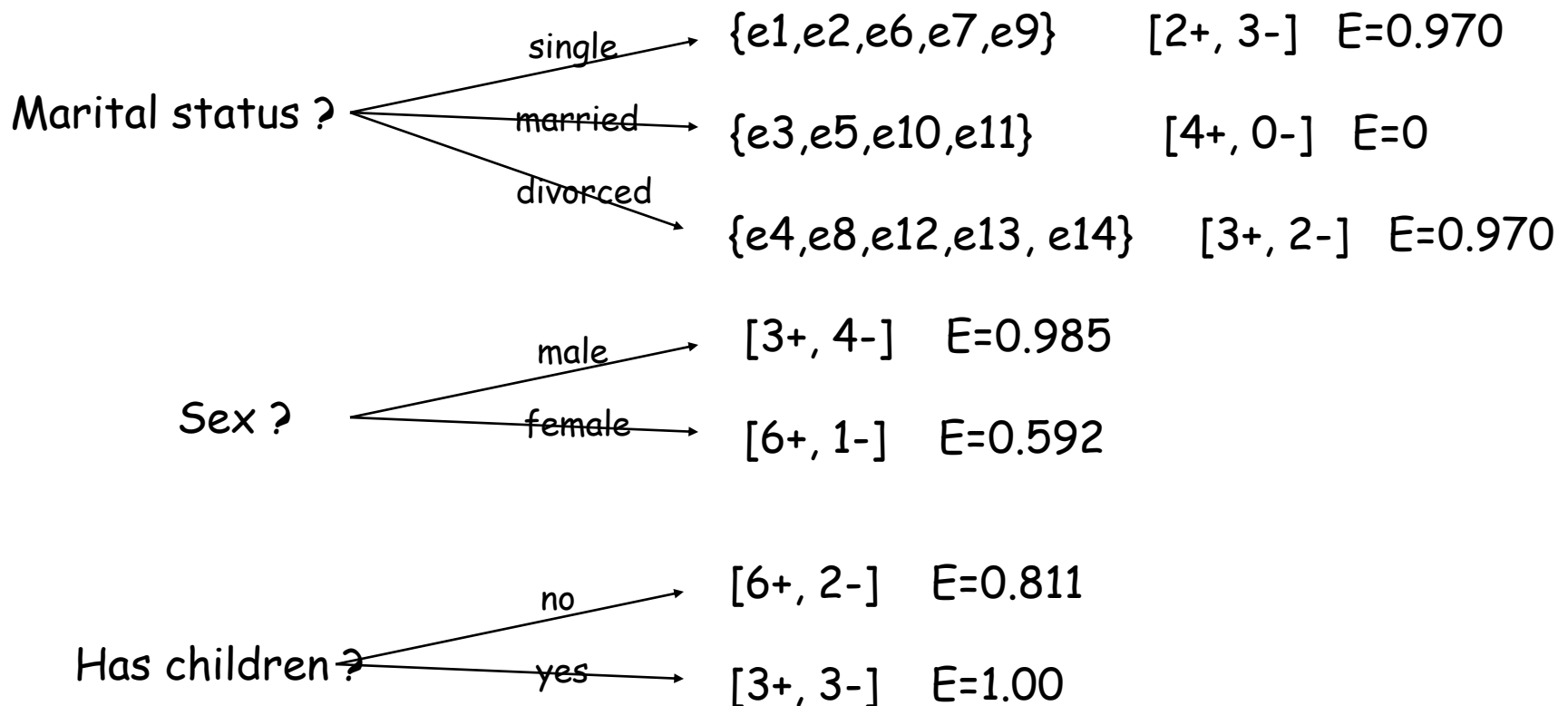
- Training set  $S$ : 14 examples (9 pos., 5 neg.)
- Notation:  $S = [9+, 5-]$
- $E(S) = -p_+ \log_2 p_+ - p_- \log_2 p_-$
- Computing entropy, if probability is estimated by relative frequency

$$E(S) = -\left(\frac{|S_+|}{|S|} \cdot \log \frac{|S_+|}{|S|}\right) - \left(\frac{|S_-|}{|S|} \cdot \log \frac{|S_-|}{|S|}\right)$$

- $E([9+,5-]) = - (9/14) \log_2(9/14) - (5/14) \log_2(5/14)$   
 $= 0.940$

# Survey data: Entropy

- $E(S) = - p_+ \log_2 p_+ - p_- \log_2 p_-$ .
- $E(9+,5-) = -(9/14) \log_2(9/14) - (5/14) \log_2(5/14) = 0.940$



# Information gain search heuristic

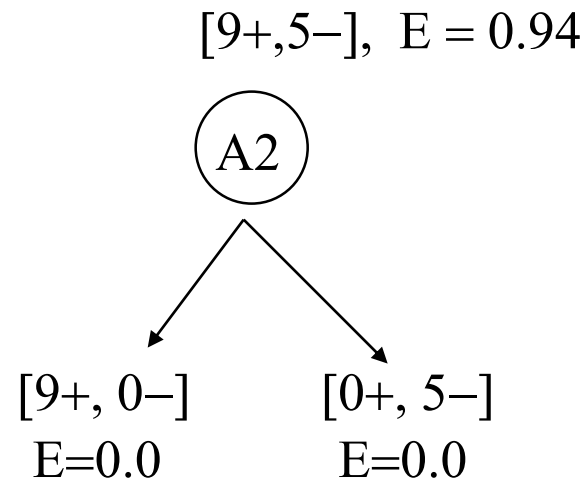
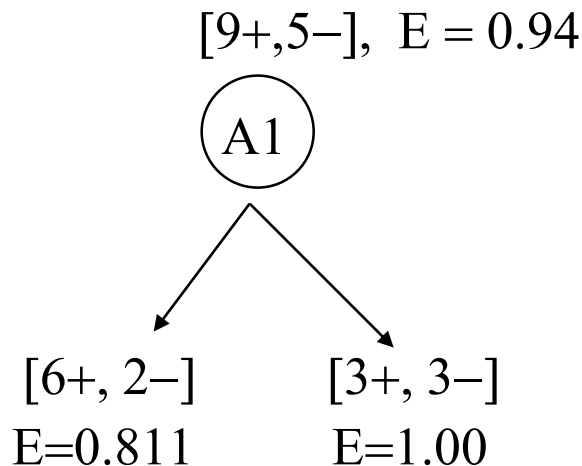
- **Information gain** measure is aimed to minimize the number of tests needed for the classification of a new object
- **Gain(S,A)** – expected reduction in entropy of S due to sorting on A

$$Gain(S, A) = E(S) - \sum_{v \in Values(A)} \frac{|S_v|}{|S|} \cdot E(S_v)$$

- **Most informative** attribute: **max Gain(S,A)**

# Information gain search heuristic

- Which attribute is more informative, A1 or A2 ?



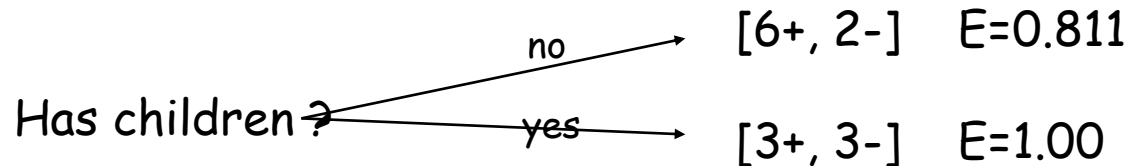
- $\text{Gain}(S, A1) = 0.94 - (8/14 \times 0.811 + 6/14 \times 1.00) = 0.048$
- $\text{Gain}(S, A2) = 0.94 - 0 = 0.94$                       A2 has max Gain



# Survey data: Information gain

$$Gain(S, A) = E(S) - \sum_{v \in Values(A)} \frac{|S_v|}{|S|} \cdot E(S_v)$$

- Values(Has children) = {no, yes}



–  $S = [9+, 5-], E(S) = 0.940$

–  $S_{no} = [6+, 2-], E(S_{no}) = 0.811$

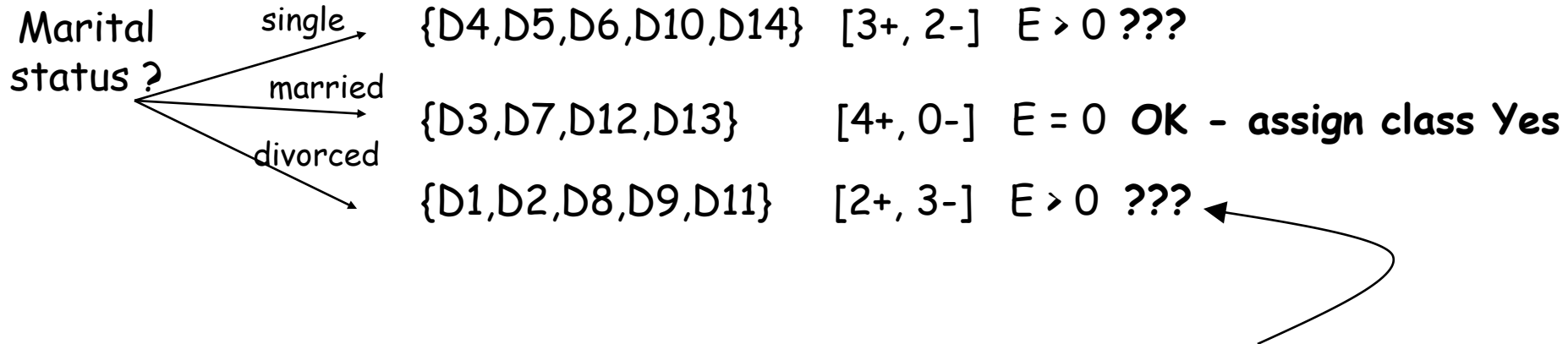
–  $S_{yes} = [3+, 3-], E(S_{yes}) = 1.0$

– **Gain(S, Has children) =  $E(S) - (8/14)E(S_{no}) - (6/14)E(S_{yes}) = 0.940 - (8/14) \times 0.811 - (6/14) \times 1.0 = \mathbf{0.048}$**

# Survey data: Information gain

- **Which attribute is the best?**
  - Gain(S, Marital status)=0.246      *MAX !*
  - Gain(S, Sex)=0.151
  - Gain(S, Has children)=0.048
  - Gain(S, Education)=0.029

# Survey data: Information gain



- Which attribute should be tested here?
  - $\text{Gain}(S_{\text{sunny}}, \text{Sex}) = 0.97 - (3/5)0 - (2/5)0 = 0.970$  **MAX !**
  - $\text{Gain}(S_{\text{sunny}}, \text{Has children}) = 0.97 - (2/5)0 - (2/5)1 - (1/5)0 = 0.570$
  - $\text{Gain}(S_{\text{sunny}}, \text{Education}) = 0.97 - (2/5)1 - (3/5)0.918 = 0.019$

# Probability estimates

- **Relative frequency :**
  - problems with small samples

$$p(\text{Class} \mid \text{Cond}) = \frac{n(\text{Class}.\text{Cond})}{n(\text{Cond})}$$

$$[6+,1-] (7) = 6/7$$

$$[2+,0-] (2) = 2/2 = 1$$

- **Laplace estimate :**
  - assumes uniform prior distribution of k classes

$$= \frac{n(\text{Class}.\text{Cond}) + 1}{n(\text{Cond}) + k} \quad k = 2$$

$$[6+,1-] (7) = 6+1 / 7+2 = 7/9$$

$$[2+,0-] (2) = 2+1 / 2+2 = 3/4$$

# Heuristic search in ID3

- **Search bias:** Search the space of decision trees from simplest to increasingly complex (greedy search, no backtracking, prefer small trees)
- **Search heuristics:** At a node, select the attribute that is most useful for classifying examples, split the node accordingly
- **Stopping criteria:** A node becomes a leaf
  - if all examples belong to same class  $C_j$ , label the leaf with  $C_j$
  - if all attributes were used, label the leaf with the most common value  $C_k$  of examples in the node
- **Extension to ID3:** handling noise - tree pruning



# Handling noise – Tree pruning

## Sources of imperfection

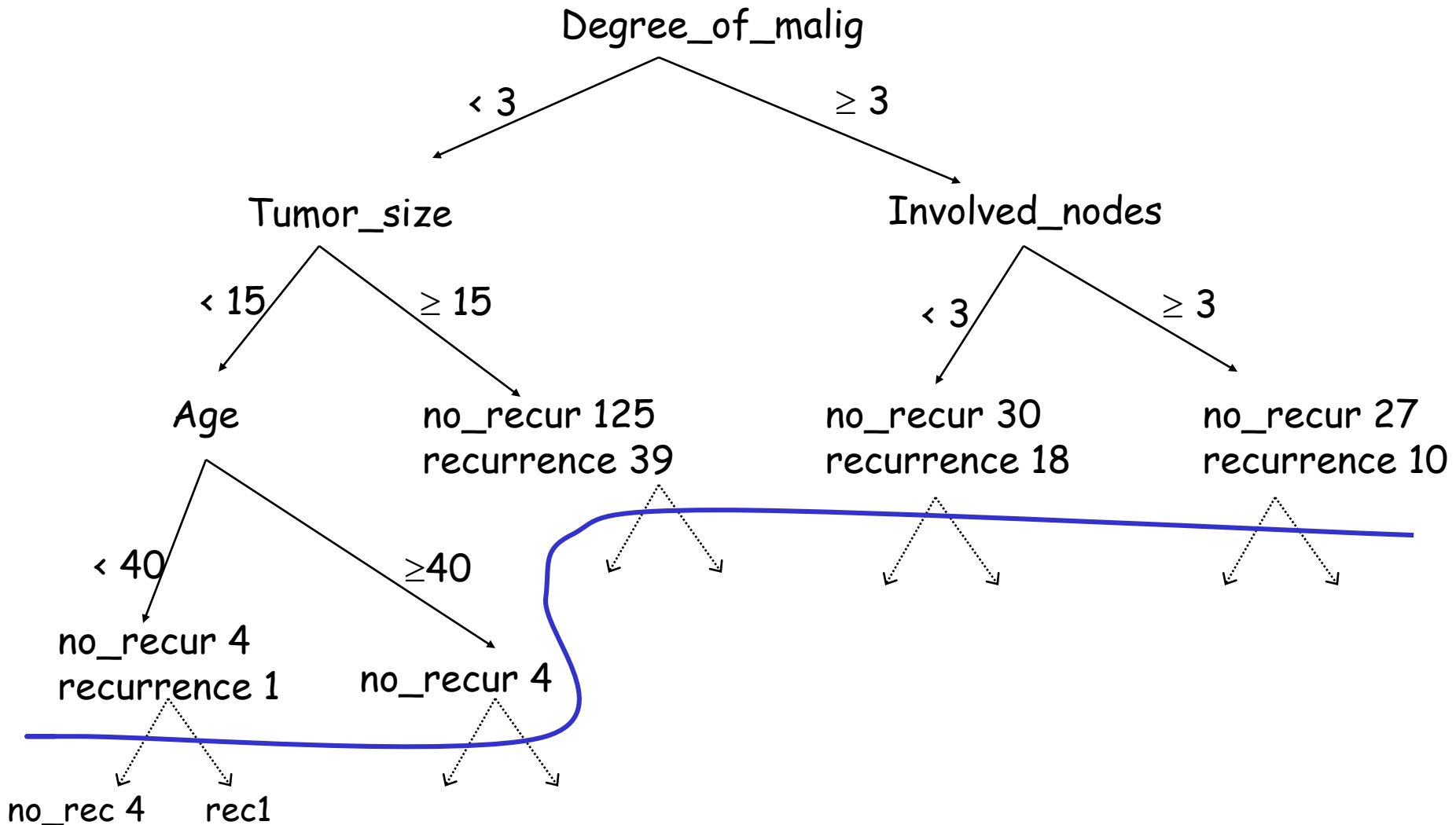
1. Random errors (noise) in training examples
  - erroneous attribute values
  - erroneous classification
2. Too sparse training examples (incompleteness)
3. Inappropriate/insufficient set of attributes (inexactness)
4. Missing attribute values in training examples

# Handling noise – Tree pruning

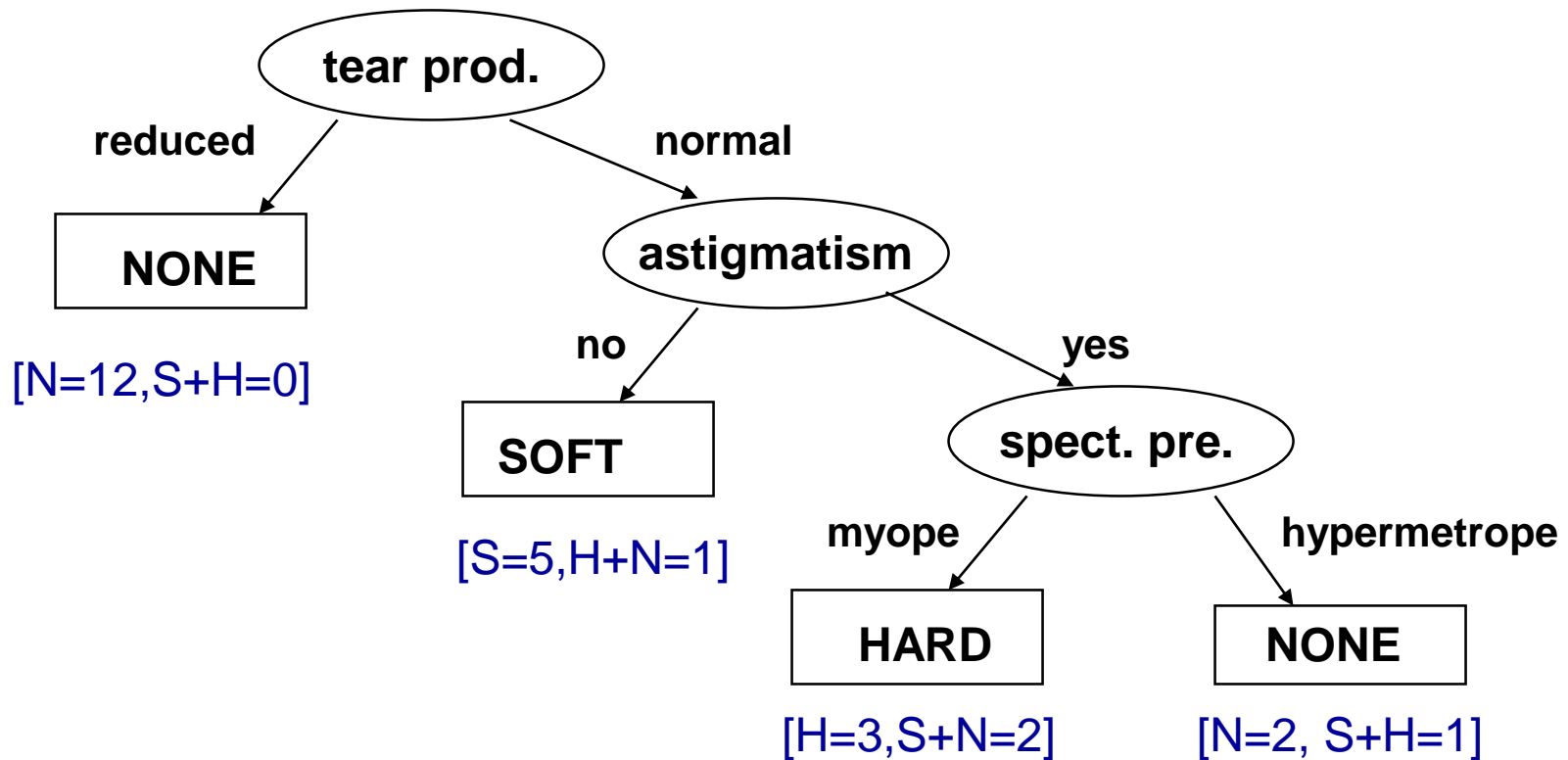
- Handling imperfect data
  - handling imperfections of type 1-3
    - pre-pruning (stopping criteria)
    - post-pruning / rule truncation
  - handling missing values
- Pruning avoids perfectly fitting noisy data: relaxing the completeness (fitting all +) and consistency (fitting all -) criteria in ID3



# Prediction of breast cancer recurrence: Tree pruning



# Pruned decision tree for contact lenses recommendation

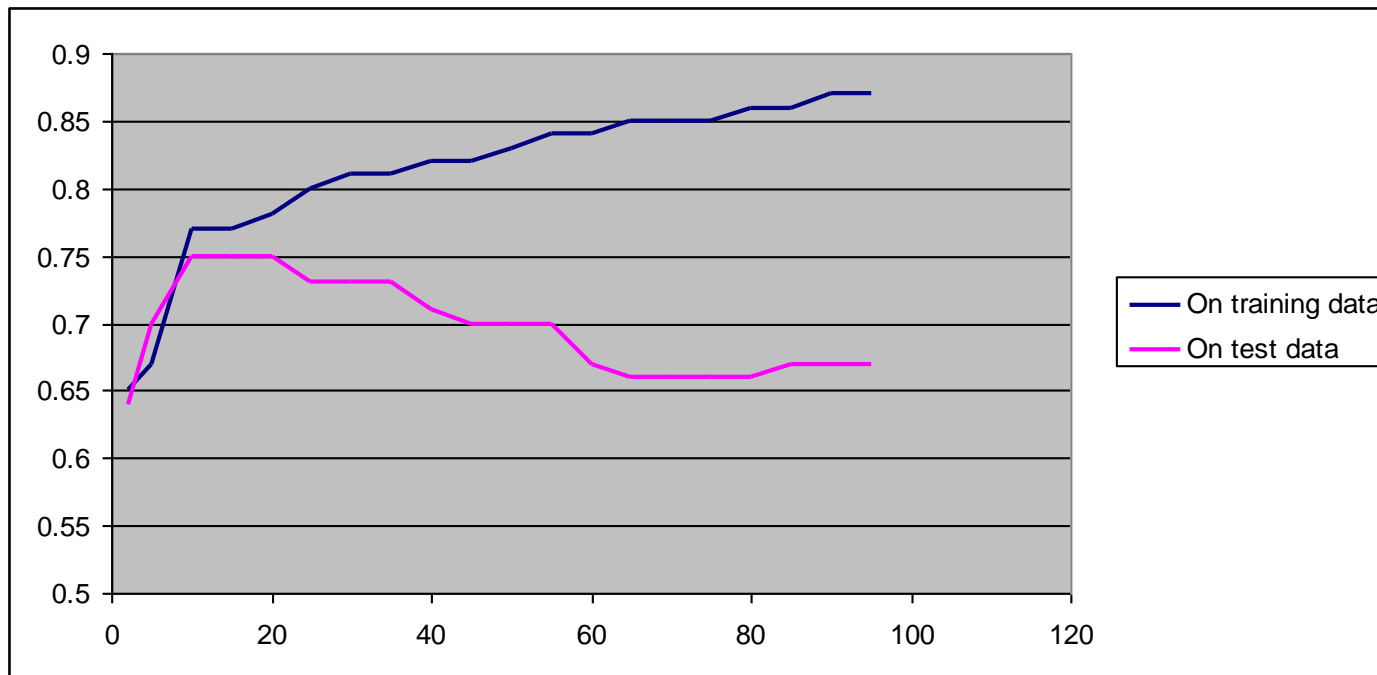


# Accuracy and error

- Accuracy: percentage of correct classifications
  - on the training set
  - on unseen instances
- How accurate is a decision tree when classifying unseen instances
  - An estimate of accuracy on unseen instances can be computed, e.g., by averaging over 4 runs:
    - split the example set into training set (e.g. 70%) and test set (e.g. 30%)
    - induce a decision tree from training set, compute its accuracy on test set
- Error =  $1 - \text{Accuracy}$
- High error may indicate data overfitting

# Overfitting and accuracy

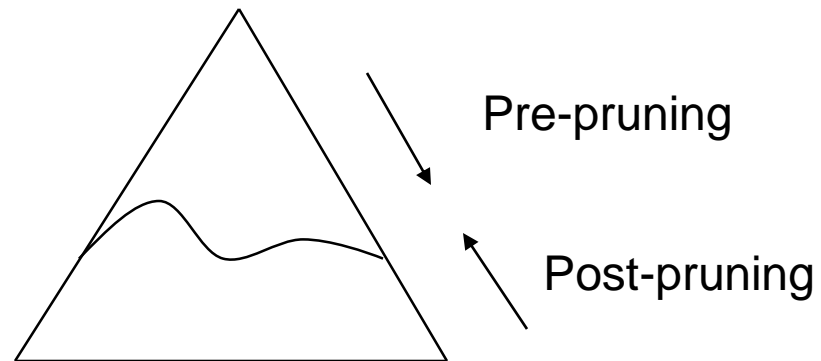
- Typical relation between tree size and accuracy



- Question: how to prune optimally?

# Avoiding overfitting

- How can we avoid overfitting?
  - Pre-pruning (forward pruning): stop growing the tree e.g., when data split not statistically significant or too few examples are in a split
  - Post-pruning: grow full tree, then post-prune



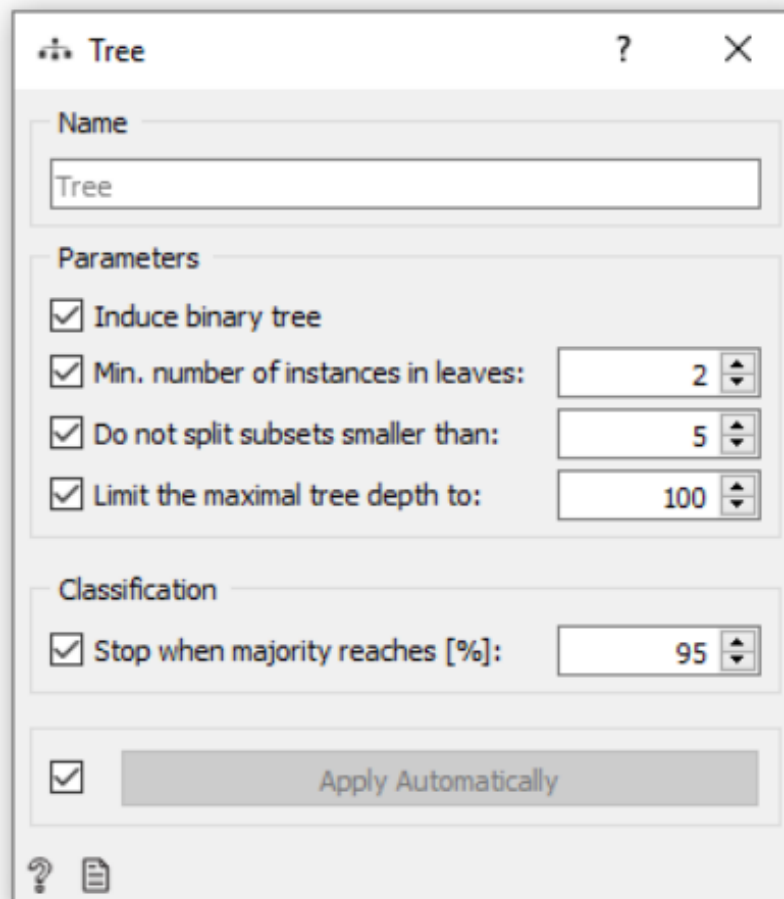
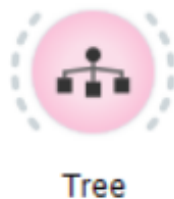
- forward pruning considered inferior (myopic)
- post pruning makes use of sub trees

# Selected decision/regression tree learners

- Decision tree learners
  - ID3 (Quinlan 1979)
  - CART (Breiman et al. 1984)
  - Assistant (Cestnik et al. 1987)
  - C4.5 (Quinlan 1993), C5 (See5, Quinlan)
  - J48 (available in WEKA), Tree (in Orange)
- Regression tree learners, model tree learners
  - M5, M5P (implemented in WEKA), Tree (in Orange)

# Selected decision tree learners

- Decision tree learners: Tree (in Orange)



The screenshot shows the configuration window for the 'Tree' widget in Orange3. The window has a title bar with a question mark and a close button. The main area is divided into several sections:

- Name:** A text input field containing the word 'Tree'.
- Parameters:** A section containing four checked checkboxes and three spinners:
  - Induce binary tree
  - Min. number of instances in leaves: 2
  - Do not split subsets smaller than: 5
  - Limit the maximal tree depth to: 100
- Classification:** A section containing one checked checkbox and one spinner:
  - Stop when majority reaches [%]: 95
- Apply Automatically:** A section containing one checked checkbox and a greyed-out button labeled 'Apply Automatically'.

At the bottom left of the window, there are icons for help (a question mark) and a document.

# Selected decision tree learners

- Homework
  - To prepare for the lecture of Petra Kralj Novak on Nov. 11, 2020 on using Tree software in Orange
  - See Blaž Zupan: Data Science with the OrangeToolbox  
[http://videlectures.net/AIndustrySeminar2019\\_zupan\\_data\\_science/](http://videlectures.net/AIndustrySeminar2019_zupan_data_science/)



# Features of C4.5 and J48

- Implemented as part of the WEKA data mining workbench
- Handling noisy data: post-pruning
- Handling incompletely specified training instances: 'unknown' values (?)
  - in learning assign conditional probability of value  $v$ :  
$$p(v|C) = p(vC) / p(C)$$
  - in classification: follow all branches, weighted by prior prob. of missing attribute values

# Other features of C4.5

- Binarization of attribute values
  - for continuous values select a boundary value maximally increasing the informativity of the attribute: sort the values and try every possible split (done automatically)
  - for discrete values try grouping the values until two groups remain \*
- ‘Majority’ classification in NULL leaf (with no corresponding training example)
  - if an example ‘falls’ into a NULL leaf during classification, the class assigned to this example is the majority class of the parent of the NULL leaf

\* the basic C4.5 doesn't support binarisation of discrete attributes, it supports grouping

# Appropriate problems for decision tree learning

- Classification problems: classify an instance into one of a discrete set of possible categories (medical diagnosis, classifying loan applicants, ...)
- Characteristics:
  - instances described by attribute-value pairs  
(discrete or real-valued attributes)
  - target function has discrete output values  
(boolean or multi-valued, if real-valued then regression trees)
  - disjunctive hypothesis may be required
  - training data may be noisy  
(classification errors and/or errors in attribute values)
  - training data may contain missing attribute values

# Classifier evaluation

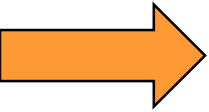
- **Use of induced models**
  - discovery of new patterns, new knowledge
  - classification of new objects
- **Evaluating the quality of induced models**
  - Accuracy, Error =  $1 - \text{Accuracy}$
  - classification accuracy on testing examples = percentage of correctly classified instances
    - split the example set into training set (e.g. 70%) to induce a concept, and test set (e.g. 30%) to test its accuracy
    - more elaborate strategies: 10-fold cross validation, leave-one-out, ...
  - comprehensibility (compactness)
  - information contents (information score), significance

# n-fold cross validation

- A method for accuracy estimation of classifiers
- Partition set  $D$  into  $n$  disjoint, almost equally-sized folds  $T_i$  where  $\bigcup_i T_i = D$
- **for**  $i = 1, \dots, n$  **do**
  - form a training set out of  $n-1$  folds:  $D_i = D \setminus T_i$
  - induce classifier  $H_i$  from examples in  $D_i$
  - use fold  $T_i$  for testing the accuracy of  $H_i$
- Estimate the accuracy of the classifier by averaging accuracies over  $n$  folds  $T_i$

## Part II. Predictive DM techniques

- Decision tree learning
- Bayesian Classifier
- Rule learning
- Evaluation



# Bayesian methods

- Bayesian methods – simple but powerful classification methods
  - Based on Bayesian formula

$$p(H | D) = \frac{p(D | H)}{p(D)} p(H)$$

- Main methods:
  - Naive Bayesian classifier
  - Semi-naïve Bayesian classifier
  - Bayesian networks \*

\* Out of scope of this course

# Naïve Bayesian classifier

- Probability of class, for given attribute values

$$p(c_j | v_1 \dots v_n) = p(c_j) \cdot \frac{p(v_1 \dots v_n | c_j)}{p(v_1 \dots v_n)}$$

- For all  $C_j$  compute probability  $p(C_j)$ , given values  $v_i$  of all attributes describing the example which we want to classify (assumption: conditional independence of attributes, when estimating  $p(C_j)$  and  $p(C_j | v_i)$ )

$$p(c_j | v_1 \dots v_n) \approx p(c_j) \cdot \prod_i \frac{p(c_j | v_i)}{p(c_j)}$$

- Output  $C_{MAX}$  with maximal posterior probability of class:

$$C_{MAX} = \arg \max_{c_j} p(c_j | v_1 \dots v_n)$$



# Semi-naïve Bayesian classifier

- Naive Bayesian estimation of probabilities (reliable)

$$\frac{p(c_j | v_i)}{p(c_j)} \cdot \frac{p(c_j | v_k)}{p(c_j)}$$

- Semi-naïve Bayesian estimation of probabilities (less reliable)

$$\frac{p(c_j | v_i, v_k)}{p(c_j)}$$

# Probability estimation

- Relative frequency:

$$p(c_j) = \frac{n(c_j)}{N}, p(c_j | v_i) = \frac{n(c_j, v_i)}{n(v_i)} \quad j = 1..k, \text{ for } k \text{ classes}$$

$$[6+, 1-] (7) = 6/7$$

problems with small samples

$$[2+, 0-] (2) = 2/2 = 1$$

- Laplace estimate (prior probability):

$$p(c_j) = \frac{n(c_j) + 1}{N + k} \quad \text{assumes uniform prior distribution of } k \text{ classes}$$

$$[6+, 1-] (7) = 6+1 / 7+2 = 7/9$$

$$[2+, 0-] (2) = 2+1 / 2+2 = 3/4$$

# Probability estimation

- Relative frequency:

$$p(c_j) = \frac{n(c_j)}{N}, p(c_j | v_i) = \frac{n(c_j, v_i)}{n(v_i)} \quad j = 1..k, \text{ for } k \text{ classes}$$

- Prior probability: Laplace law

$$p(c_j) = \frac{n(c_j) + 1}{N + k}$$

- m-estimate:

$$p(c_j) = \frac{n(c_j) + m \cdot p_a(c_j)}{N + m}$$

# Probability estimation: intuition

- Experiment with  $N$  trials,  $n$  successful
- Estimate probability of success of next trial
- **Relative frequency:  $n/N$** 
  - reliable estimate when number of trials is large
  - Unreliable when number of trials is small, e.g.,  $1/1=1$
- **Laplace:  $(n+1)/(N+2)$ ,  $(n+1)/(N+k)$ ,  $k$  classes**
  - Assumes uniform distribution of classes
- **$m$ -estimate:  $(n+m.p_a)/(N+m)$** 
  - Prior probability of success  $p_a$ , parameter  $m$  (weight of prior probability, i.e., number of ‘virtual’ examples )

# Explanation of Bayesian classifier

- Based on information theory
  - Expected number of bits needed to encode a message = optimal code length  $-\log p$  for a message, whose probability is  $p$  (\*)
- Explanation based of the sum of information gains of individual attribute values  $v_i$  (Kononenko and Bratko 1991, Kononenko 1993)

$$\begin{aligned} & -\log( p(c_j | v_1 \dots v_n) ) = \\ & = -\log( p(c_j) ) - \sum_{i=1}^n ( -\log p(c_j) + \log( p(c_j | v_i) ) ) \end{aligned}$$

\*  $\log p$  denotes binary logarithm

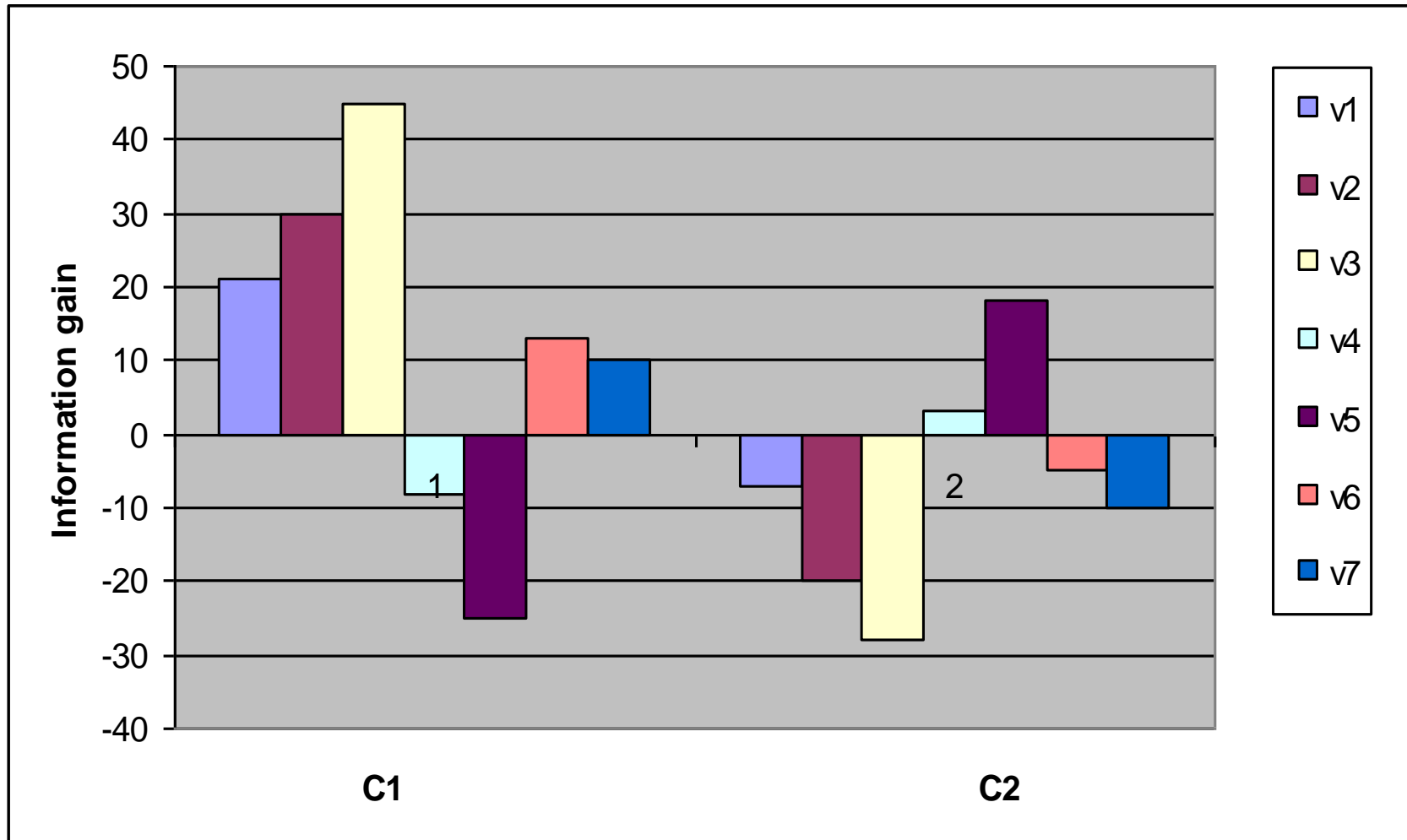
# Example of explanation of semi-naïve Bayesian classifier

Hip surgery prognosis

Class = no (“no complications”, most probable class, 2 class problem)

Attribute value	For decision (bit)	Against (bit)
Age = 70-80	0.07	
Sex = Female		-0.19
Mobility before injury = Fully mobile	0.04	
State of health before injury = Other	0.52	
Mechanism of injury = Simple fall		-0.08
Additional injuries = None	0	
Time between injury and operation > 10 days	0.42	
Fracture classification acc. To Garden = Garden III		-0.3
Fracture classification acc. To Pauwels = Pauwels III		-0.14
Transfusion = Yes	0.07	
Antibiotic profilaxies = Yes		-0.32
Hospital rehabilitation = Yes	0.05	
General complications = None		0
<b>Combination:</b>	0.21	
Time between injury and examination < 6 hours		
AND Hospitalization time between 4 and 5 weeks		
<b>Combination:</b>	0.63	
Therapy = Arthroplastic AND anticoagulant therapy = Yes		

# Visualization of information gains for/against $C_i$



# Naïve Bayesian classifier

- Naïve Bayesian classifier can be used
  - when we have sufficient number of training examples for reliable probability estimation
- It achieves good classification accuracy
  - can be used as ‘gold standard’ for comparison with other classifiers
- Resistant to noise (errors)
  - Reliable probability estimation
  - Uses all available information
- Successful in many application domains
  - Web page and document classification
  - Medical diagnosis and prognosis, ...



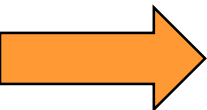
# Improved classification accuracy due to using m-estimate

	Primary tumor	Breast cancer	thyroid	Rheumatology
#instan	339	288	884	355
#class	22	2	4	6
#attrib	17	10	15	32
#values	2	2.7	9.1	9.1
majority	25%	80%	56%	66%
entropy	3.64	0.72	1.59	1.7

	Relative freq.	m-estimate
Primary tumor	48.20%	52.50%
Breast cancer	77.40%	79.70%
hepatitis	58.40%	90.00%
lymphography	79.70%	87.70%

## Part II. Predictive DM techniques

- Decision tree learning
- Bayesian Classifier
- Rule learning
- Evaluation

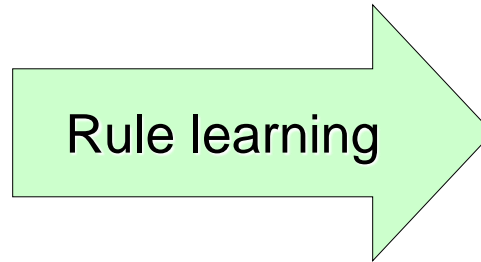


# Rule Learning

Person	Age	Spect. presc.	Astigm.	Tear prod.	Lenses
O1	young	myope	no	reduced	NONE
O2	young	myope	no	normal	SOFT
O3	young	myope	yes	reduced	NONE
O4	young	myope	yes	normal	HARD
O5	young	hypermetrope	no	reduced	NONE
O6-O13	...	...	...	...	...
O14	pre-presbyc	hypermetrope	no	normal	SOFT
O15	pre-presbyc	hypermetrope	yes	reduced	NONE
O16	pre-presbyc	hypermetrope	yes	normal	NONE
O17	presbyopic	myope	no	reduced	NONE
O18	presbyopic	myope	no	normal	NONE
O19-O23	...	...	...	...	...
O24	presbyopic	hypermetrope	yes	normal	NONE

data

knowledge discovery  
from data



Model: a set of rules

Patterns: individual rules

**Given:** transaction data table, relational database (a set of objects, described by attribute values)

**Find:** a classification model in the form of a set of rules;  
or a set of interesting patterns in the form of individual rules

# Rule set representation

- Rule base is a disjunctive set of conjunctive rules
- Standard form of rules:
  - IF Condition THEN Class
  - Class IF Conditions
  - Class  $\leftarrow$  Conditions
- Form of CN2 rules:
  - IF Conditions THEN MajClass [ClassDistr]
- Rule base: {R1, R2, R3, ..., DefaultRule}

# Contact lens data: Classification rules

**Type of task:** prediction and classification

**Hypothesis language:** rules  $X \rightarrow C$ , if X then C  
X conjunction of attribute values, C class

tear production=reduced  $\rightarrow$  **lenses=NONE**

tear production=normal & astigmatism=yes &  
spect. pre.=hypermetrope  $\rightarrow$  **lenses=NONE**

tear production=normal & astigmatism=no  $\rightarrow$  **lenses=SOFT**

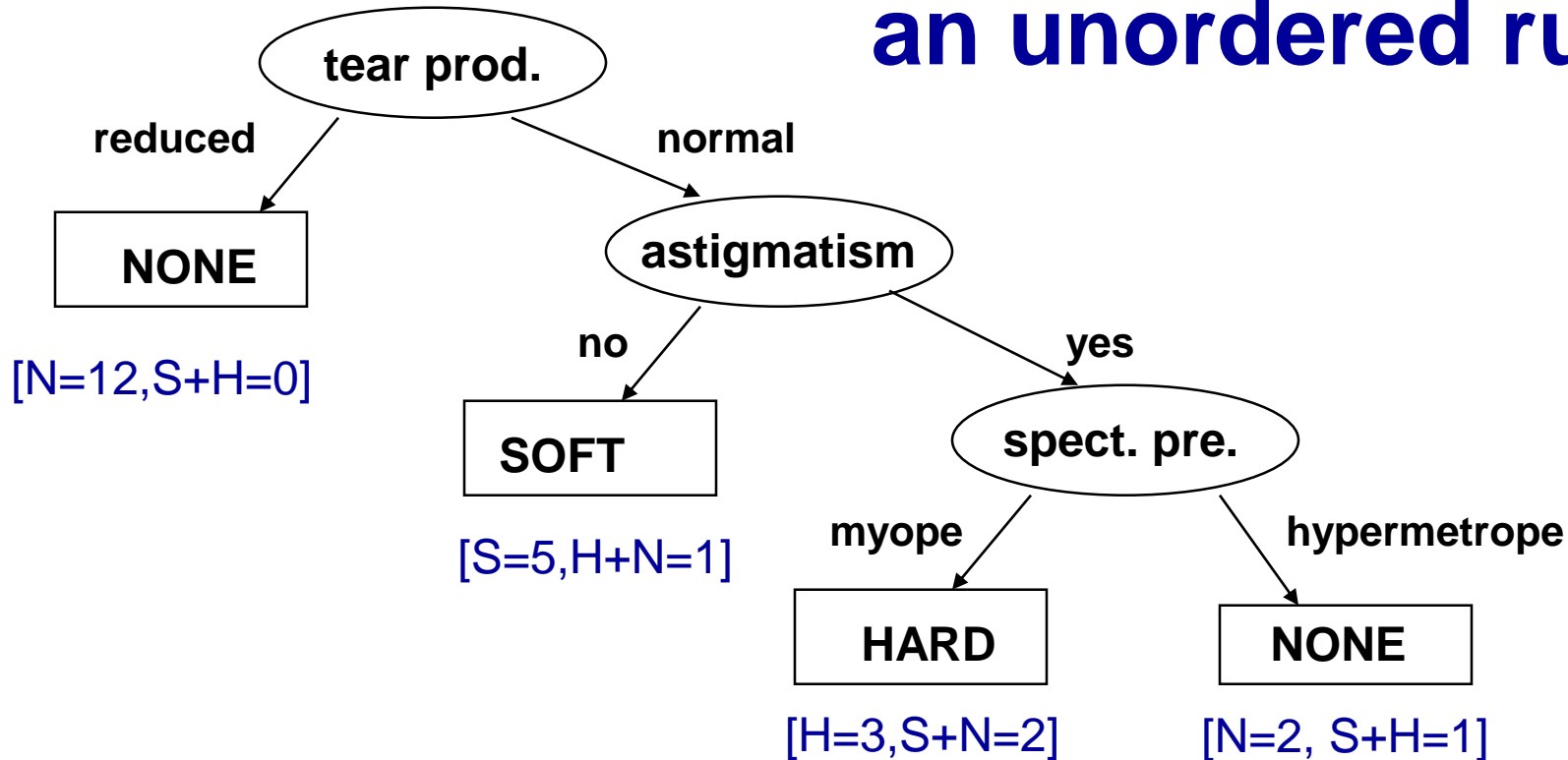
tear production=normal & astigmatism=yes &  
spect. pre.=myope  $\rightarrow$  **lenses=HARD**

DEFAULT **lenses=NONE**

# Rule learning

- Two rule learning approaches:
  - Learn decision tree, convert to rules
  - Learn set/list of rules
    - Learning an unordered set of rules
    - Learning an ordered list of rules
- Heuristics, overfitting, pruning

# Contact lenses: convert decision tree to an unordered rule set



tear production=reduced  $\Rightarrow$  lenses=NONE  $[S=0, H=0, N=12]$

tear production=normal & astigmatism=yes & spect. pre.=hypermetrope  $\Rightarrow$   
lenses=NONE  $[S=0, H=1, N=2]$

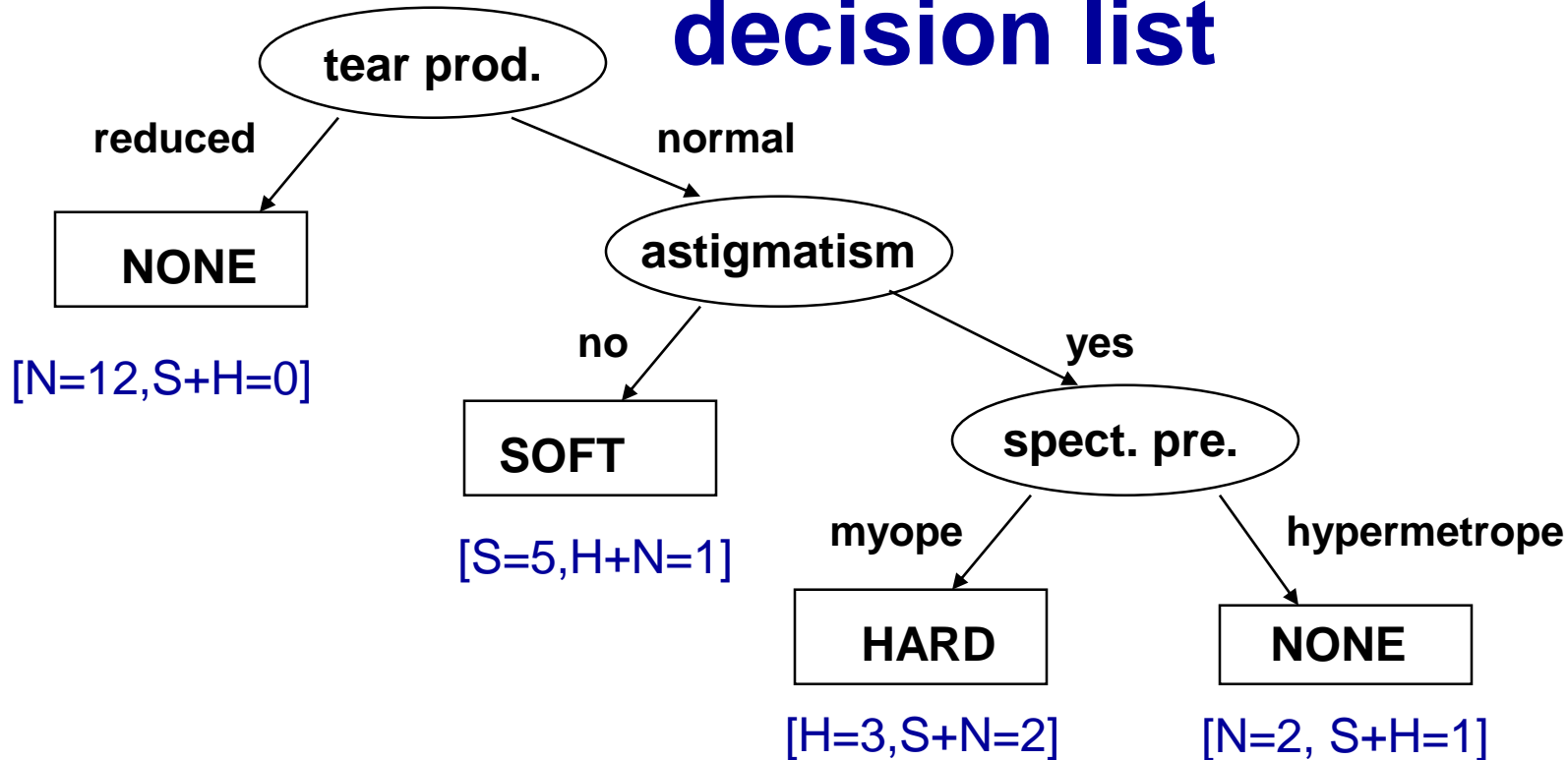
tear production=normal & astigmatism=no  $\Rightarrow$  lenses=SOFT  $[S=5, H=0, N=1]$

tear production=normal & astigmatism=yes & spect. pre.=myope  $\Rightarrow$  lenses=HARD  
 $[S=0, H=3, N=2]$

DEFAULT lenses=NONE

Order independent rule set (may overlap)

# Contact lenses: convert decision tree to decision list



```

IF tear production=reduced THEN lenses=NONE
ELSE /*tear production=normal*/
  IF astigmatism=no THEN lenses=SOFT
  ELSE /*astigmatism=yes*/
    IF spect. pre.=myope THEN lenses=HARD
    ELSE /* spect.pre.=hypermetrope*/
      lenses=NONE
  
```

Ordered (order dependent) rule list



# Converting decision tree to rules, and rule post-pruning (Quinlan 1993)

- Very frequently used method, e.g., in C4.5 and J48
- Procedure:
  - grow a full tree (allowing overfitting)
  - convert the tree to an equivalent set of rules
  - prune each rule independently of others
  - sort final rules into a desired sequence for use

# Concept learning: Task reformulation for rule learning: (pos. vs. neg. examples of Target class)

Person	Age	Spect. presc.	Astigm.	Tear prod.	Lenses
O1	17	myope	no	reduced	NO
O2	23	myope	no	normal	YES
O3	22	myope	yes	reduced	NO
O4	27	myope	yes	normal	YES
O5	19	hypermetrope	no	reduced	NO
O6-O13	...	...	...	...	...
O14	35	hypermetrope	no	normal	YES
O15	43	hypermetrope	yes	reduced	NO
O16	39	hypermetrope	yes	normal	NO
O17	54	myope	no	reduced	NO
O18	62	myope	no	normal	NO
O19-O23	...	...	...	...	...
O24	56	hypermetrope	yes	normal	NO

# Original covering algorithm (AQ, Michalski 1969,86)

**Given** examples of  $N$  classes  $C_1, \dots, C_N$

**for** each class  $C_i$  **do**

–  $E_i := P_i \cup N_i$  ( $P_i$  pos.,  $N_i$  neg.)

–  $\text{RuleBase}(C_i) := \text{empty}$

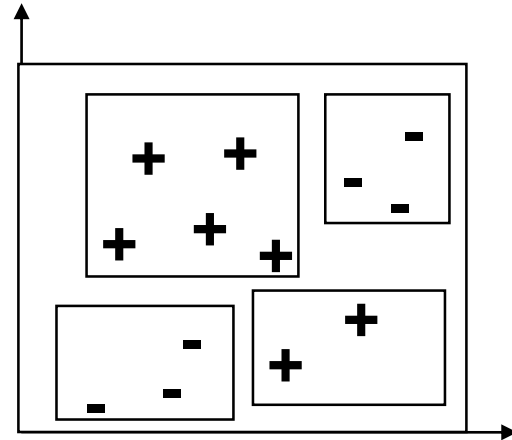
– **repeat** {**learn-set-of-rules**}

- **learn-one-rule**  $R$  covering some positive examples and no negatives

- add  $R$  to  $\text{RuleBase}(C_i)$

- delete from  $P_i$  all pos. ex. covered by  $R$

– **until**  $P_i = \text{empty}$



# Multi-class learning: One-against-all learning strategy

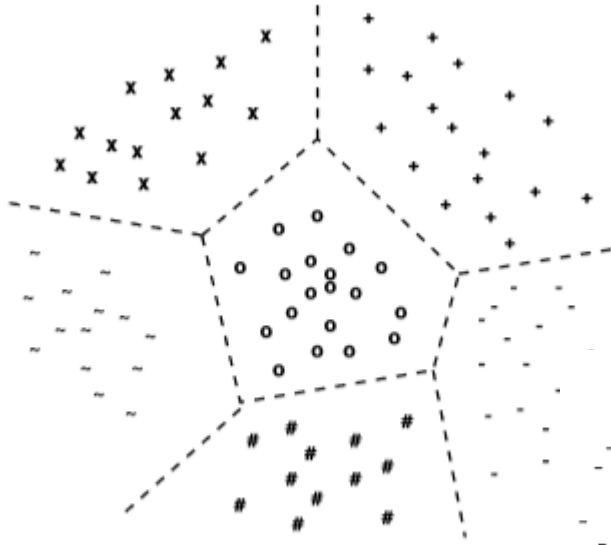


Fig. 10.2: A multiclass classification

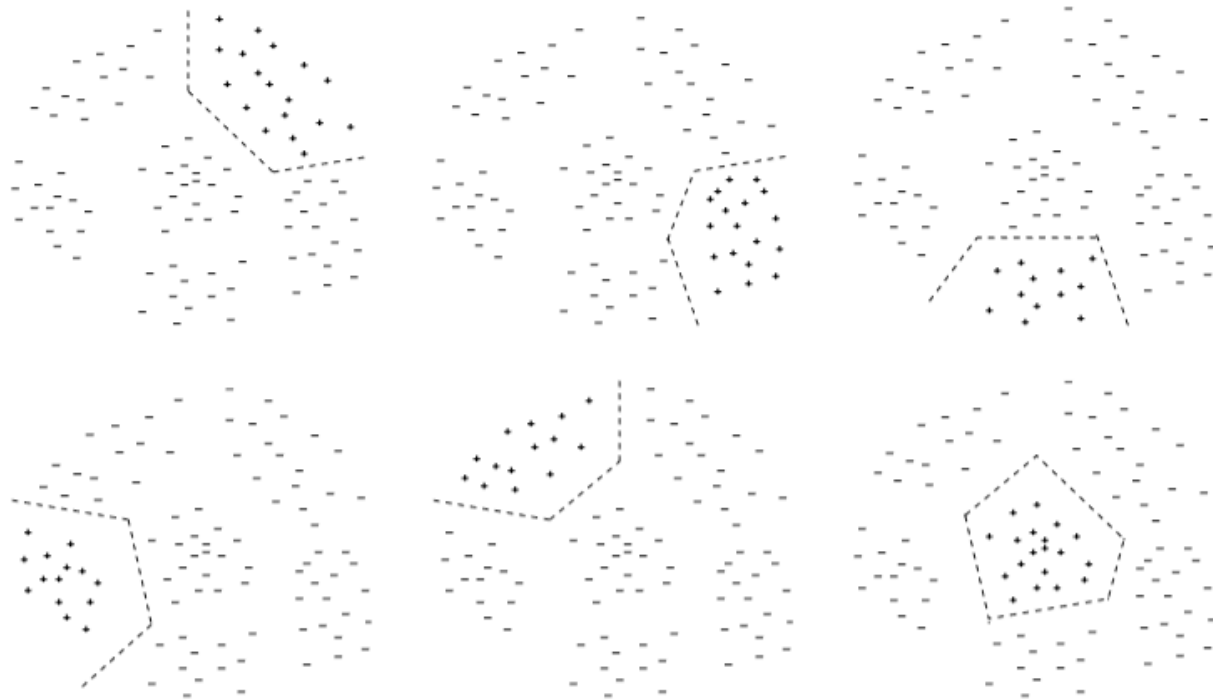
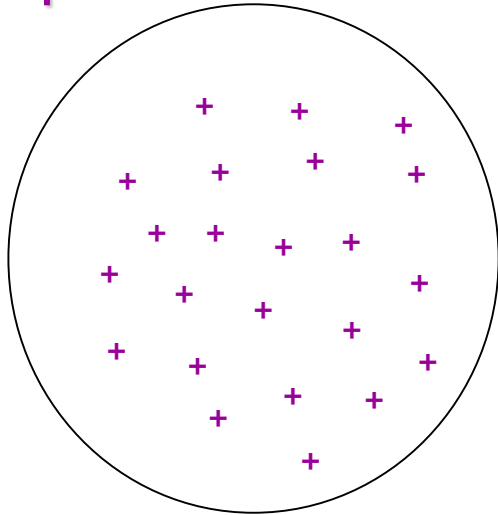


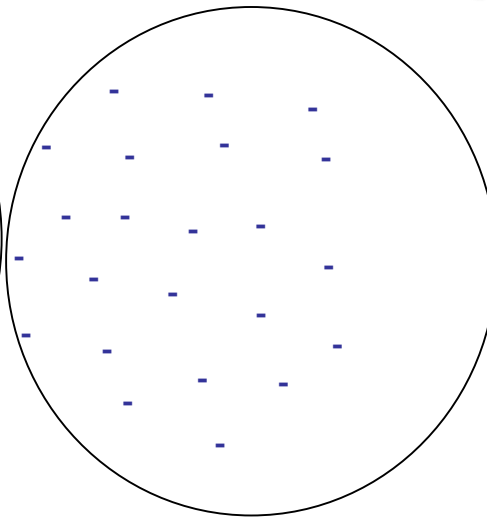
Fig. 10.4: The six binary learning problems that are the result of one-against-all class binarization of the multiclass dataset of Figure 10.2.

# Covering algorithm

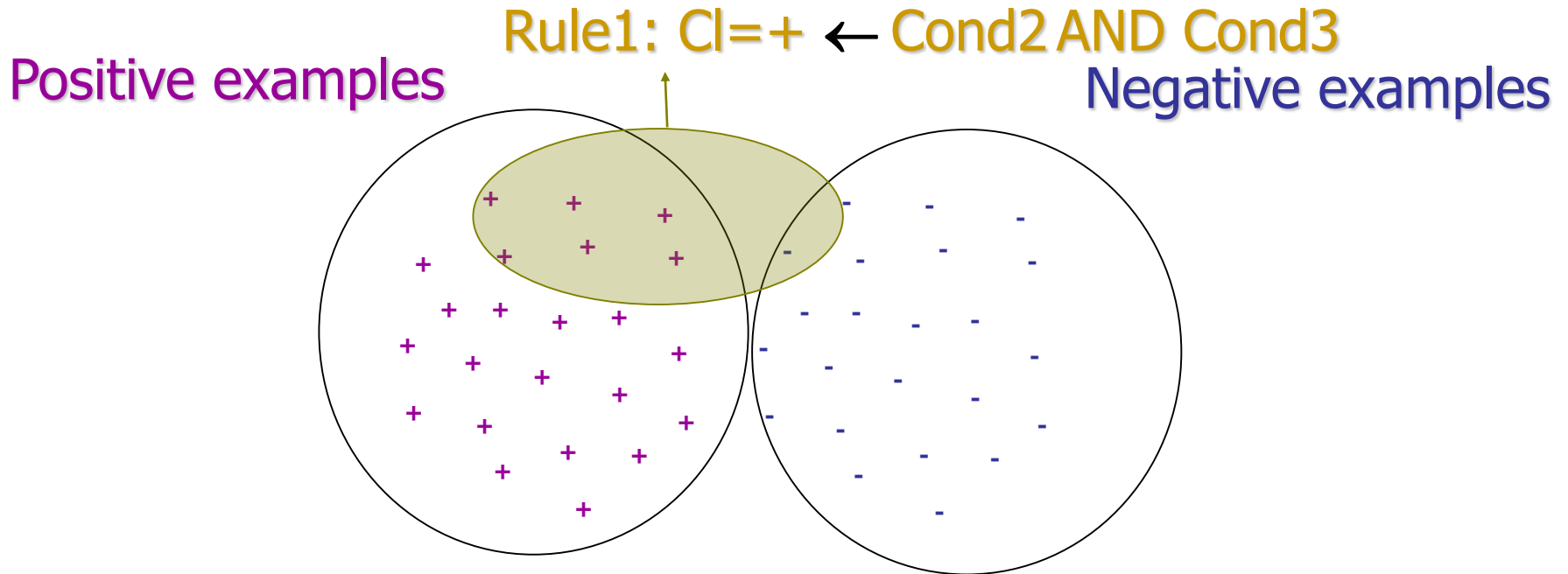
Positive examples



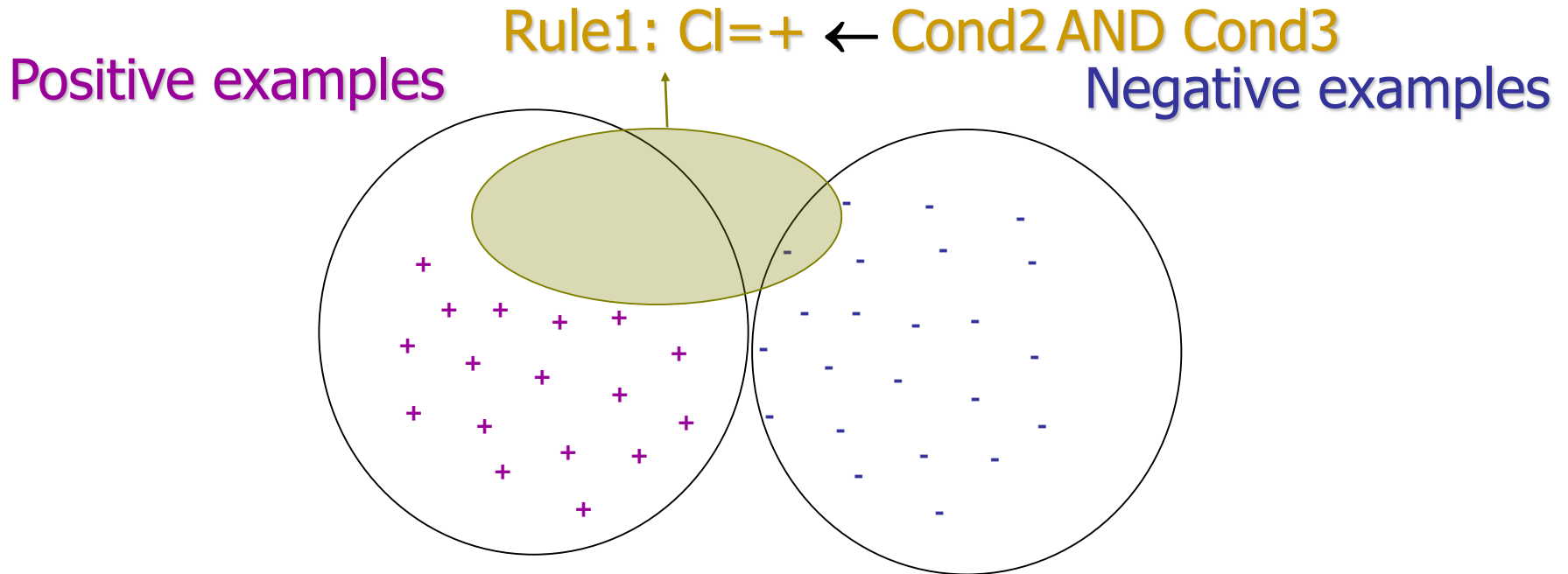
Negative examples



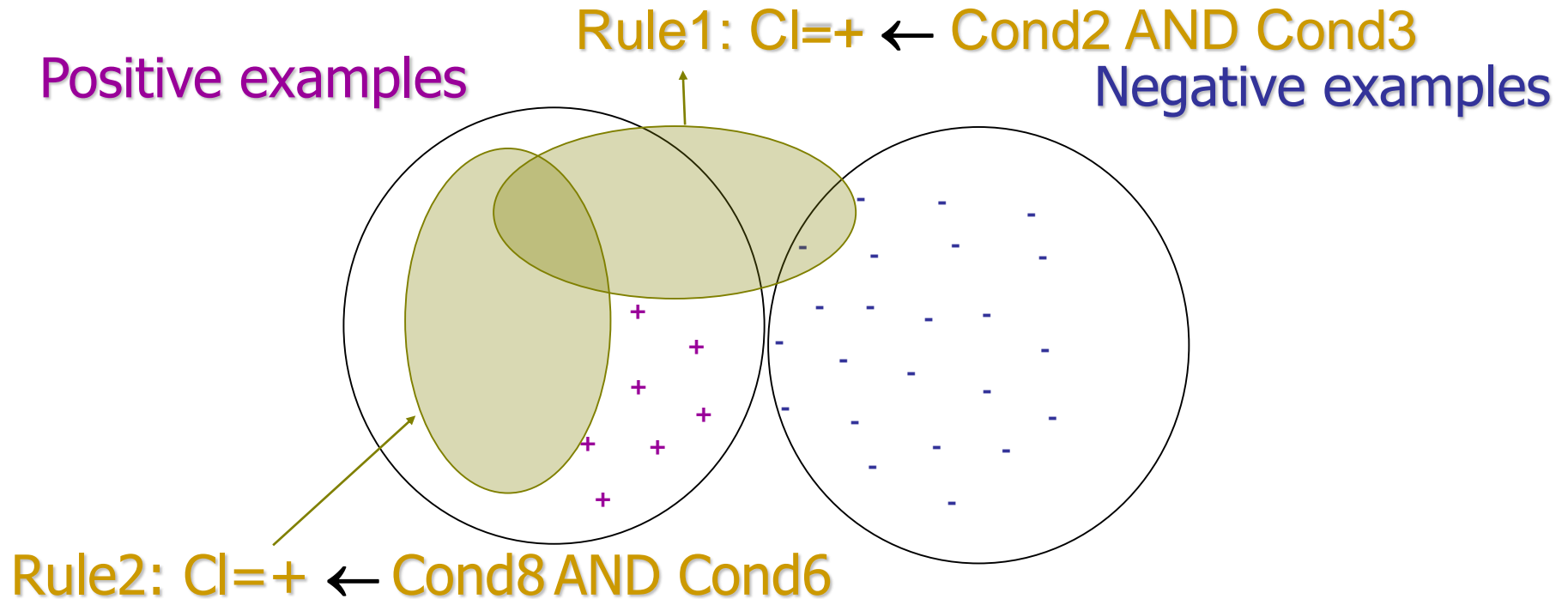
# Covering algorithm



# Covering algorithm



# Covering algorithm





# Learn-one-rule: Greedy vs. beam search

- learn-one-rule by greedy general-to-specific search, at each step selecting the `best` descendant, no backtracking
  - e.g., the best descendant of the initial rule  
`lenses=NONE` ←
  - is rule `lenses=NONE` ← tear production=reduced
- beam search: maintain a list of k best candidates at each step; descendants (specializations) of each of these k candidates are generated, and the resulting set is again reduced to k best candidates

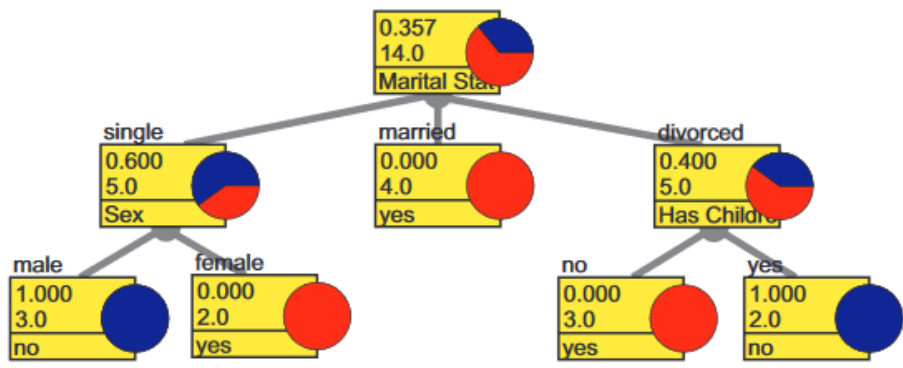
# Learn-one-rule: Greedy vs. beam search

- learn-one-rule by greedy general-to-specific search, at each step selecting the `best' descendant, no backtracking
  - e.g., best descendant of initial rule `lenses=NONE` ←  
is rule `lenses=NONE` ← `tear production=reduced`
  - e.g., best descendant of initial rule `Approved=yes` ←  
is rule `Approved=yes` ← `Marital status = married`
- beam search: maintain a list of k best candidates at each step; descendants (specializations) of each of these k candidates are generated, and the resulting set is again reduced to k best candidates

# Recall: Binary classification problem

## Survey data

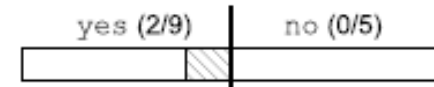
Education	Marital Status	Sex	Has Children	Approved
primary	single	male	no	no
primary	single	male	yes	no
primary	married	male	no	yes
university	divorced	female	no	yes
university	married	female	yes	yes
secondary	single	male	no	no
university	single	female	no	yes
secondary	divorced	female	no	yes
secondary	single	female	yes	yes
secondary	married	male	yes	yes
primary	married	female	no	yes
secondary	divorced	male	yes	no
university	divorced	female	yes	no
secondary	divorced	male	no	yes



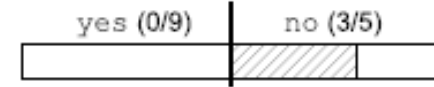
# Survey data: Classification rule learning

Education	Marital Status	Sex	Has Children	Approved
primary	single	male	no	no
primary	single	male	yes	no
primary	married	male	no	yes
university	divorced	female	no	yes
university	married	female	yes	yes
secondary	single	male	no	no
university	single	female	no	yes
secondary	divorced	female	no	yes
secondary	single	female	yes	yes
secondary	married	male	yes	yes
primary	married	female	no	yes
secondary	divorced	male	yes	no
university	divorced	female	yes	no
secondary	divorced	male	no	yes

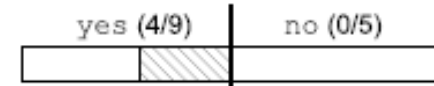
```
IF MaritalStatus = single
  AND Sex = female
THEN Approved = yes
```



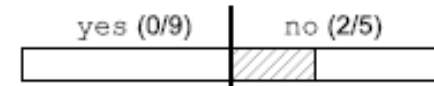
```
IF MaritalStatus = single
  AND Sex = male
THEN Approved = no
```



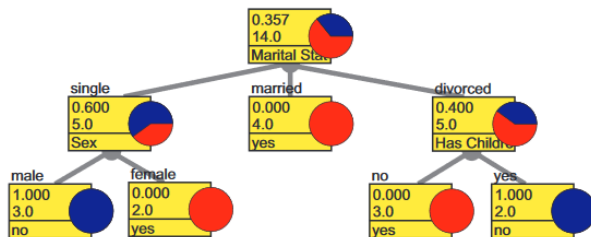
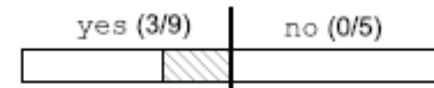
```
IF MaritalStatus = married
THEN Approved = yes
```



```
IF MaritalStatus = divorced
  AND HasChildren = yes
THEN Approved = no
```



```
IF MaritalStatus = divorced
  AND HasChildren = no
THEN Approved = yes
```

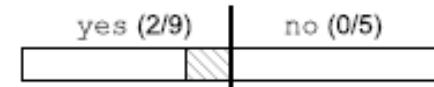


# Survey data:

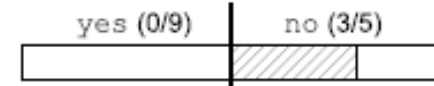
## Classification rule pruning

Education	Marital Status	Sex	Has Children	Approved
primary	single	male	no	no
primary	single	male	yes	no
primary	married	male	no	yes
university	divorced	female	no	yes
university	married	female	yes	yes
secondary	single	male	no	no
university	single	female	no	yes
secondary	divorced	female	no	yes
secondary	single	female	yes	yes
secondary	married	male	yes	yes
primary	married	female	no	yes
secondary	divorced	male	yes	no
university	divorced	female	yes	no
secondary	divorced	male	no	yes

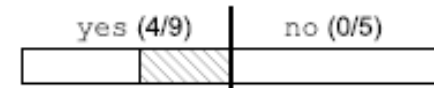
IF MaritalStatus = single  
AND Sex = female  
THEN Approved = yes



IF MaritalStatus = single  
AND Sex = male  
THEN Approved = no



IF MaritalStatus = married  
THEN Approved = yes



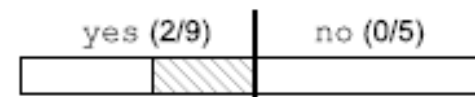
IF MaritalStatus = divorced  
AND HasChildren = yes  
THEN Approved = no



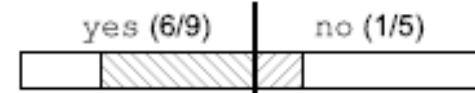
IF MaritalStatus = divorced  
AND HasChildren = no  
THEN Approved = yes



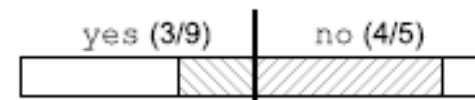
IF MaritalStatus = married  
THEN Approved = yes



IF Sex = female  
THEN Approved = yes

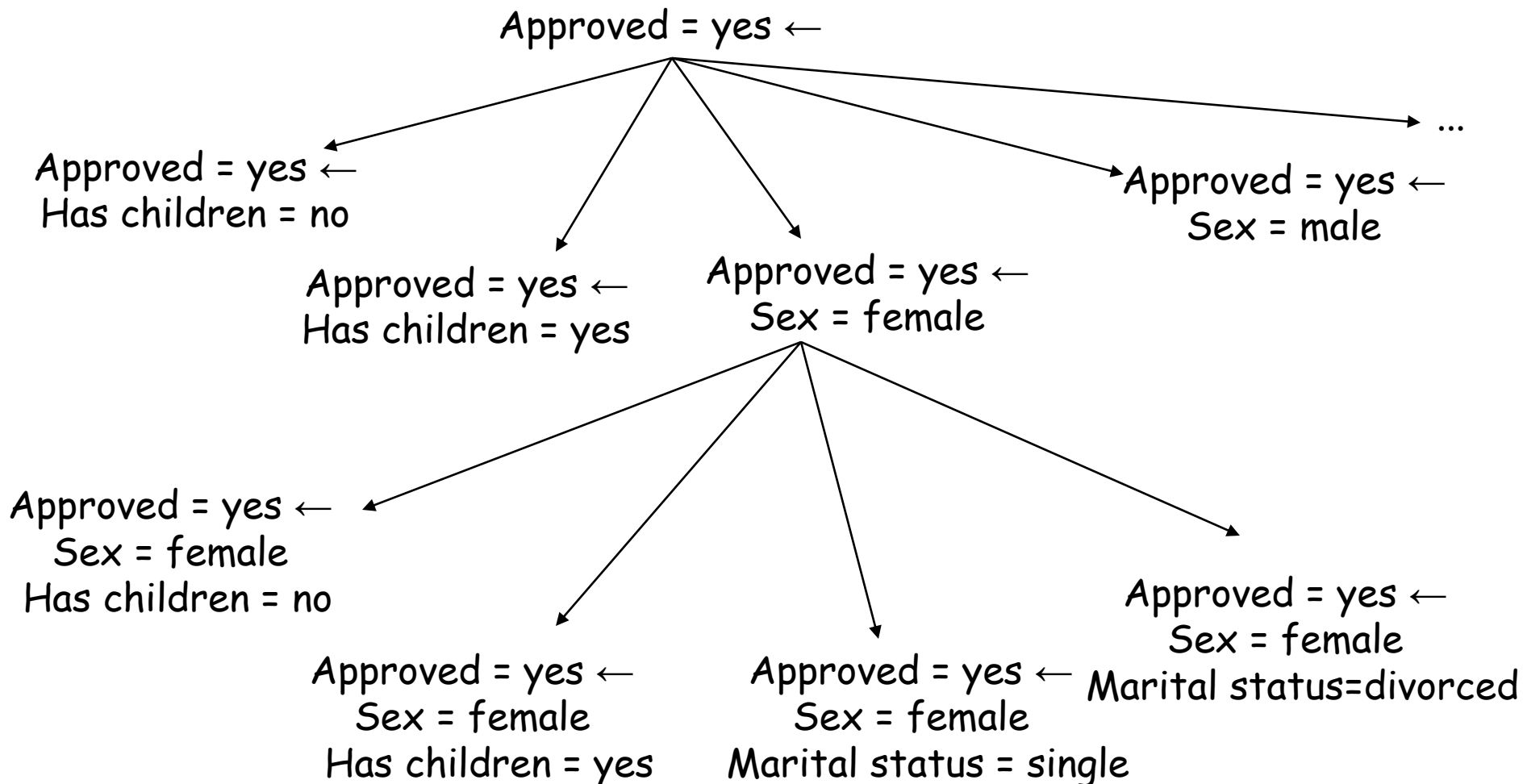


IF Sex = male  
THEN Approved = no

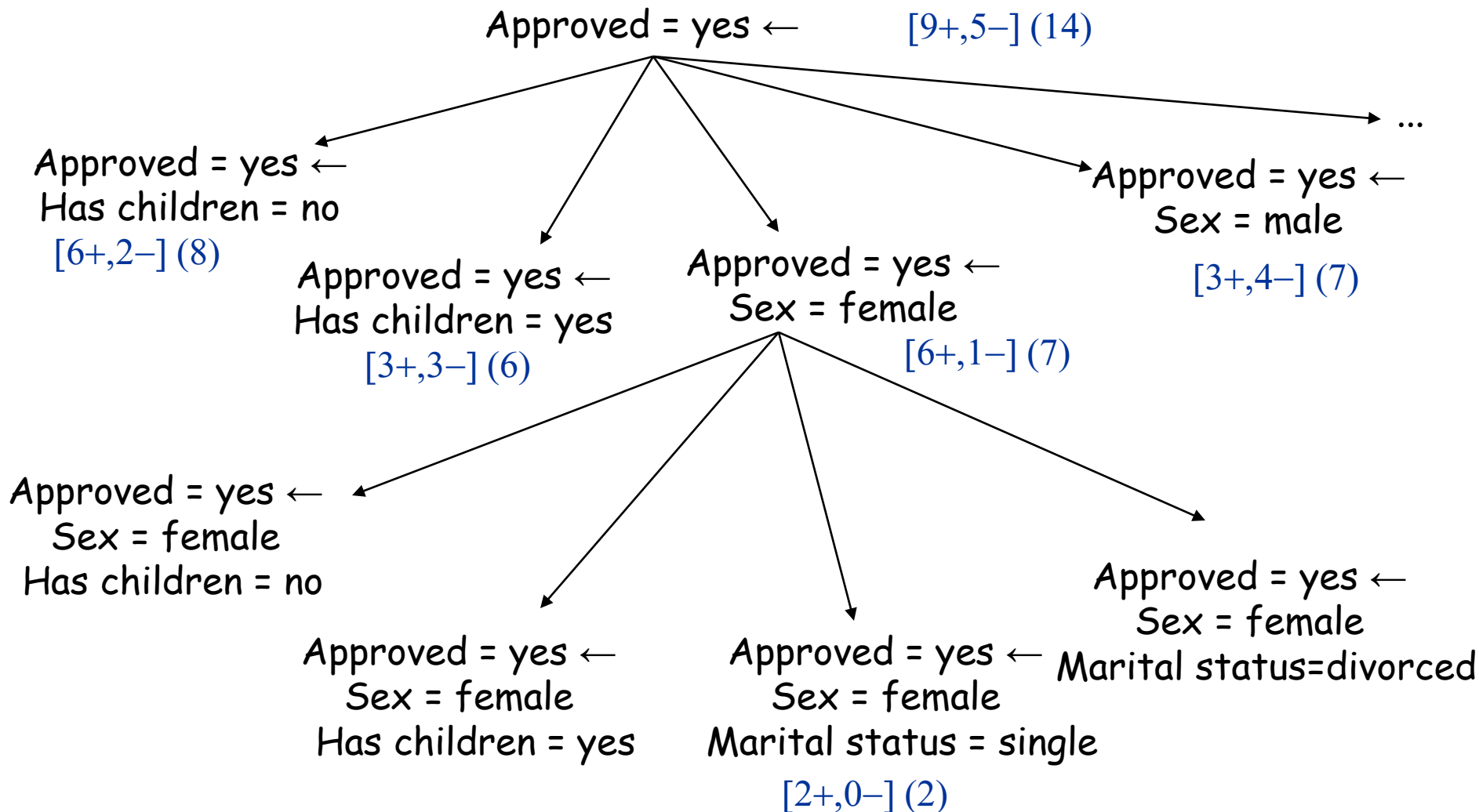


DEFAULT Approved = yes

# Learn-one-rule as heuristic search: 2<sup>nd</sup> rule in Survey data example



# Learn-one-rule as heuristic search: 2<sup>nd</sup> rule in Survey data example



# What is “high” rule accuracy (rule precision) ?

- Rule evaluation measures:
  - aimed at maximizing classification accuracy
  - minimizing Error = 1 - Accuracy
  - avoiding overfitting
- BUT: Rule accuracy/precision should be traded off against the “default” accuracy/precision of the rule **CI ← true**
  - 68% accuracy is OK if there are 20% examples of that class in the training set, but bad if there are 80%
- **Relative accuracy** (*relative precision*)
  - $\text{RAcc}(\text{CI} \leftarrow \text{Cond}) = p(\text{CI} \mid \text{Cond}) - p(\text{CI})$



# Learn-one-rule: search heuristics

- Assume two classes (+,-), learn rules for + class (C1). Search for specializations of one rule  $R = C1 \leftarrow \text{Cond}$  from RuleBase.
- Expected **classification accuracy**:  $A(R) = p(C1|\text{Cond})$
- **Informativity** (info needed to specify that example covered by Cond belongs to C1):  $I(R) = -\log_2 p(C1|\text{Cond})$
- **Accuracy gain** (increase in expected accuracy):  

$$AG(R',R) = p(C1|\text{Cond}') - p(C1|\text{Cond})$$
- **Information gain** (decrease in the information needed):  

$$IG(R',R) = \log_2 p(C1|\text{Cond}') - \log_2 p(C1|\text{Cond})$$
- **Weighted** measures favoring more general rules: WAG, WIG  

$$WAG(R',R) =$$

$$p(\text{Cond}')/p(\text{Cond}) \cdot (p(C1|\text{Cond}') - p(C1|\text{Cond}))$$
- **Weighted relative accuracy** trades off coverage and relative accuracy  $WRAcc(R) = p(\text{Cond}) \cdot (p(C1|\text{Cond}) - p(C1))$

# Ordered set of rules: if-then-else rules

- rule Class IF Conditions is learned by first determining Conditions and then Class
- **Notice:** mixed sequence of classes  $C_1, \dots, C_n$  in RuleBase
- **But: ordered** execution when classifying a new instance: rules are sequentially tried and the first rule that `fires' (covers the example) is used for classification
- **Decision list**  $\{R_1, R_2, R_3, \dots, D\}$ : rules  $R_i$  are interpreted as **if-then-else** rules
- If no rule fires, then DefaultClass (majority class in  $E_{cur}$ )

# Sequential covering algorithm

- RuleBase := empty
- $E_{\text{cur}} := E$
- **repeat**
  - learn-one-rule R
  - RuleBase := RuleBase U R
  - $E_{\text{cur}} := E_{\text{cur}} - \{\text{examples covered and correctly classified by R}\}$  **(DELETE ONLY POS. EX.!)**
  - **until** performance(R,  $E_{\text{cur}}$ ) < ThresholdR
- RuleBase := sort RuleBase by performance(R,E)
- return RuleBase

# Learn ordered set of rules (CN2, Clark and Niblett 1989)

- RuleBase := empty
- $E_{\text{cur}} := E$
- **repeat**
  - learn-one-rule R
  - RuleBase := RuleBase U R
  - $E_{\text{cur}} := E_{\text{cur}} - \{\text{all examples covered by R}\}$   
**(NOT ONLY POS. EX.!)**
- **until** performance(R,  $E_{\text{cur}}$ ) < ThresholdR
- RuleBase := sort RuleBase by performance(R, E)
- RuleBase := RuleBase U DefaultRule( $E_{\text{cur}}$ )

# Learn-one-rule: Beam search in CN2

- Beam search in CN2 learn-one-rule algo.:
  - construct BeamSize of best rule bodies (conjunctive conditions) that are statistically significant
  - BestBody - min. entropy of examples covered by Body
  - construct best rule  $R := \text{Head} \leftarrow \text{BestBody}$  by adding majority class of examples covered by BestBody in rule Head
- performance  $(R, E_{\text{cur}}) : - \text{Entropy}(E_{\text{cur}})$ 
  - performance  $(R, E_{\text{cur}}) < \text{ThresholdR}$  (neg. num.)
  - Why? Ent.  $> t$  is bad, Perf. =  $-\text{Ent} < -t$  is bad

# Variations

- Sequential vs. simultaneous covering of data (as in TDIDT): choosing between attribute-values vs. choosing attributes
- Learning rules vs. learning decision trees and converting them to rules
- Pre-pruning vs. post-pruning of rules
- What statistical evaluation functions to use
- Probabilistic classification
  
- Best performing rule learning algorithm: Ripper
- JRip implementation of Ripper in WEKA, available in ClowdFlows

# CN2 rule learner in Orange



CN2 Rule Induction

Name  
CN2 rule inducer

Rule ordering  
 Ordered  
 Unordered

Covering algorithm  
 Exclusive  
 Weighted  $\gamma$ : 0.70

Rule search  
Evaluation measure: Entropy  
Beam width: 5

Rule filtering  
Minimum rule coverage: 1  
Maximum rule length: 5  
 Statistical significance (default  $\alpha$ ): 1.00  
 Relative significance (parent  $\alpha$ ): 1.00

Apply Automatically

? 📄

# Probabilistic classification

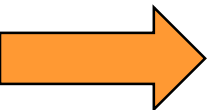
- In the ordered case of standard CN2 rules are interpreted in an IF-THEN-ELSE fashion, and the first fired rule assigns the class.
- In the unordered case all rules are tried and all rules which fire are collected. If a clash occurs, a probabilistic method is used to resolve the clash.
- A simplified example:
  1. tear production=reduced => lenses=NONE [S=0,H=0,N=12]
  2. tear production=normal & astigmatism=yes & spect. pre.=hypermetrope => lenses=NONE [S=0,H=1,N=2]
  3. tear production=normal & astigmatism=no => lenses=SOFT [S=5,H=0,N=1]
  4. tear production=normal & astigmatism=yes & spect. pre.=myope => lenses=HARD [S=0,H=3,N=2]
  5. DEFAULT lenses=NONE

Suppose we want to classify a person with normal tear production and astigmatism. Two rules fire: rule 2 with coverage [S=0,H=1,N=2] and rule 4 with coverage [S=0,H=3,N=2]. The classifier computes total coverage as [S=0,H=4,N=4], resulting in probabilistic classification into class **H** with probability 0.5 and **N** with probability 0.5. In this case, the clash can not be resolved, as both probabilities are equal.



## Part II. Predictive DM techniques

- Decision tree learning
- Bayesian Classifier
- Rule learning
- Evaluation



# Classifier evaluation

- Accuracy and Error
- n-fold cross-validation
- Confusion matrix
- ROC

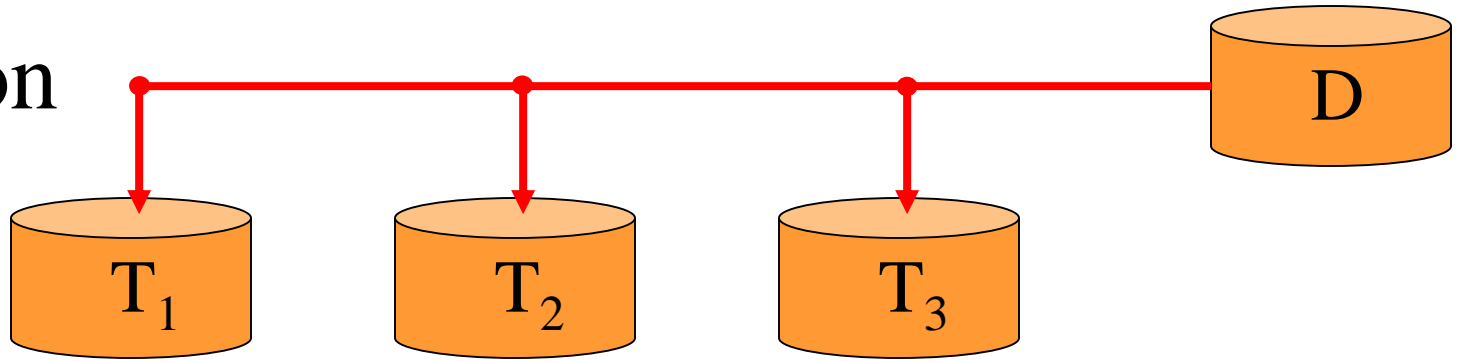
# Evaluating hypotheses

- **Use of induced hypotheses**
  - discovery of new patterns, new knowledge
  - classification of new objects
- **Evaluating the quality of induced hypotheses**
  - Accuracy, Error =  $1 - \text{Accuracy}$
  - classification accuracy on testing examples = percentage of correctly classified instances
    - split the example set into training set (e.g. 70%) to induce a concept, and test set (e.g. 30%) to test its accuracy
    - more elaborate strategies: 10-fold cross validation, leave-one-out, ...
  - comprehensibility (compactness)
  - information contents (information score), significance

# n-fold cross validation

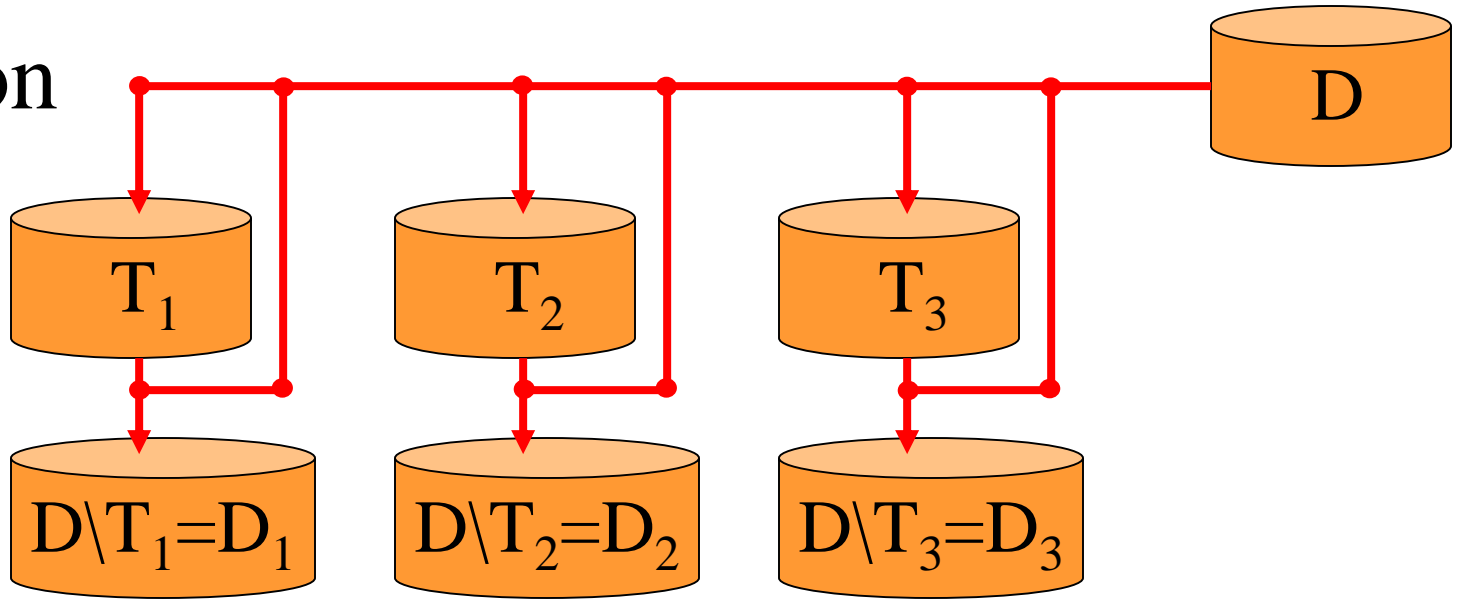
- A method for accuracy estimation of classifiers
- Partition set  $D$  into  $n$  disjoint, almost equally-sized folds  $T_i$  where  $\bigcup_i T_i = D$
- **for**  $i = 1, \dots, n$  **do**
  - form a training set out of  $n-1$  folds:  $D_i = D \setminus T_i$
  - induce classifier  $H_i$  from examples in  $D_i$
  - use fold  $T_i$  for testing the accuracy of  $H_i$
- Estimate the accuracy of the classifier by averaging accuracies over  $n$  folds  $T_i$

• Partition



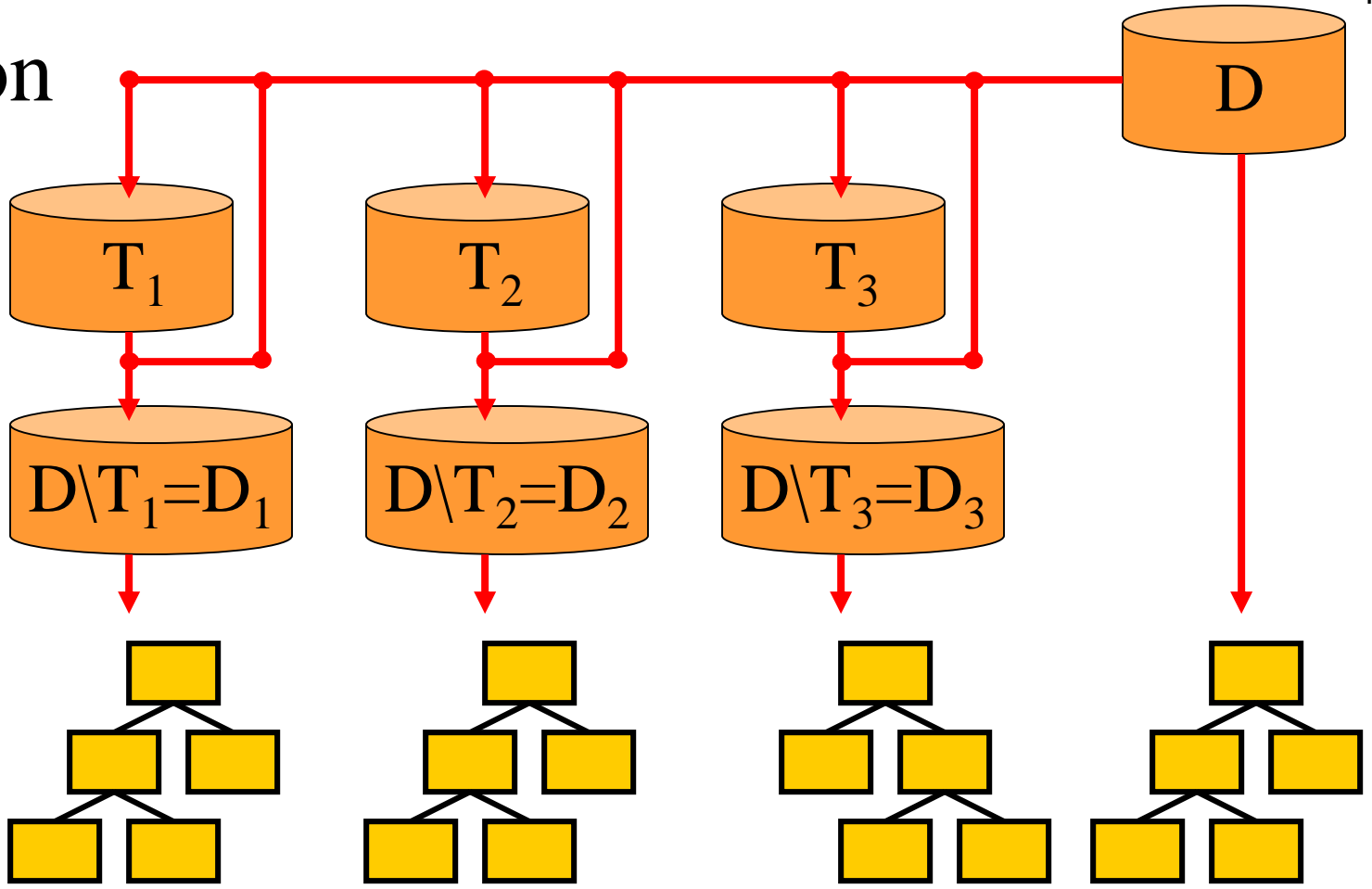
•Partition

•Train

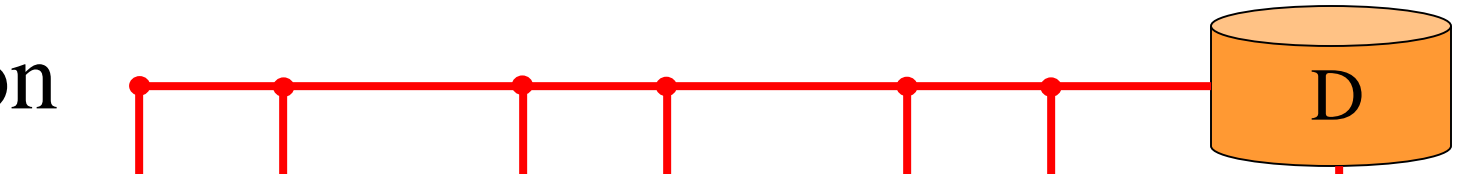


• Partition

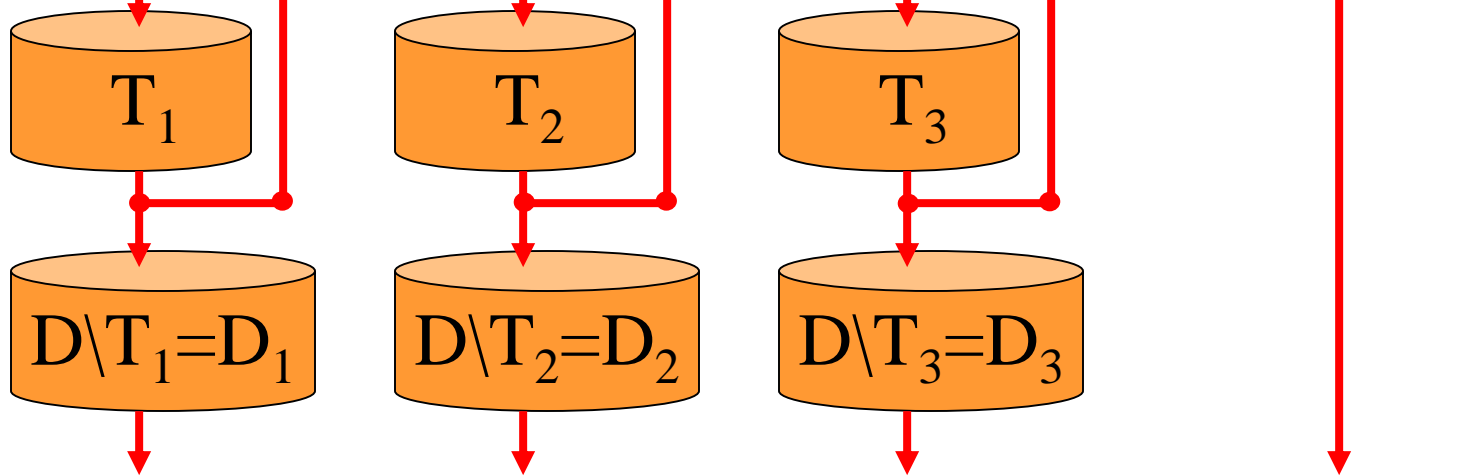
• Train



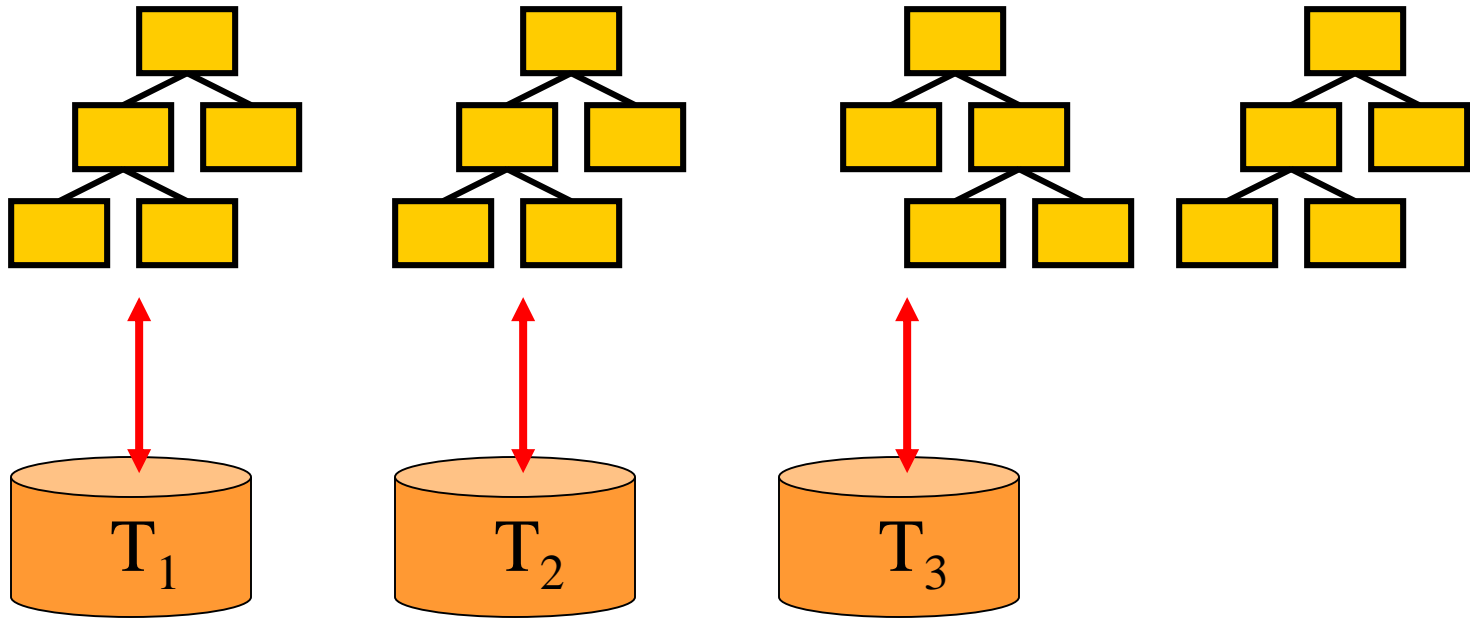
• Partition



• Train



• Test





# Confusion matrix and rule (in)accuracy

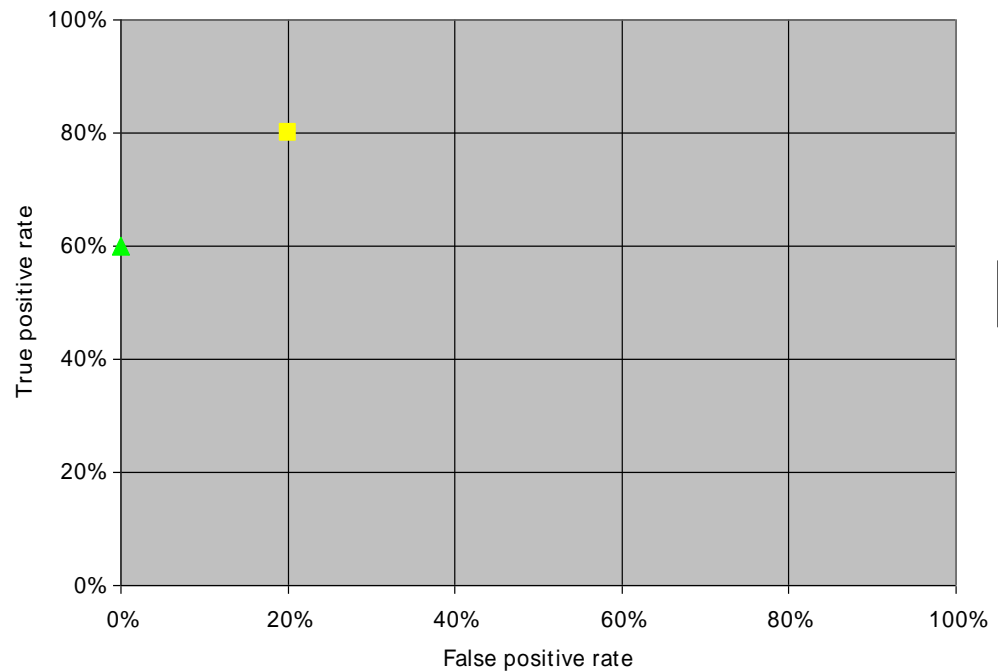
- Accuracy of a classifier is measured as  $TP+TN / N$ .
- Suppose two rules are both 80% accurate on an evaluation dataset, are they always equally good?
  - e.g., Rule 1 correctly classifies 40 out of 50 positives and 40 out of 50 negatives; Rule 2 correctly classifies 30 out of 50 positives and 50 out of 50 negatives
  - on a test set which has more negatives than positives, Rule 2 is preferable;
  - on a test set which has more positives than negatives, Rule 1 is preferable; unless...
  - ...the proportion of positives becomes so high that the 'always positive' predictor becomes superior!
- Conclusion: classification accuracy is not always an appropriate rule quality measure

# ROC space

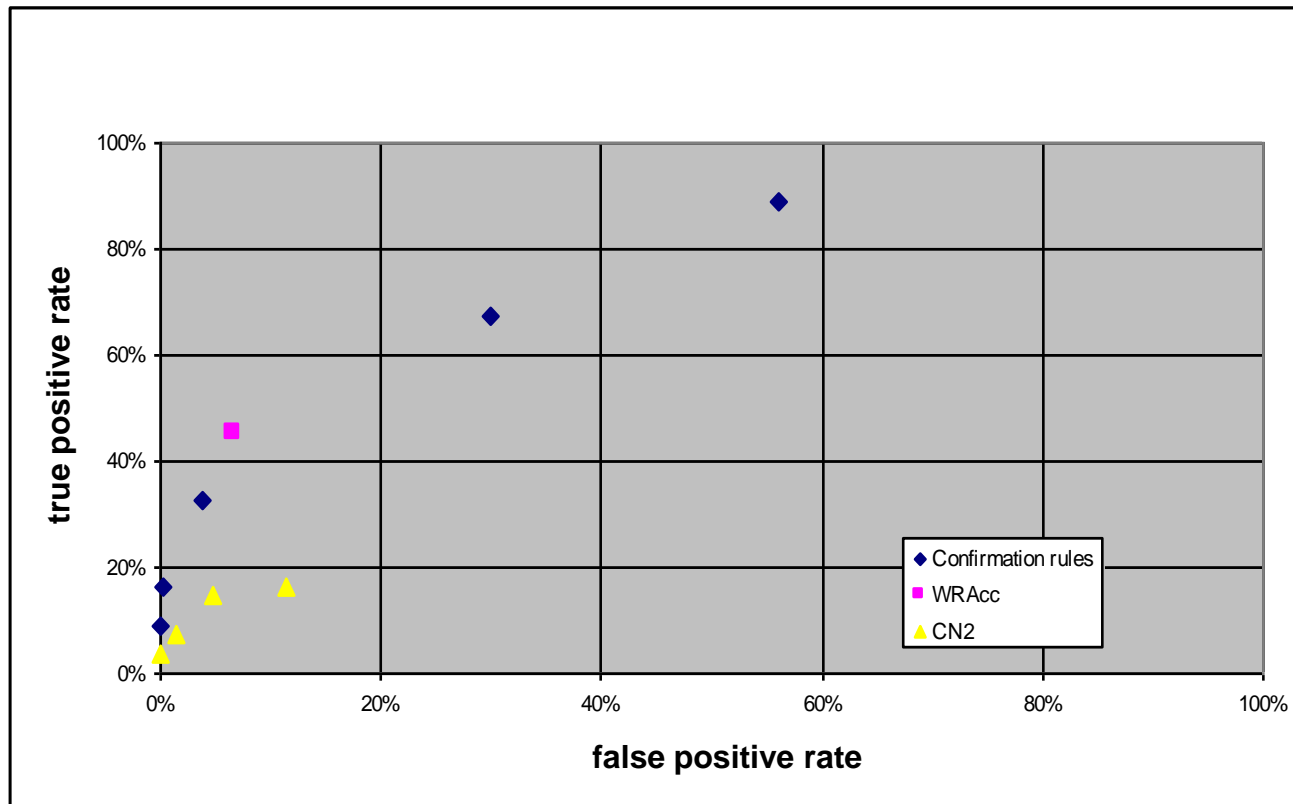
- **True positive rate** =  
#true pos. / #pos.
  - $TPR_1 = 40/50 = 80\%$
  - $TPR_2 = 30/50 = 60\%$
- **False positive rate**  
= #false pos. / #neg.
  - $FPR_1 = 10/50 = 20\%$
  - $FPR_2 = 0/50 = 0\%$
- **ROC space** has
  - FPr on X axis
  - TPr on Y axis

Classifier 1			
	Predicted positive	Predicted negative	
Positive examples	40	10	50
Negative examples	10	40	50
	50	50	100

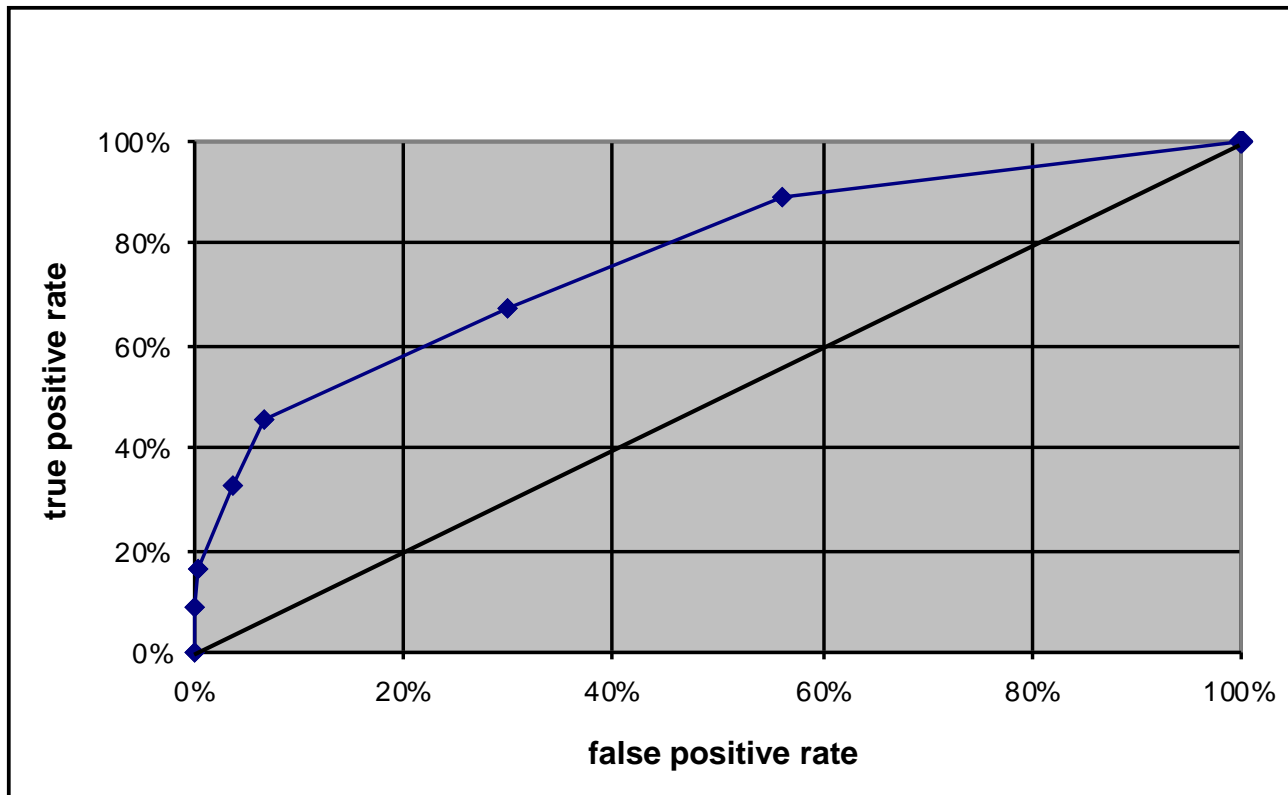
Classifier 2			
	Predicted positive	Predicted negative	
Positive examples	30	20	50
Negative examples	0	50	50
	30	70	100



# The ROC space



# The ROC convex hull



# Course Outline

## I. Introduction

- Data Mining and KDD process
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## II. Predictive DM

- Decision Tree learning
- Bayesian classifier
- Classification rule learning
- Classifier evaluation

## III. Predictive DM

- Regression

## IV. Descriptive DM

- Predictive vs. descriptive induction
- Subgroup discovery
- Association rule learning
- Hierarchical clustering

## III. Predictive DM – Regression

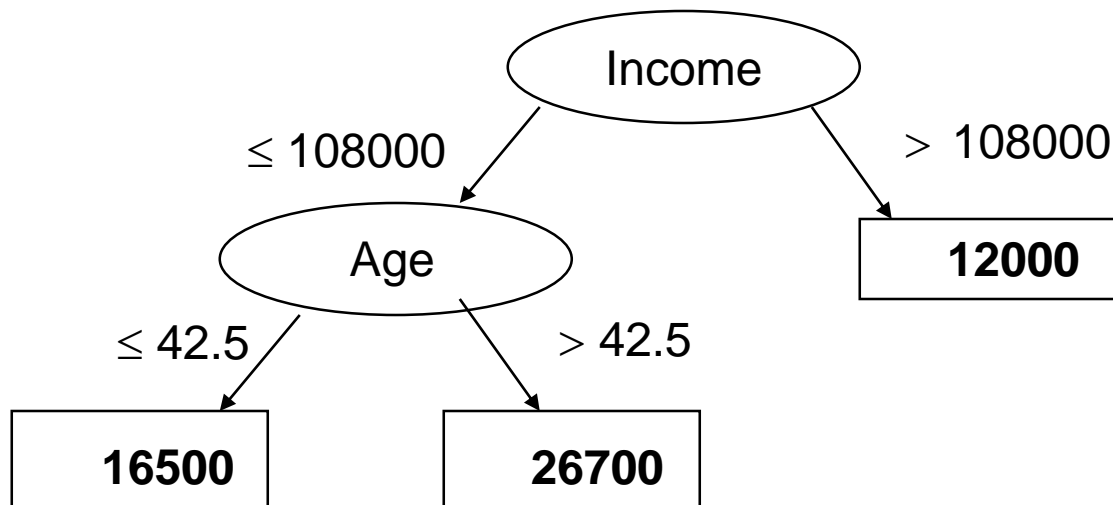
- Estimation or regression task: given objects described with attribute values, induce a model to predict the numeric class value
- Data are objects, characterized with attributes (discrete or continuous), classes of objects are continuous (numeric)
- Regression trees, linear and logistic regression, ANN, kNN, ...
- Regression tree learners, model tree learners:
  - M5, M5P (implemented in WEKA), Tree (in Orange)

# Estimation/regression example:

## Customer data

Customer	Gender	Age	Income	Spent	
c1	male	30	214000	18800	
c2	female	19	139000	15100	
c3	male	55	50000	12400	
c4	female	48	26000	8600	
c5	male	63	191000	28100	
O6-O13	...	...	...	...	
c14	female	61	95000	18100	
c15	male	56	44000	12000	
c16	male	36	102000	13800	
c17	female	57	215000	29300	
c18	male	33	67000	9700	
c19	female	26	95000	11000	
c20	female	55	214000	28800	

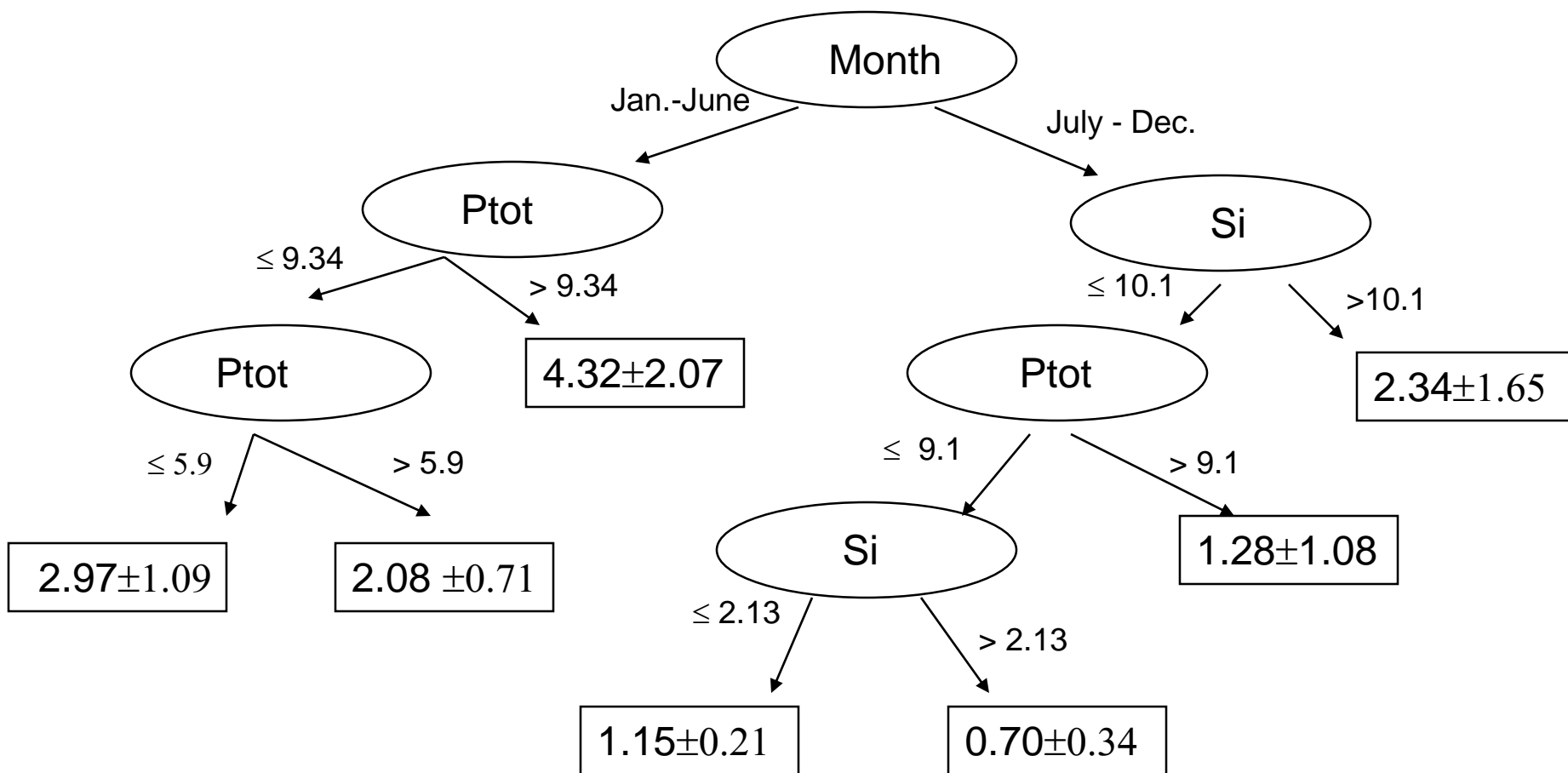
# Customer data: regression tree



In the nodes one usually has  
Predicted value +- st. deviation



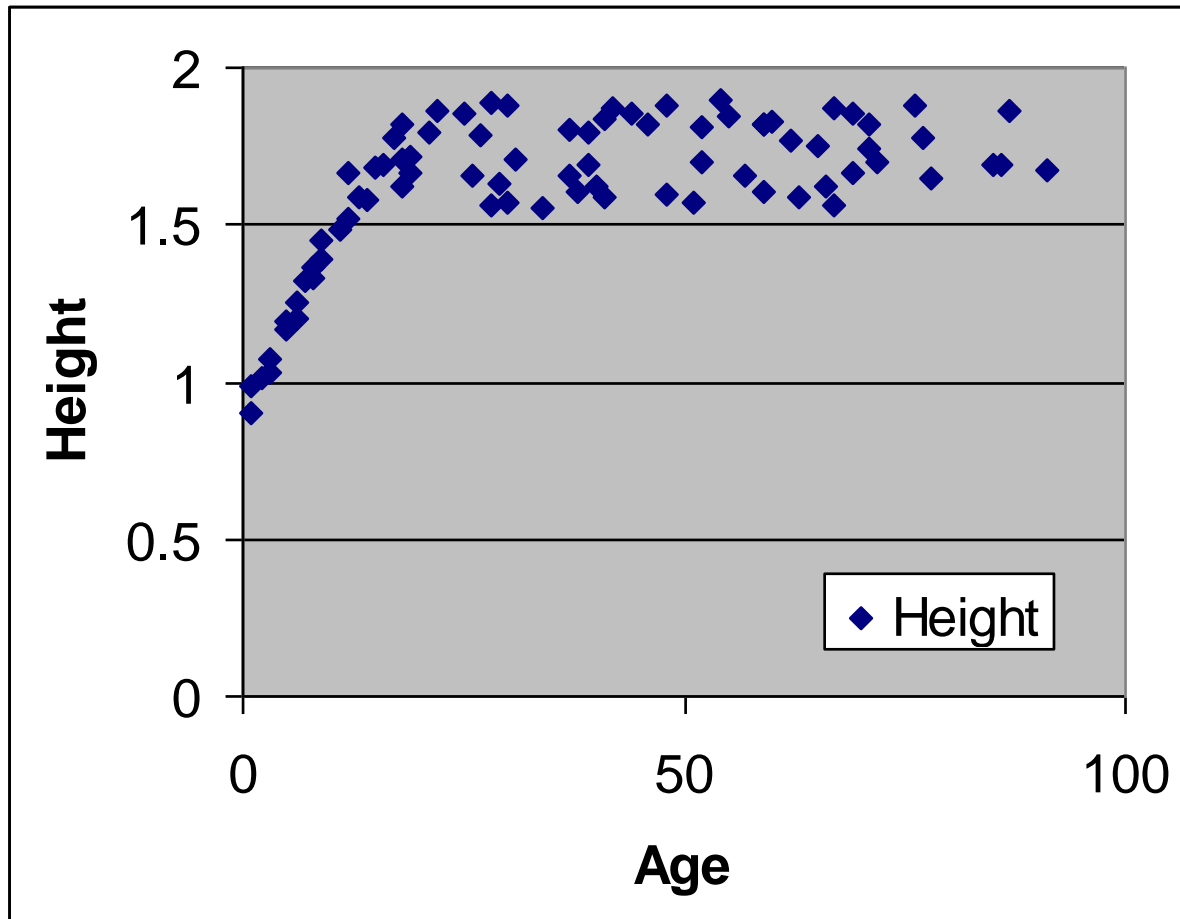
# Predicting algal biomass: regression tree



<b>Regression</b>	<b>Classification</b>
<b>Data:</b> attribute-value description	
<b>Target variable:</b> Continuous	<b>Target variable:</b> Categorical (nominal)
<b>Evaluation:</b> cross validation, separate test set, ...	
<b>Error:</b> MSE, MAE, RMSE, ...	<b>Error:</b> 1-accuracy
<b>Algorithms:</b> Linear regression, regression trees, ...	<b>Algorithms:</b> Decision trees, Naïve Bayes, ...
<b>Baseline predictor:</b> Mean of the target variable	<b>Baseline predictor:</b> Majority class

# Example regression problem

- data about 80 people: Age and Height



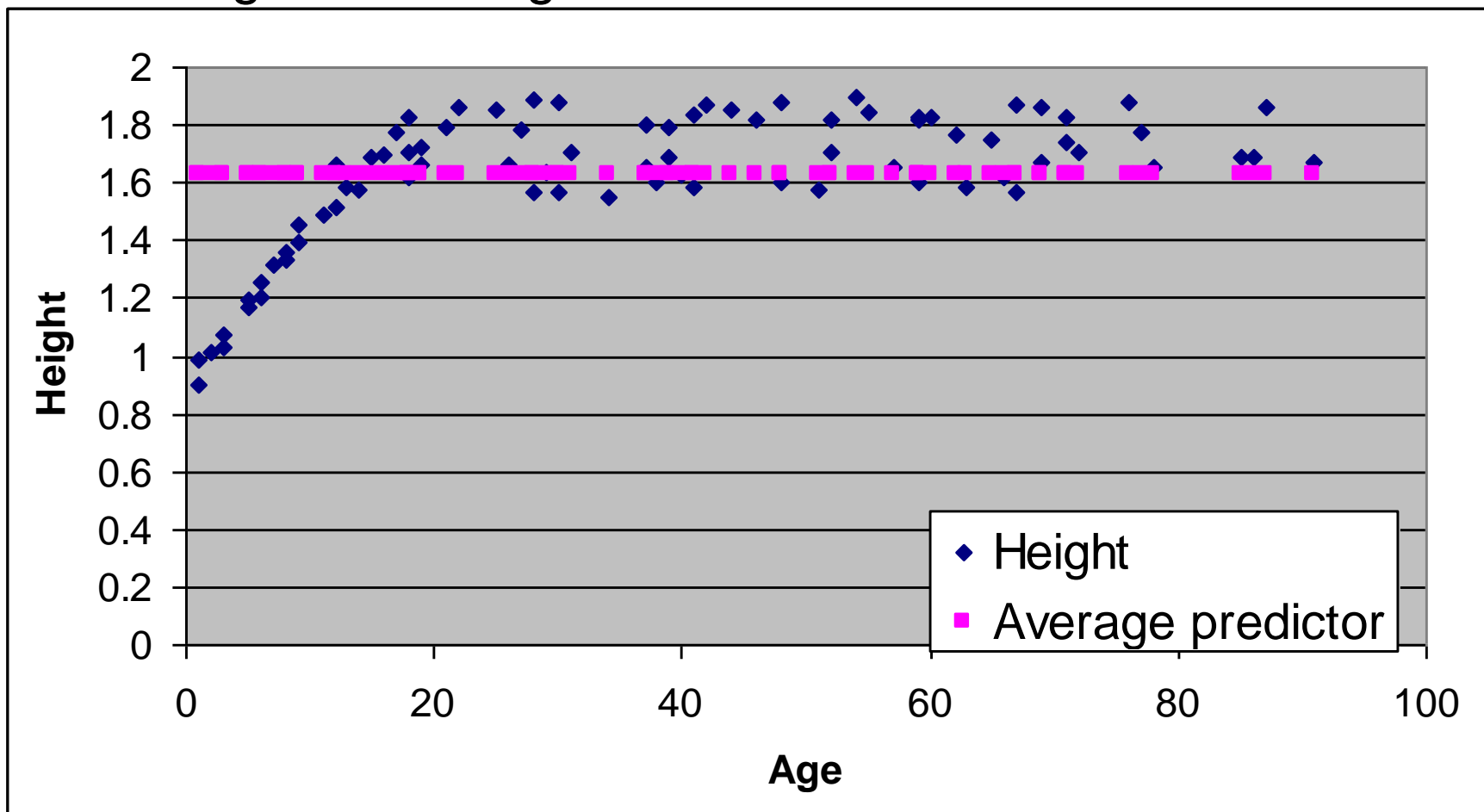
Age	Height
3	1.03
5	1.19
6	1.26
9	1.39
15	1.69
19	1.67
22	1.86
25	1.85
41	1.59
48	1.60
54	1.90
71	1.82
...	...

# Test set

Age	Height
2	0.85
10	1.4
35	1.7
70	1.6

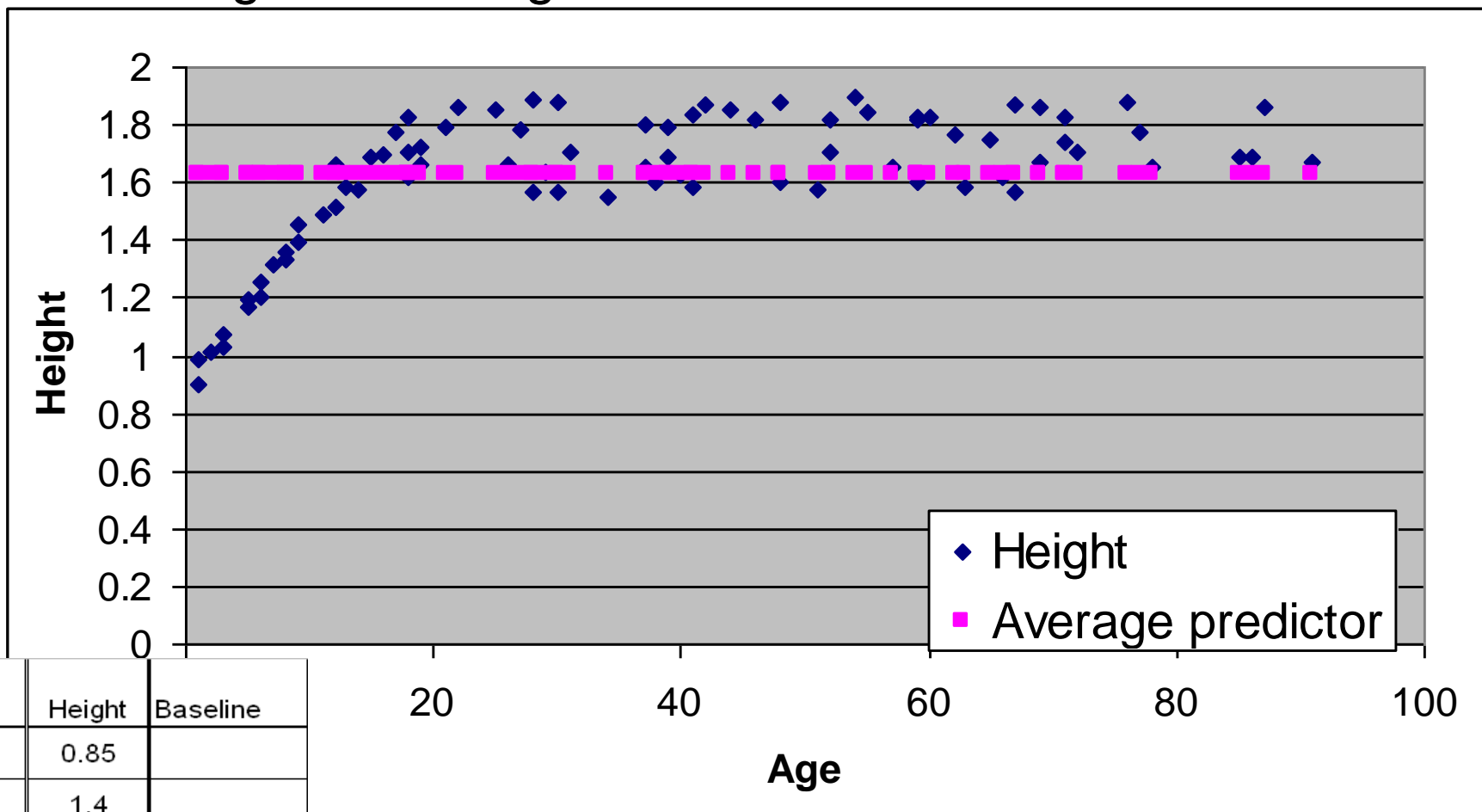
# Baseline numeric model

- Average of the target variable



# Baseline numeric predictor

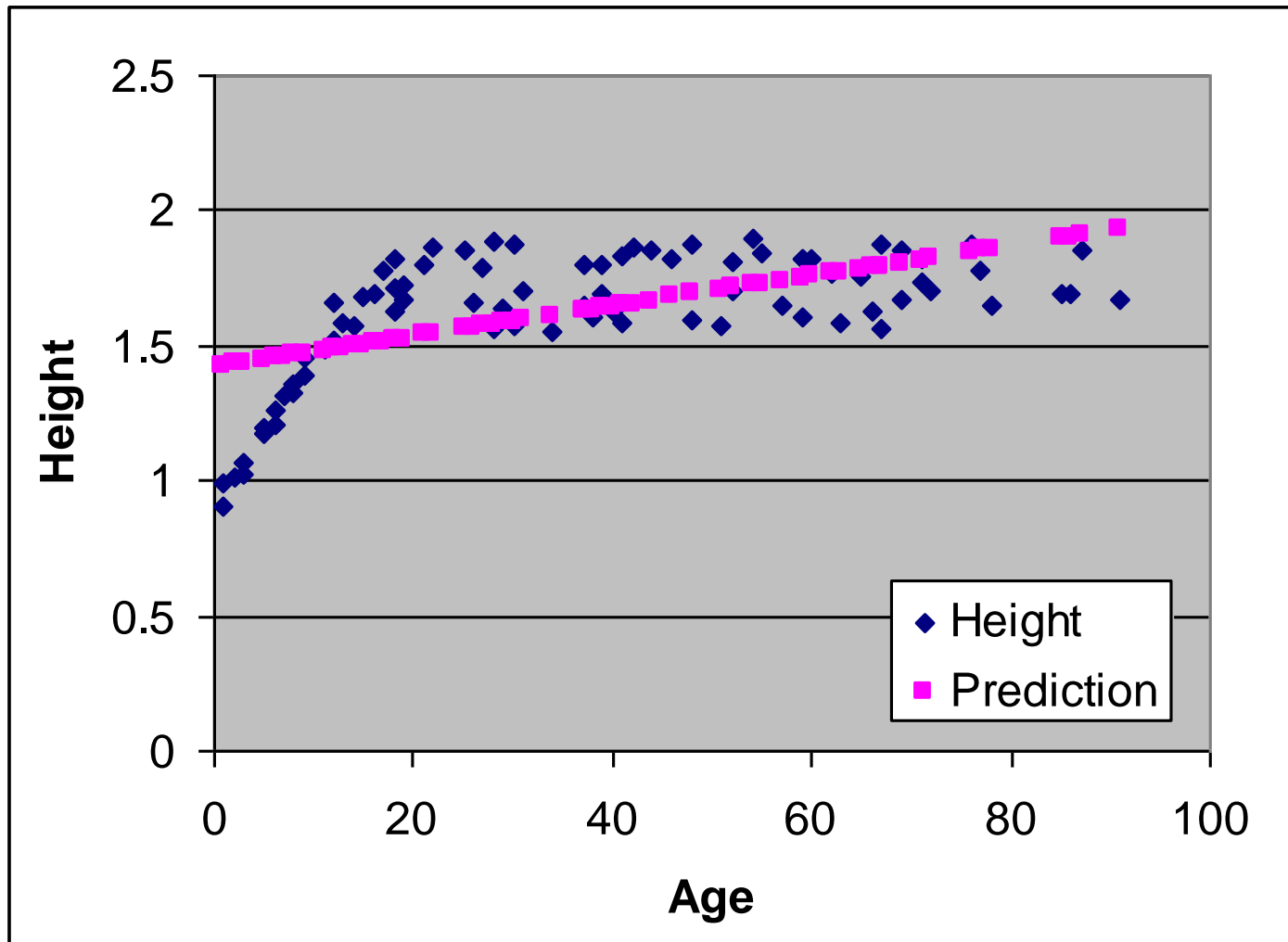
- Average of the target variable is 1.63



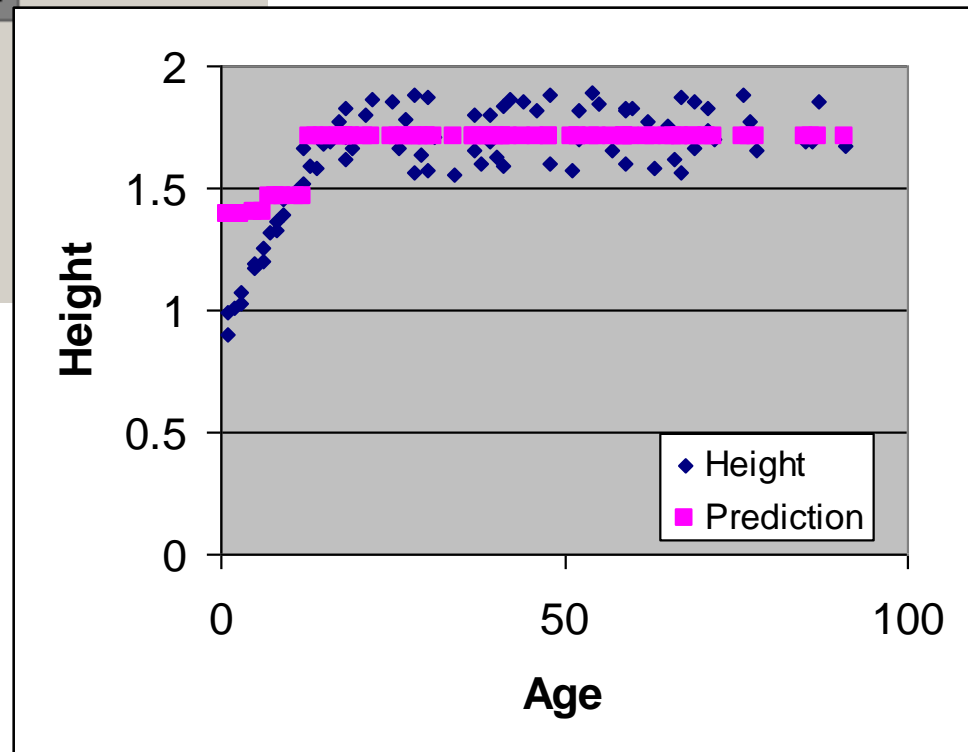
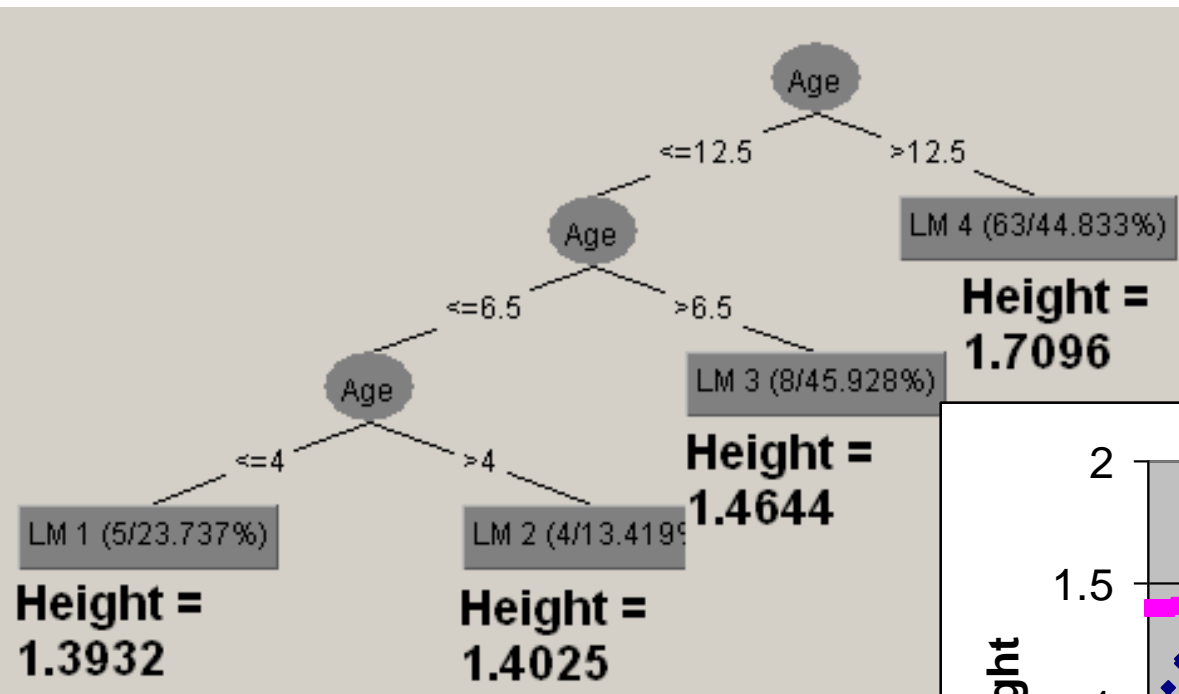
Age	Height	Baseline
2	0.85	
10	1.4	
35	1.7	
70	1.6	

# Linear Regression Model

$$\text{Height} = 0.0056 * \text{Age} + 1.4181$$

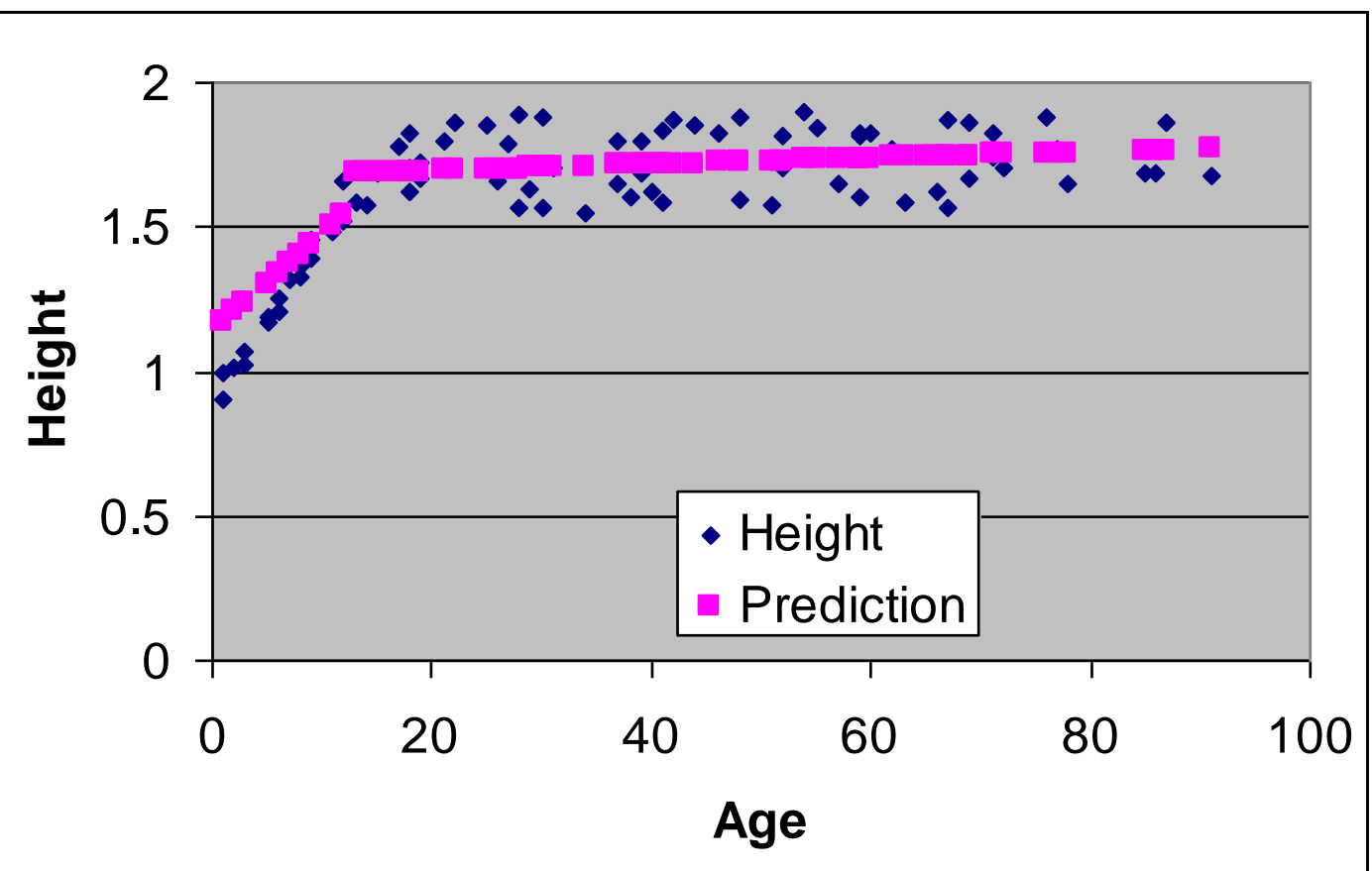
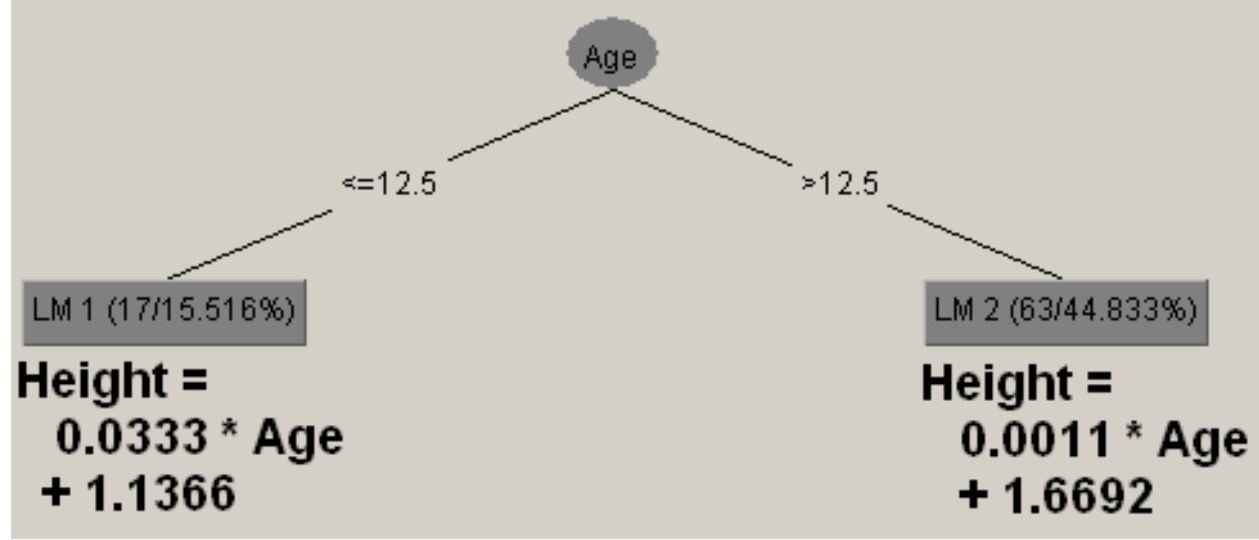


# Regression tree



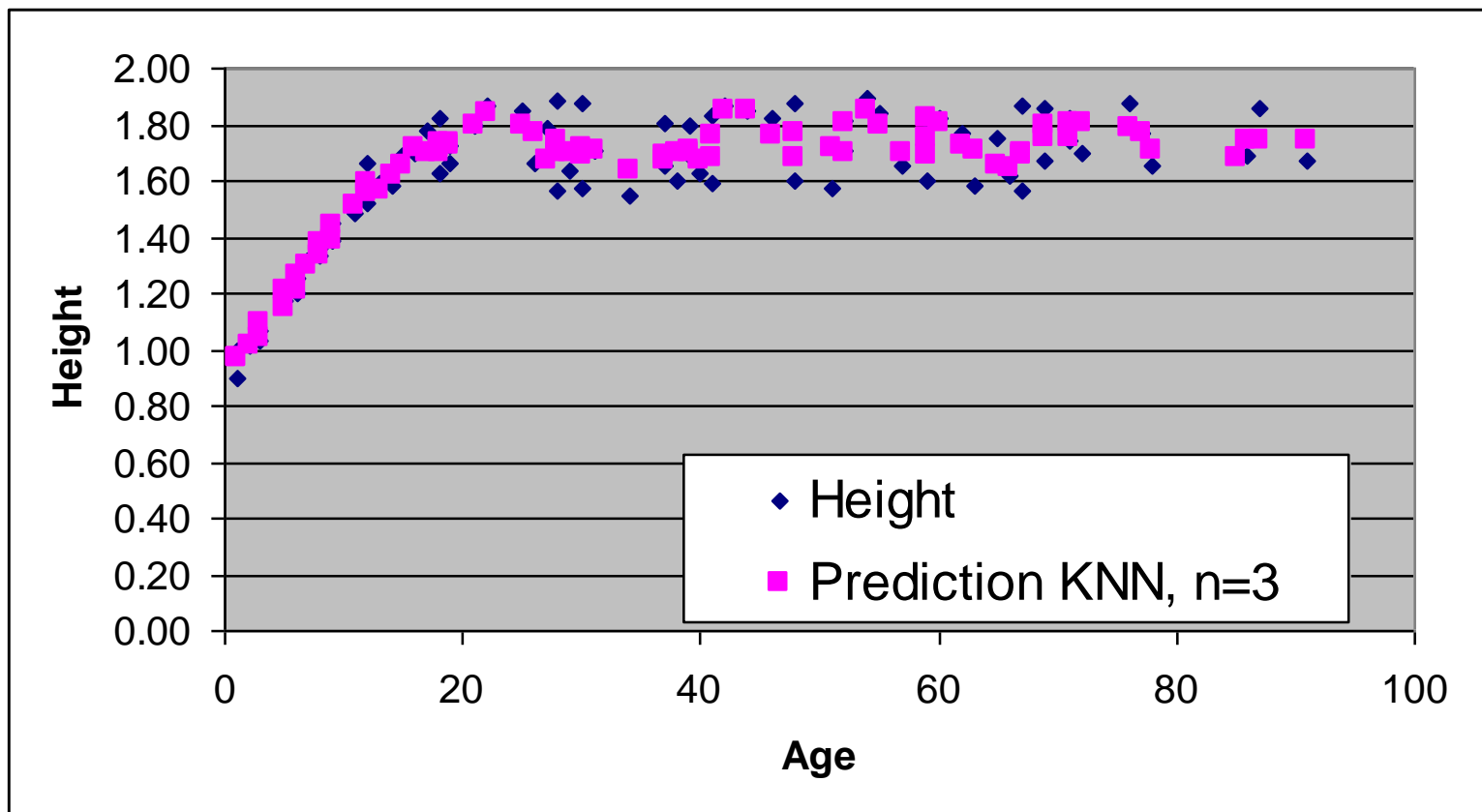


# Model tree



# kNN – K nearest neighbors

- Looks at K closest examples (by age) and predicts the average of their target variable
- K=3



# Which predictor is the best?

Age	Height	Baseline	Linear regression	Regression tree	Model tree	kNN
2	0.85	1.63	1.43	1.39	1.20	1.01
10	1.4	1.63	1.47	1.46	1.47	1.51
35	1.7	1.63	1.61	1.71	1.71	1.67
70	1.6	1.63	1.81	1.71	1.75	1.81

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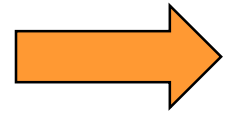
## III. Predictive DM

- Regression

## IV. Descriptive DM

- Predictive vs. descriptive induction
- Subgroup discovery
- Association rule learning
- Hierarchical clustering

# Part IV. Descriptive DM techniques



- Predictive vs. descriptive induction
- Subgroup discovery
- Association rule learning
- Hierarchical clustering

# Descriptive DM:

## Subgroup discovery example - Customer data

Customer	Gender	Age	Income	Spent	BigSpender
c1	male	30	214000	18800	yes
c2	female	19	139000	15100	yes
c3	male	55	50000	12400	no
c4	female	48	26000	8600	no
c5	male	63	191000	28100	yes
O6-O13	...	...	...	...	...
c14	female	61	95000	18100	yes
c15	male	56	44000	12000	no
c16	male	36	102000	13800	no
c17	female	57	215000	29300	yes
c18	male	33	67000	9700	no
c19	female	26	95000	11000	no
c20	female	55	214000	28800	yes

# Customer data: Subgroup discovery

**Type of task:** description (pattern discovery)

**Hypothesis language:** rules  $X \rightarrow Y$ , if X then Y  
X is conjunctions of items, Y is target class

Age > 52 & Sex = male  $\rightarrow$  BigSpender = no

Age > 52 & Sex = male & Income  $\leq$  73250  
 $\rightarrow$  BigSpender = no

# Descriptive DM:

## Association rule learning example - Customer data

Customer	Gender	Age	Income	Spent	BigSpender
c1	male	30	214000	18800	yes
c2	female	19	139000	15100	yes
c3	male	55	50000	12400	no
c4	female	48	26000	8600	no
c5	male	63	191000	28100	yes
O6-O13	...	...	...	...	...
c14	female	61	95000	18100	yes
c15	male	56	44000	12000	no
c16	male	36	102000	13800	no
c17	female	57	215000	29300	yes
c18	male	33	67000	9700	no
c19	female	26	95000	11000	no
c20	female	55	214000	28800	yes



# Customer data: Association rules

**Type of task:** description (pattern discovery)

**Hypothesis language:** rules  $X \rightarrow Y$ , if X then Y  
X, Y conjunctions of items

1. Age > 52 & BigSpender = no  $\rightarrow$  Sex = male
2. Age > 52 & BigSpender = no  $\rightarrow$   
Sex = male & Income  $\leq$  73250
3. Sex = male & Age > 52 & Income  $\leq$  73250  $\rightarrow$   
BigSpender = no

# Descriptive DM:

## Clustering and association rule learning

### example - Customer data

Customer	Gender	Age	Income	Spent	BigSpender
c1	male	30	214000	18800	yes
c2	female	19	139000	15100	yes
c3	male	55	50000	12400	no
c4	female	48	26000	8600	no
c5	male	63	191000	28100	yes
O6-O13	...	...	...	...	...
c14	female	61	95000	18100	yes
c15	male	56	44000	12000	no
c16	male	36	102000	13800	no
c17	female	57	215000	29300	yes
c18	male	33	67000	9700	no
c19	female	26	95000	11000	no
c20	female	55	214000	28800	yes

# Predictive vs. descriptive induction

- **Predictive induction:** Inducing classifiers for solving classification and prediction tasks,
  - Classification rule learning, Decision tree learning, ...
  - Bayesian classifier, ANN, SVM, ...
  - Data analysis through hypothesis generation and testing
- **Descriptive induction:** Discovering interesting regularities in the data, uncovering patterns, ... for solving KDD tasks
  - Symbolic clustering, Association rule learning, Subgroup discovery, ...
  - Exploratory data analysis

# Descriptive DM

- Often used for preliminary explanatory data analysis
- User gets feel for the data and its structure
- Aims at deriving descriptions of characteristics of the data
- Visualization and descriptive statistical techniques can be used

# Predictive vs. descriptive DM: Summary from a rule learning perspective

- **Predictive DM:** Induces **rulesets** acting as classifiers for solving classification and prediction tasks
- **Descriptive DM:** Discovers **individual rules** describing interesting regularities in the data
- **Therefore:** Different goals, different heuristics, different evaluation criteria

# Descriptive DM

- **Description**

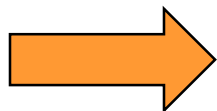
- **Data description and summarization**: describe elementary and aggregated data characteristics (statistics, ...)
- **Dependency analysis**:
  - describe associations, dependencies, ...
  - discovery of properties and constraints

- **Segmentation**

- **Clustering**: separate objects into subsets according to distance and/or similarity (clustering, SOM, visualization, ...)
- **Subgroup discovery**: find unusual subgroups that are significantly different from the majority (deviation detection w.r.t. overall class distribution)

# Part IV. Descriptive DM techniques

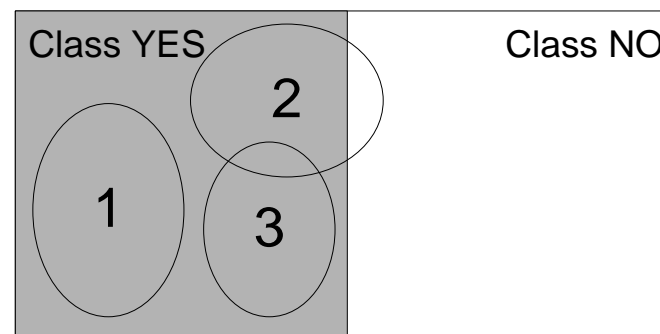
- Predictive vs. descriptive induction
- Subgroup discovery
- Association rule learning
- Hierarchical clustering



# Subgroup Discovery

Person	Age	Spect. presc.	Astigm.	Tear prod.	Lenses
O1	17	myope	no	reduced	NO
O2	23	myope	no	normal	YES
O3	22	myope	yes	reduced	NO
O4	27	myope	yes	normal	YES
O5	19	hypermetrope	no	reduced	NO
O6-O13	...	...	...	...	...
O14	35	hypermetrope	no	normal	YES
O15	43	hypermetrope	yes	reduced	NO
O16	39	hypermetrope	yes	normal	NO
O17	54	myope	no	reduced	NO
O18	62	myope	no	normal	NO
O19-O23	...	...	...	...	...
O24	56	hypermetrope	yes	normal	NO

Subgroup Discovery



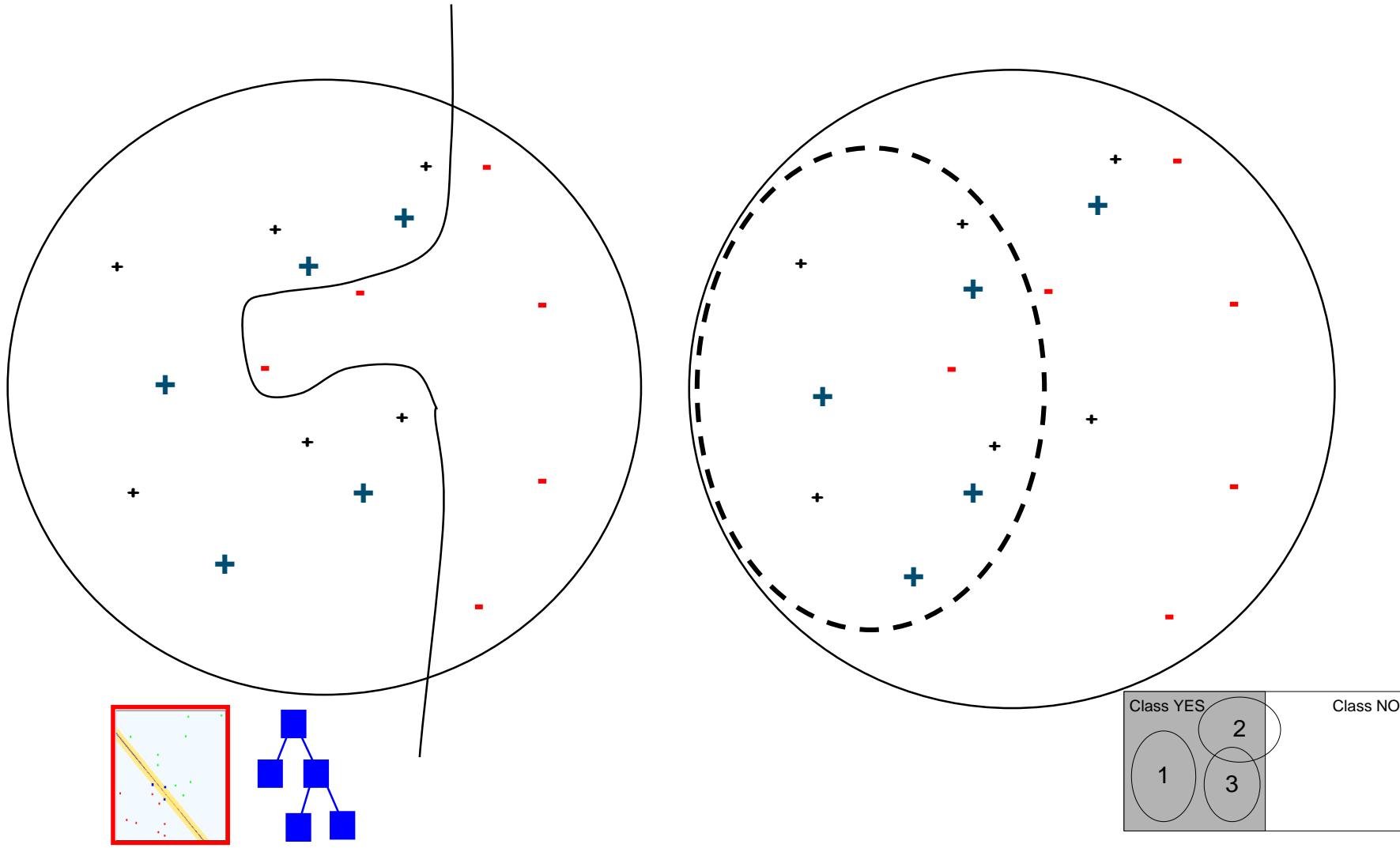
- A task in which individual interpretable patterns in the form of rules are induced from data, labeled by a predefined property of interest.
- SD algorithms learn several independent rules that describe groups of target class examples
  - subgroups must be large and significant



# Classification versus Subgroup Discovery

- **Classification (predictive induction) - constructing sets of classification rules**
  - aimed at learning a model for classification or prediction
  - rules are dependent
- **Subgroup discovery (descriptive induction) – constructing individual subgroup describing rules**
  - aimed at finding interesting patterns in target class examples
    - large subgroups (high target class coverage)
    - with significantly different distribution of target class examples (high TP/FP ratio, high significance, high WRAcc)
  - each rule (pattern) is an independent chunk of knowledge

# Classification versus Subgroup discovery



# Subgroup discovery

Education	Marital Status	Sex	Has Children	Approved
primary	single	male	no	no
primary	single	male	yes	no
primary	married	male	no	yes
university	divorced	female	no	yes
university	married	female	yes	yes
secondary	single	male	no	no
university	single	female	no	yes
secondary	divorced	female	no	yes
secondary	single	female	yes	yes
secondary	married	male	yes	yes
primary	married	female	no	yes
secondary	divorced	male	yes	no
university	divorced	female	yes	no
secondary	divorced	male	no	yes

Approved = yes ← Sex = female

Approved = yes ← Marital status = married

Approved = yes ← Marital status = divorced & Has children = no

Approved = yes ← Education = university

Selected rules discovered by Apriori-SD subgroup discovery algorithm.

# Subgroup discovery in High CHD Risk Group Detection

**Input:** Patient records described by anamnestic, laboratory and ECG attributes

**Task:** Find and characterize population subgroups with high CHD risk (large enough, distributionally unusual)

From **best induced descriptions**, five were selected by the expert as **most actionable** for CHD risk screening (by GPs):

high-CHD-risk ← male & pos. fam. history & age > 46

high-CHD-risk ← female & bodymassIndex > 25 & age > 63

high-CHD-risk ← ...

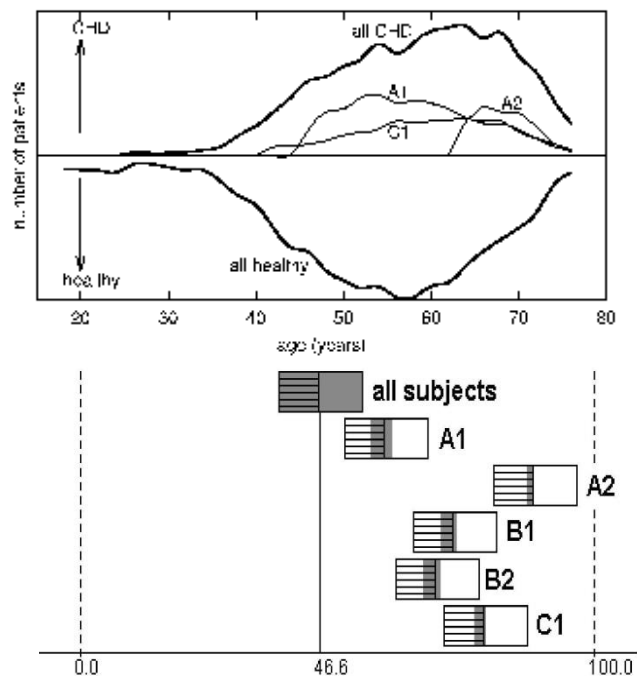
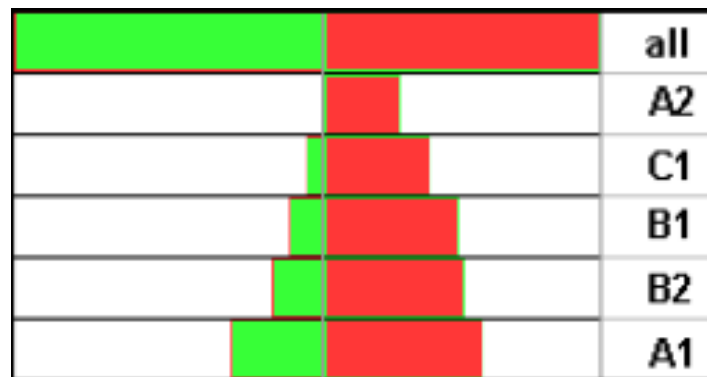
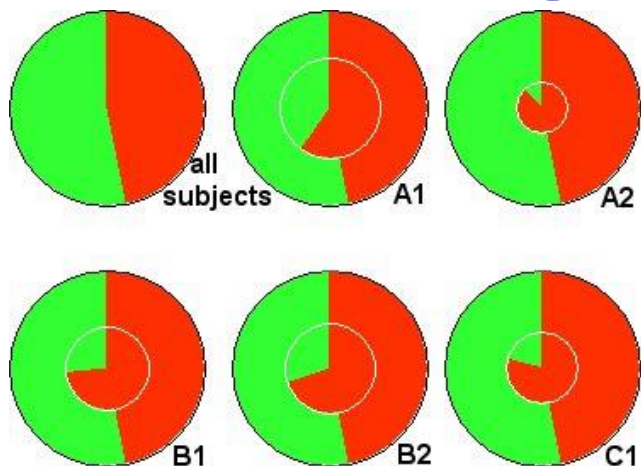
high-CHD-risk ← ...

high-CHD-risk ← ...

# Subgroup Discovery: Medical Use Case

- **Find and characterize population subgroups with high risk for coronary heart disease (CHD)** (Gamberger, Lavrač, Krstačić)
- **A1 for males: principal risk factors**  
CHD ← pos. fam. history & age > 46
- **A2 for females: principal risk factors**  
CHD ← bodyMassIndex > 25 & age > 63
- **A1, A2** (anamnestic info only), **B1, B2** (an. and physical examination), **C1** (an., phy. and ECG)
- **A1: supporting factors** (found by statistical analysis):  
psychosocial stress, as well as cigarette smoking, hypertension and overweight

# Subgroup visualization



**The CHD task:** Find, characterize and visualize population subgroups with high CHD risk (large enough, distributionally unusual, most actionable)

# Subgroup discovery in functional genomics

- Functional genomics is a typical scientific discovery domain, studying genes and their functions
- Very large number of attributes (genes)
- Interesting subgroup describing patterns discovered by SD algorithm

CancerType = Leukemia

IF KIAA0128 = DIFF. EXPRESSED

AND prostoglandin d2 synthase = NOT\_ DIFF. EXPRESSED

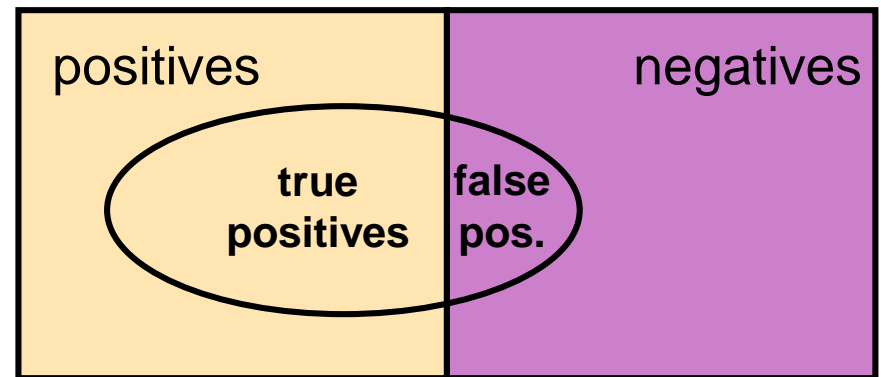
- Interpretable by biologists

D. Gamberger, N. Lavrač, F. Železný, J. Tolar

Journal of Biomedical Informatics 37(5):269-284,

# Subgroups vs. classifiers

- Classifiers:
  - Classification rules aim at pure subgroups
  - A set of rules forms a domain model
- Subgroups:
  - Rules describing subgroups aim at significantly higher proportion of positives
  - Each rule is an independent chunk of knowledge
- Link
  - SD can be viewed as cost-sensitive classification
  - Instead of  $FN_{cost}$  we aim at increased  $TP_{profit}$



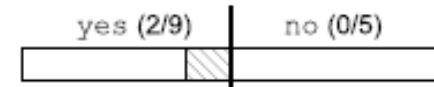


# Recall: Survey data

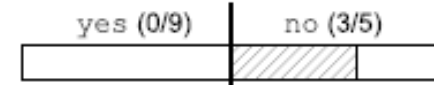
## Classification rule learning

Education	Marital Status	Sex	Has Children	Approved
primary	single	male	no	no
primary	single	male	yes	no
primary	married	male	no	yes
university	divorced	female	no	yes
university	married	female	yes	yes
secondary	single	male	no	no
university	single	female	no	yes
secondary	divorced	female	no	yes
secondary	single	female	yes	yes
secondary	married	male	yes	yes
primary	married	female	no	yes
secondary	divorced	male	yes	no
university	divorced	female	yes	no
secondary	divorced	male	no	yes

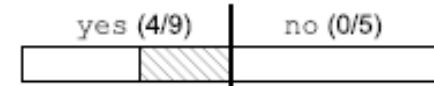
```
IF MaritalStatus = single
  AND Sex = female
THEN Approved = yes
```



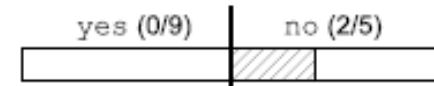
```
IF MaritalStatus = single
  AND Sex = male
THEN Approved = no
```



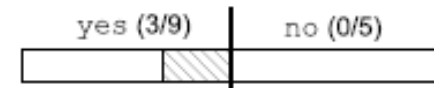
```
IF MaritalStatus = married
THEN Approved = yes
```



```
IF MaritalStatus = divorced
  AND HasChildren = yes
THEN Approved = no
```



```
IF MaritalStatus = divorced
  AND HasChildren = no
THEN Approved = yes
```

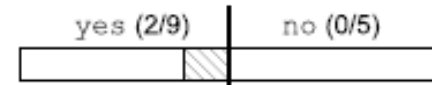


# Survey data

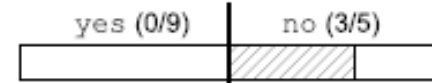
## Subgroup discovery

Education	Marital Status	Sex	Has Children	Approved
primary	single	male	no	no
primary	single	male	yes	no
primary	married	male	no	yes
university	divorced	female	no	yes
university	married	female	yes	yes
secondary	single	male	no	no
university	single	female	no	yes
secondary	divorced	female	no	yes
secondary	single	female	yes	yes
secondary	married	male	yes	yes
primary	married	female	no	yes
secondary	divorced	male	yes	no
university	divorced	female	yes	no
secondary	divorced	male	no	yes

```
IF MaritalStatus = single
  AND Sex = female
THEN Approved = yes
```



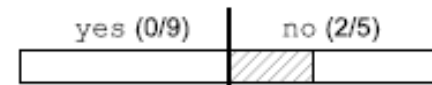
```
IF MaritalStatus = single
  AND Sex = male
THEN Approved = no
```



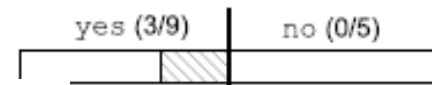
```
IF MaritalStatus = married
THEN Approved = yes
```



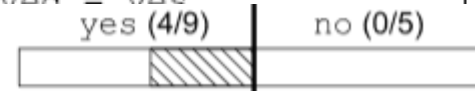
```
IF MaritalStatus = divorced
  AND HasChildren = yes
THEN Approved = no
```



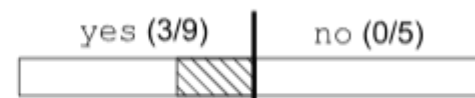
```
IF MaritalStatus = divorced
  AND HasChildren = no
THEN Approved = yes
```



```
IF MaritalStatus = married
THEN Approved = yes
```



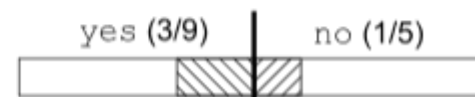
```
IF MaritalStatus = divorced
  AND HasChildren = no
THEN Approved = yes
```



```
IF Sex = female
THEN Approved = yes
```



```
IF Education = university
THEN Approved = yes
```



# Classification Rule Learning for Subgroup Discovery: Deficiencies

- Only first few rules induced by the covering algorithm have sufficient support (coverage)
- Subsequent rules are induced from smaller and strongly biased example subsets (pos. examples not covered by previously induced rules), which hinders their ability to detect population subgroups
- ‘Ordered’ rules are induced and interpreted sequentially as a **if-then-else** decision list

# CN2-SD: Adapting CN2 Rule Learning to Subgroup Discovery

- Weighted covering algorithm
- Weighted relative accuracy (WRAcc) search heuristics, with added example weights
- Probabilistic classification
- Evaluation with different interestingness measures

# CN2-SD: CN2 Adaptations

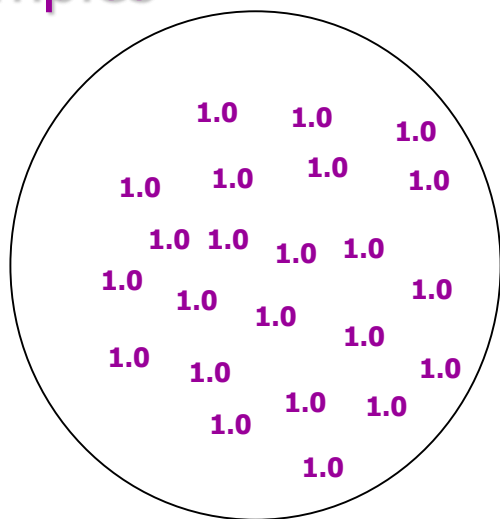
- General-to-specific search (beam search) for best rules
- Rule quality measure:
  - CN2: Laplace:  $\text{Acc}(\text{Class} \leftarrow \text{Cond}) =$   
 $= p(\text{Class}|\text{Cond}) = (n_c + 1) / (n_{\text{rule}} + k)$
  - CN2-SD: **Weighted Relative Accuracy**  
 $\text{WRAcc}(\text{Class} \leftarrow \text{Cond}) =$   
 $p(\text{Cond}) (p(\text{Class}|\text{Cond}) - p(\text{Class}))$
- **Weighted** covering approach (**example weights**)
- Significance testing (likelihood ratio statistics)
- Output: Unordered rule sets (**probabilistic classification**)

# CN2-SD: Weighted Covering

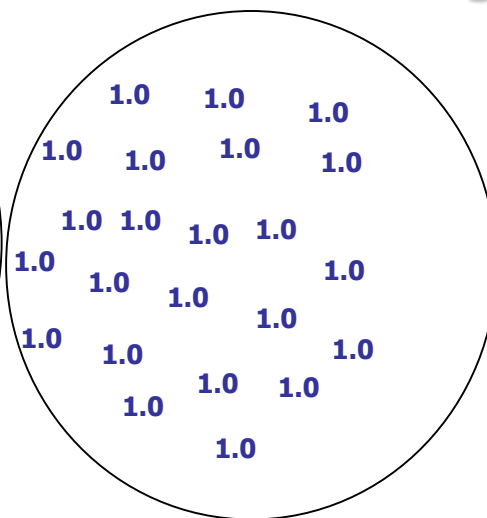
- Standard covering approach:  
covered examples are **deleted** from current training set
- **Weighted covering approach:**
  - weights assigned to examples
  - covered pos. examples are **re-weighted:**  
in all covering loop iterations, store count  $i$  how many times (with how many rules induced so far) a pos. example has been covered:  $w(e,i), w(e,0)=1$ 
    - **Additive weights:  $w(e,i) = 1/(i+1)$**   
 **$w(e,i)$  – pos. example  $e$  being covered  $i$  times**

# Subgroup Discovery

Positive examples



Negative examples

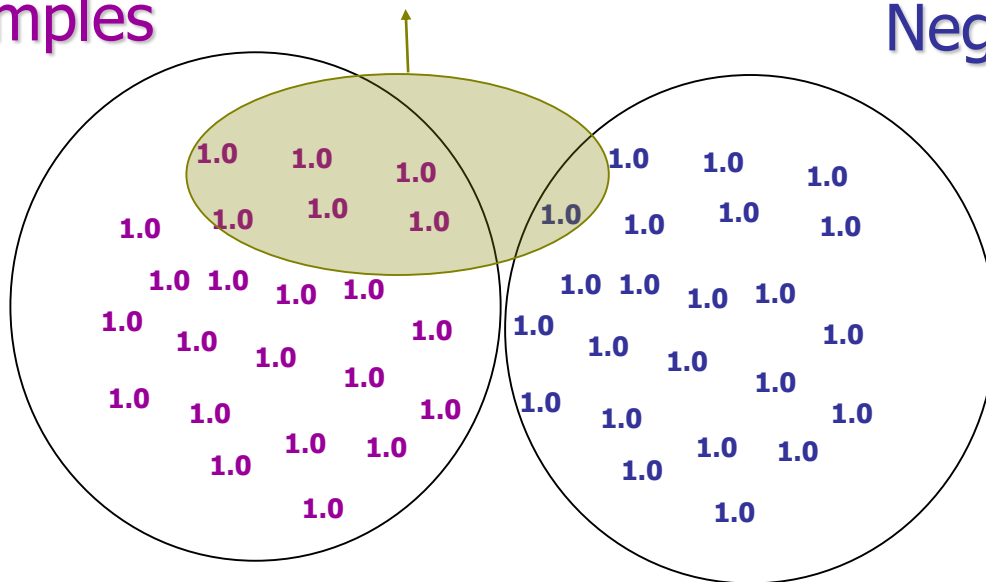


# Subgroup Discovery

Positive examples

Rule1:  $Cl=+$  ← Cond6 AND Cond2

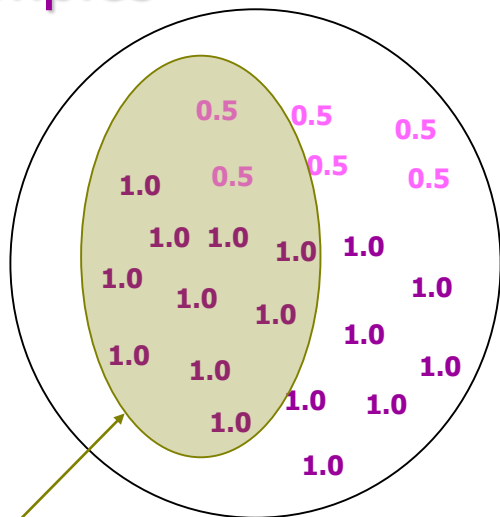
Negative examples



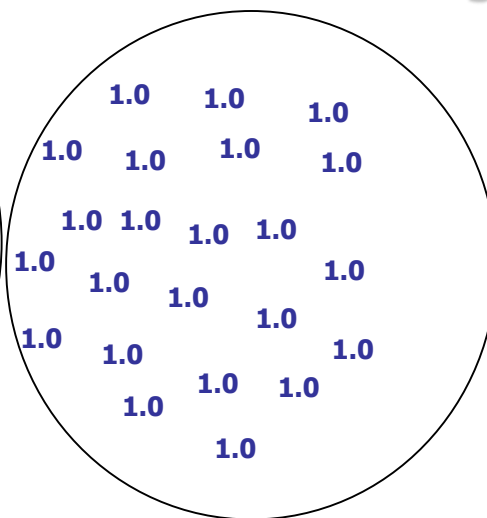


# Subgroup Discovery

Positive examples



Negative examples



Rule2:  $Cl=+$  ← Cond3 AND Cond4



# CN2-SD: Weighted WRAcc Search Heuristic

- **Weighted relative accuracy (WRAcc) search heuristics, with added example weights**

$$\text{WRAcc}(\text{CI} \leftarrow \text{Cond}) = p(\text{Cond}) (p(\text{CI}|\text{Cond}) - p(\text{CI}))$$

increased coverage, decreased # of rules, approx. equal accuracy (PKDD-2000)

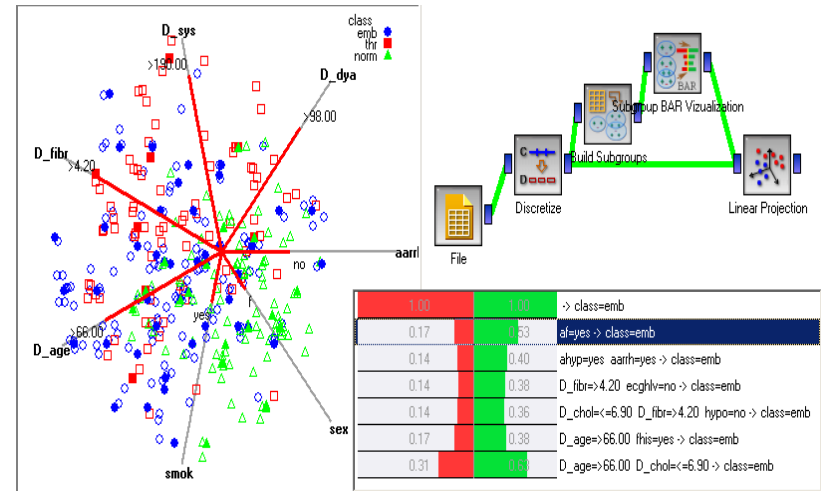
- In WRAcc computation, probabilities are estimated with relative frequencies, adapt:

$$\text{WRAcc}(\text{CI} \leftarrow \text{Cond}) = p(\text{Cond}) (p(\text{CI}|\text{Cond}) - p(\text{CI})) = \\ n'(\text{Cond})/N' ( n'(\text{CI}.\text{Cond})/n'(\text{Cond}) - n'(\text{CI})/N' )$$

- $N'$  : sum of weights of examples
- $n'(\text{Cond})$  : sum of weights of all covered examples
- $n'(\text{CI}.\text{Cond})$  : sum of weights of all correctly covered examples

# SD algorithms in the Orange DM Platform

- **Orange** data mining toolkit
  - classification and subgroup discovery algorithms
  - data mining workflows
  - visualization

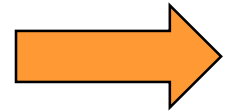


## ■ SD Algorithms in Orange

- SD (Gamberger & Lavrač, JAIR 2002)
- Apriori-SD (Kavšek & Lavrač, AAI 2006)
- CN2-SD (Lavrač et al., JMLR 2004): Adapting CN2 classification rule learner to Subgroup Discovery

# Part IV. Descriptive DM techniques

- Predictive vs. descriptive induction
- Subgroup discovery
- Association rule learning
- Hierarchical clustering



# Association Rule Learning

**Rules:**  $X \Rightarrow Y$ , if  $X$  then  $Y$

$X$  and  $Y$  are itemsets (records, conjunction of items), where items/features are binary-valued attributes)

**Given:** Transactions

	i1	i2	.....	i50
itemsets (records)	t1	1	1	0
	t2	0	1	0
	...	.....	.....	.....

**Find:** A set of association rules in the form  $X \Rightarrow Y$

**Example:** Market basket analysis

beer & coke  $\Rightarrow$  peanuts & chips (0.05, 0.65)

- Support:  $\text{Sup}(X, Y) = \#XY/\#D = p(XY)$
- Confidence:  $\text{Conf}(X, Y) = \#XY/\#X = \text{Sup}(X, Y)/\text{Sup}(X) = p(XY)/p(X) = p(Y|X)$

# Association Rule Learning: Examples

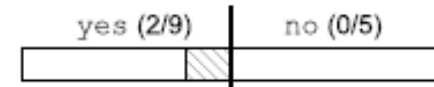
- Market basket analysis
  - beer & coke  $\Rightarrow$  peanuts & chips (5%, 65%)  
(IF beer AND coke THEN peanuts AND chips)
  - Support 5%: 5% of all customers buy all four items
  - Confidence 65%: 65% of customers that buy beer and coke also buy peanuts and chips
- Insurance
  - mortgage & loans & savings  $\Rightarrow$  insurance (2%, 62%)
  - Support 2%: 2% of all customers have all four
  - Confidence 62%: 62% of all customers that have mortgage, loan and savings also have insurance

# Recall: Survey data

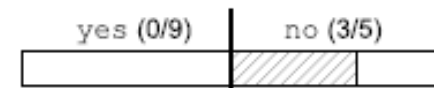
## Classification rule learning

Education	Marital Status	Sex	Has Children	Approved
primary	single	male	no	no
primary	single	male	yes	no
primary	married	male	no	yes
university	divorced	female	no	yes
university	married	female	yes	yes
secondary	single	male	no	no
university	single	female	no	yes
secondary	divorced	female	no	yes
secondary	single	female	yes	yes
secondary	married	male	yes	yes
primary	married	female	no	yes
secondary	divorced	male	yes	no
university	divorced	female	yes	no
secondary	divorced	male	no	yes

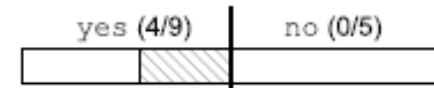
```
IF MaritalStatus = single
  AND Sex = female
THEN Approved = yes
```



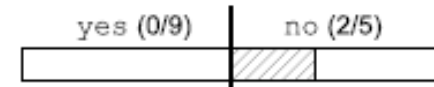
```
IF MaritalStatus = single
  AND Sex = male
THEN Approved = no
```



```
IF MaritalStatus = married
THEN Approved = yes
```



```
IF MaritalStatus = divorced
  AND HasChildren = yes
THEN Approved = no
```



```
IF MaritalStatus = divorced
  AND HasChildren = no
THEN Approved = yes
```



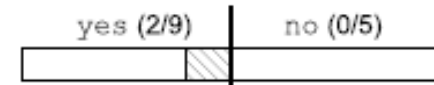


# Survey data

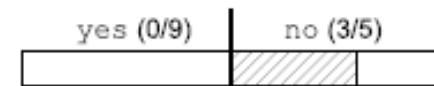
## association rule learning

Education	Marital Status	Sex	Has Children	Approved
primary	single	male	no	no
primary	single	male	yes	no
primary	married	male	no	yes
university	divorced	female	no	yes
university	married	female	yes	yes
secondary	single	male	no	no
university	single	female	no	yes
secondary	divorced	female	no	yes
secondary	single	female	yes	yes
secondary	married	male	yes	yes
primary	married	female	no	yes
secondary	divorced	male	yes	no
university	divorced	female	yes	no
secondary	divorced	male	no	yes

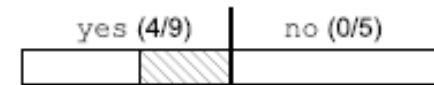
IF MaritalStatus = single  
AND Sex = female  
THEN Approved = yes



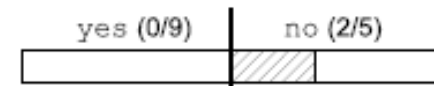
IF MaritalStatus = single  
AND Sex = male  
THEN Approved = no



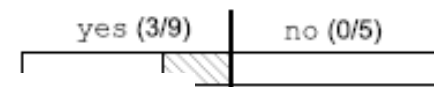
IF MaritalStatus = married  
THEN Approved = yes



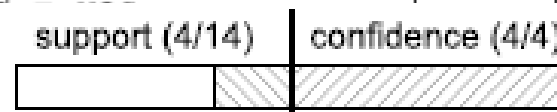
IF MaritalStatus = divorced  
AND HasChildren = yes  
THEN Approved = no



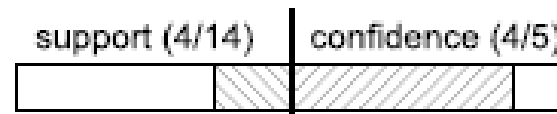
IF MaritalStatus = divorced  
AND HasChildren = no



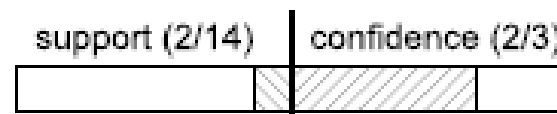
IF Education = university  
THEN Sex = female



IF Approved = no  
THEN Sex = male



IF Education = secondary  
AND MaritalStatus = divorced  
THEN HasChildren = no  
AND Approved = yes



# Association Rule Learning

**Given:** a set of transactions  $D$

**Find:** all association rules that hold on the set of transactions that have

- user defined minimum support, i.e., support  $>$  **MinSup**, and
- user defined minimum confidence, i.e., confidence  $>$  **MinConf**

It is a form of exploratory data analysis, rather than hypothesis verification

# Searching for the associations

- Find all large itemsets
- Use the large itemsets to generate association rules
- If  $XY$  is a large itemset, compute
$$r = \text{support}(XY) / \text{support}(X)$$
- If  $r > \text{MinConf}$ , then  $X \Rightarrow Y$  holds  
(support  $>$  MinSup, as  $XY$  is large)

# Large itemsets

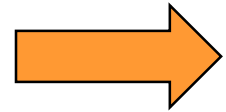
- Large itemsets are itemsets that appear in at least MinSup transaction
- All subsets of a large itemset are large itemsets (e.g., if A,B appears in at least MinSup transactions, so do A and B)
- This observation is the basis for very efficient algorithms for association rules discovery (linear in the number of transactions)

# Association vs. Classification rules

- Exploration of dependencies
  - Different combinations of dependent and independent attributes
  - Complete search (all rules found)
- Focused prediction
  - Predict one attribute (class) from the others
  - Heuristic search (subset of rules found)

# Part IV. Descriptive DM techniques

- Predictive vs. descriptive induction
- Subgroup discovery
- Association rule learning
- Hierarchical clustering



# Hierarchical clustering

- **Algorithm** (agglomerative hierarchical clustering):

Each instance is a cluster;

repeat

find **nearest** pair  $C_i$  in  $C_j$ ;

**fuse**  $C_i$  in  $C_j$  in a new cluster

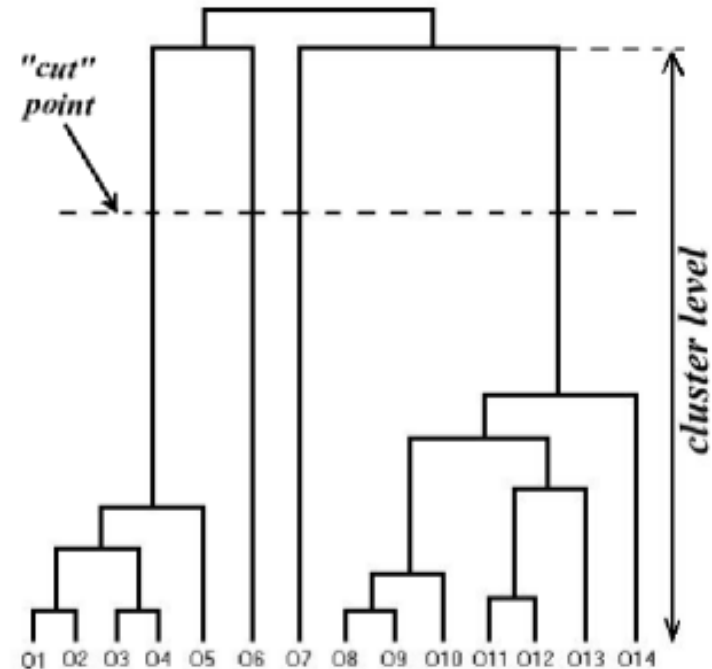
$C_r = C_i \cup C_j$ ;

determine **dissimilarities** between

$C_r$  and other clusters;

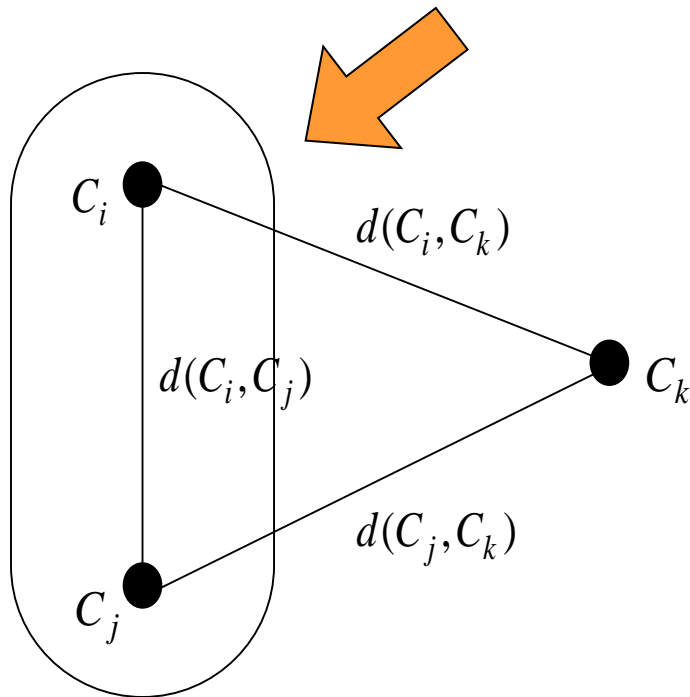
until one cluster left;

- **Dendrogram:**



# Hierarchical clustering

- Fusing the nearest pair of clusters

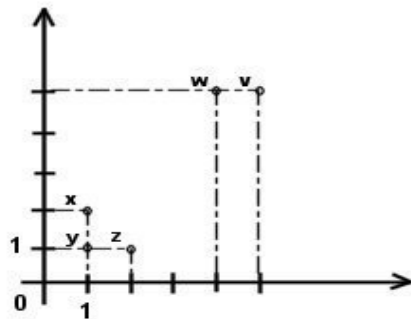


- Minimizing intra-cluster similarity
- Maximizing inter-cluster similarity

- Computing the dissimilarities from the “new” cluster



# Hierarchical clustering: example



a) sample problem

	x	y	z	w	v
x	0	1	1	5	5.66
y		0	1.41	4.24	5
z			0	4.47	5
w				0	1
v					0

b) dissimilarity matrix

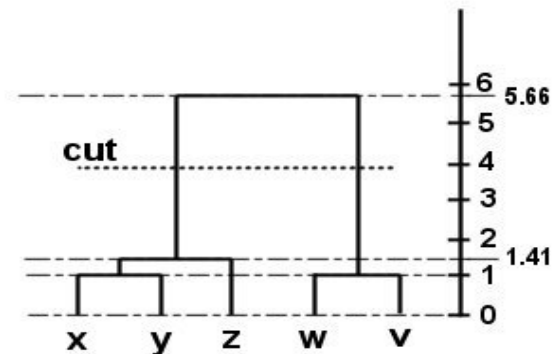
	(x,y)	z	w	v
(x,y)	0	1.41	5	5.66
z		0	4.47	5
w			0	1
v				0

c) dissimilarity matrix after 'fusing' elements **x** and **y**

	(x,y)	z	(w,v)
(x,y)	0	1.41	5.66
z		0	5
(w,v)			0

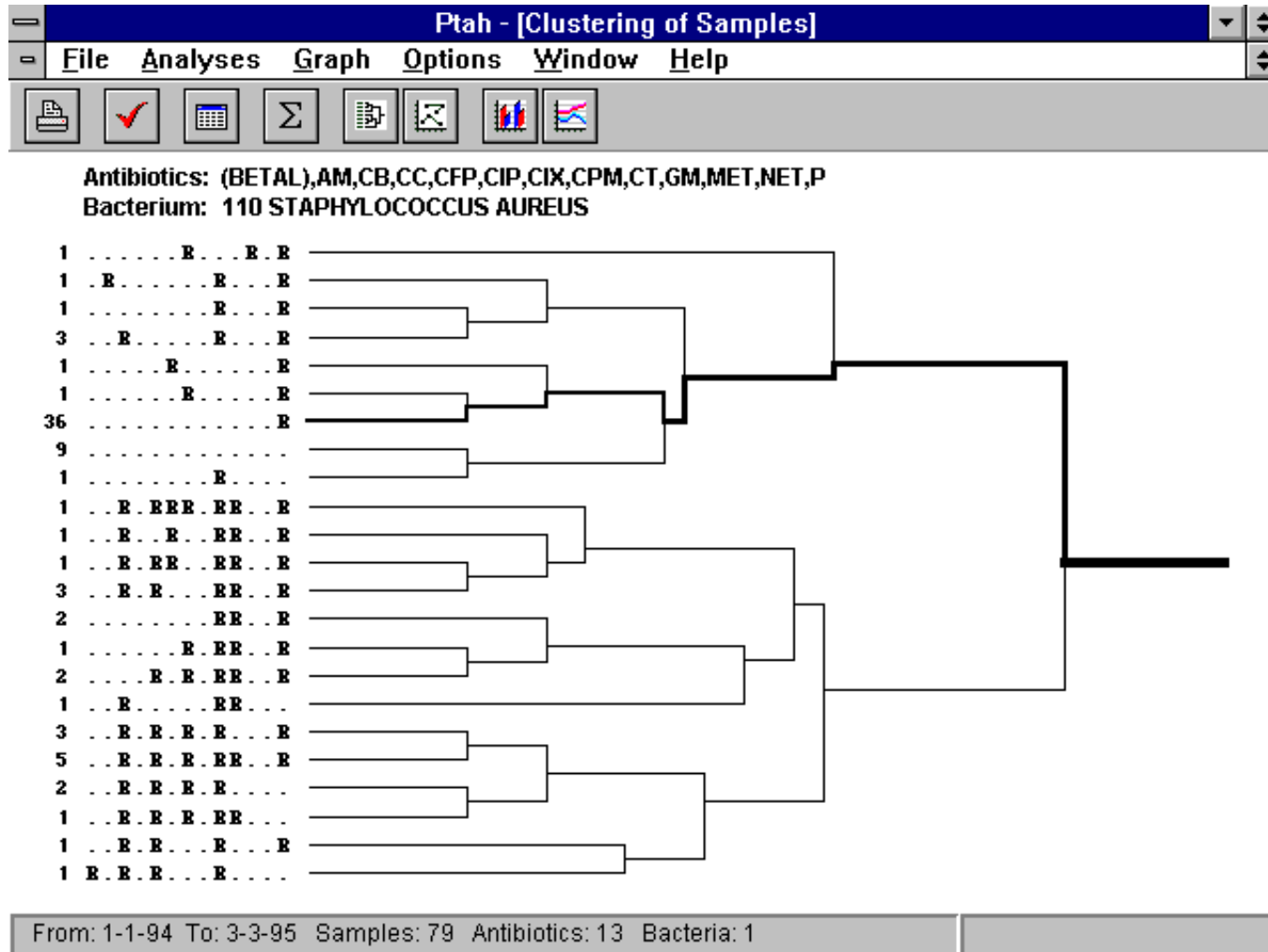
d) dissimilarity matrix after 'fusing' elements **w** and **v**

	(x,y,z)	(w,v)
(x,y,z)	0	5.66
(w,v)		0

e) dissimilarity matrix after 'fusing' cluster **(x,y)** and element **z**

f) dendrogram

# Results of clustering



A dendrogram of resistance vectors

[Bohanec et al., "PTAH: A system for supporting nosocomial infection therapy", IDAMAP book, 1997]

# Course Outline

## I. Introduction

- Data Mining and KDD process
- Introduction to Data Mining
- Data Mining platforms

## II. Predictive DM

- Decision Tree learning
- Bayesian classifier
- Classification rule learning
- Classifier evaluation

## III. Predictive DM

- Regression

## IV. Descriptive DM

- Predictive vs. descriptive induction
- Subgroup discovery
- Association rule learning
- Hierarchical clustering